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3/17/65
ABSOLUTE TOTAL APPARENT IONIZATION, ELECTRON STRIPPING, 
ELECTRON CAPTURE, AND PARTIAL IONIZATION CROSS SECTIONS 
IN THE ENERGY RANGE 0.15 - 1.00 MeV

A THESIS
Presented to 
The Faculty of the Graduate Division
by
Lawrence Jackson Puckett

In Partial Fulfillment
of the Requirements for the Degree 
Doctor of Philosophy 
in the School of Physics

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December, 1966
ABSOLUTE TOTAL APPARENT IONIZATION, ELECTRON STRIPPING, ELECTRON CAPTURE, AND PARTIAL IONIZATION CROSS SECTIONS IN THE ENERGY RANGE 0.15 - 1.00 MeV

Approved:  
Chairman

Date approved by Chairman: Jan. 3, 1967
This thesis is gratefully dedicated

to my wife Anne,

my daughter Lynne,

and my son David.
ACKNOWLEDGMENTS

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SUMMARY

Absolute total apparent cross sections have been measured for the processes leading to electron and ion production in the gases He, Ar, H₂, and N₂ by incident beams of He⁺⁺, He⁺, and H⁺ in the energy range 0.15 to 1.00 MeV. From these measurements absolute total apparent cross sections for ionization, electron capture, and stripping were deduced. In the same energy range, the relative cross sections were measured for production of He⁺ and He⁺⁺ in helium gas by incident H⁺. These relative cross sections were normalized through the use of previous measurements made in this laboratory to obtain absolute cross sections. Also, preliminary results are presented on the cross sections for production of Ar⁺ through Ar⁴⁺ in argon gas by fast H⁺.

The primary source of the fast beams used in this investigation was a 1 MV Van de Graaff positive ion accelerator. The beams of H⁺, He⁺, and He⁺⁺ were obtained by allowing the H⁺ and He⁺ beams supplied by the accelerator to undergo charge changing collisions in a gas cell. The composite beam that emerged from the gas cell was separated into its various charge components in an electrostatic analyzer. The beam of the selected charge state was then passed into the collision region of the apparatus which followed.

For measurements of the total apparent electron and ion production cross sections, the collision chamber employed in the apparatus contained two parallel arrays of plates (arranged like a condenser) between which the beam passed. The slow ions and electrons created in the beam collisi-
sions with the gas were collected on these plates by a uniform electro-
static collection field. The currents produced by the collected electrons
and ions were measured on sensitive electrometers. The fast beams were
trapped in a detector that served any one of three purposes. It could be
used to measure (1) the net current of the beam, (2) the secondary emission
current produced by the beam striking a copper foil in the detector, or
(3) the net beam power, from which the "particle-current" for a neutral
beam could be determined. The target gas pressure was measured by means
of a cold-trapped McLeod gauge, and the possible errors associated with
the use of this type of gauge are extensively discussed.

The present measurements of the total apparent electron capture
cross sections for incident He$^{++}$ are compared with the results obtained
contrast to the present results, all of the comparison results were ob-
tained in experiments that employed the observation of the change in the
charge state of the fast beam. The agreement between the present results
and those shown for comparison is generally good. It is pointed out that
the disagreement among some of the comparison results is beyond the ex-
perimental errors.

The present measurements of the total apparent ionization cross
sections for He$^{0}$ and H$^{0}$ projectiles are compared with those results of
E. S. Solov'ev, et al. extending up to 0.18 MeV. Their comparison results
were obtained in a similar apparatus to that which was used in the present
experiment. Comparisons were also made with theoretical calculations of
the ionization of H$^{0}$ by incident H$^{0}$ (D. R. Bates and G. Griffing) and by
He$^{0}$ (D. R. Bates and A. Williams). Simple procedures were used to scale
the theoretical results for the atomic target to the molecular target used in this experiment and agreement within the experimental error limits was obtained in every case.

The total stripping cross sections for the $H^0$ projectile were compared with the results of Solov'ev and C. F. Barnett, et al. Comparisons were also made with the theoretical cross section for stripping of $H^0$ incident on $H^0$ (Bates and Griffing)—scaled to a molecular hydrogen target—and with the calculation of the stripping of $H^0$ incident on He (Bates and Williams). The present results agree within the experimental error limits with Barnett's results and with theory, and in most cases with the results of Solov'ev. Reasons are presented to support the belief that the present results are more accurate than those of Solov'ev.

The results obtained with the $He^0$ projectile for the total apparent ionization cross sections are generally in good agreement with those of Solov'ev. However, the total apparent stripping cross sections in both the present and Solov'ev's results for the $He^0$ projectile were usually about 40 percent greater than similar quantities measured by Allison, Pivovar, et al., and Barnett, et al. Conclusions pertaining to this discrepancy are discussed.

The present results for the total apparent ionization cross sections are combined with those for $H^+ \text{ and } He^+$, which were previously measured in this laboratory, to provide a general comparison for all of the hydrogen and helium projectiles. The functional dependence of the ionization cross sections derived from the Bethe-Born approximation predicts that point charge projectiles of equal charge and velocity should have equal cross sections. In this cross section expression, the scaling pro-
procedure between various point-charge projectiles is straightforward and was used to compare the $H^+$ and $He^{++}$ cross sections at equivelocity. In the upper energy range of this investigation, the agreement was quite good.

The Bethe-Born cross section expression is strictly valid only for point-charge ions, and therefore it was of interest to determine the relationship between the non-point-charge atomic projectiles ($He^0$ and $H^0$) and the point-charge ions ($H^+$ and $He^{++}$). It was found that the ionization cross sections for incident $H^0$ were uniformly lower than those of $H^+$ by a factor of 0.64 in all four target gases. This constant offset in the $H^0$ curve implied that the $H^0$ projectile exhibited an effective charge equal to $\sqrt{0.64} = 0.80$ of the proton charge. However, the same sort of uniform offset in the $He^0$ cross section curves was not observed. In fact the separation of the two curves ranged from about zero to $He^0$ being about a factor of 1.2 greater than $H^+$. It is concluded that the Born approximation calculations for the ionization collisions observed in this experiment are essentially correct for velocities greater than about $5 \times 10^6$ m/sec, and in some cases agreement between experimental and theoretical results is obtained at even lower velocities.

A completely different apparatus was employed for the measurement of the relative cross sections for production of ions of specified charge states. In this apparatus, the collision chamber was located on top of a vertical axle. The slow ion spectrometer and beam detector were mounted on rather massive counterbalanced supports affixed to separately rotate on precision bearings about the common axle. The beam collimator, the spectrometer collimator, and the beam detector protruded through flexible
bellows into the chamber and were aimed at a common point on the rotation axis.

The detector for the proton beam was a shielded Faraday cup. The spectrometer employed a set of accelerating and focusing electrodes for the slow recoil ions and a 60° sector magnetic field for charge-to-mass and momentum analyses of the ions in a 5 cm radius-of-curvature geometry. Postanalysis acceleration into an electron multiplier detector was employed to provide near 100 percent ion detection efficiency.

In this apparatus, the beam was allowed to undergo collisions in two different environments. When a determination of the angular distribution of the recoil ions was attempted, a field-free collision region was employed. However, when the results showed no perceptible angular dependence, tests were undertaken which demonstrated that virtually all of the recoil ions had energies considerably less than two electron volts. Even so, it was expected that the angular spectrum of the recoil ions would be sharply peaked around 90°. However, considerations of the thermal motion of the target gas indicated that the expected peaks in the angular distribution, corresponding to the low energy ions that were observed, would be so broadened as to be difficult to detect. It was concluded that a heavy projectile-target combination was necessary to produce sufficient energy transfer so that the thermal motion of the target would not mask the angular distribution of the recoil ions. It was also concluded for the case of H⁺ incident on He that a collection field could be reliably and efficiently employed to sweep the ions into the spectrometer. The measurements with a collection field served to determine the relative cross sections for production of variously charged ions irrespective of their recoil an-
Excellent agreement was obtained between the present cross sections for production of \( \text{He}^+ \) and \( \text{He}^{++} \) and those of Solov'ev up to 0.18 MeV and Wexler extending upwards from 0.80 MeV. It was observed that the cross section for production of \( \text{He}^{++} \) was less than one percent of the total ionization cross sections for all but the lowest energies employed in this investigation. In accordance with the prediction of the Born approximation, good agreement was obtained at the higher energies between the cross sections for production of \( \text{He}^+ \) by protons and equivelocity electrons. However, for the \( \text{He}^{++} \) production, the electron cross sections were about a factor of two larger. It thus appeared that the scaling procedure suggested by the form of the Born cross section expression was not as applicable to multiple ionization as for single (or total) ionization cross sections.

Preliminary cross section results are presented for the formation of the first four ions in argon by incident protons. Generally good agreement was obtained between the present results and those of Solov'ev and Wexler for the first two ions. However, for \( \text{Ar}^{3+} \) the present results are about a factor of ten greater than those of Solov'ev, and in rather good agreement with Wexler, whose extrapolated results are about a factor of eight greater than those of Solov'ev.

It appears that the equivelocity electron cross sections for multiple ionization of argon are in substantially better agreement with the proton cross sections than they were in the helium target. Perhaps this indicates that the assumptions in the Born approximation are valid to
lower velocities for a light target such as helium.

Numerous tests were employed, and the results are discussed, to establish the validity of all of the cross section measurements presented herein.
CHAPTER I

INTRODUCTION

This investigation concerned the measurement of the total apparent cross sections for ion and electron production, from which apparent ionization, electron capture, and stripping cross sections were deduced. Also measured, in a separate apparatus, were the cross sections for production of slow ions of specified charge state, which, hereinafter, will be denoted as "partial ionization cross sections." The ionizing projectiles are helium and hydrogen ions and atoms in the energy range from 0.15 to 1.00 MeV. This cross section terminology is explained in detail in Chapter II; however, in order to understand the following remarks, it is sufficient to note that a measurement of a cross section for a particular event is related to the probability that the event will occur.

The ionizing and charge changing collisions associated with the passage of ions and atoms through gaseous targets are of both theoretical and applied value. Several direct practical applications are found, for example, in the field of controlled thermonuclear research. A common method of supplying a plasma with ions is through high energy injection into the containment vessel. The two problems that arise here are concerned with trapping and containment inside the vessel. In trapping a beam incident into the containment field from outside, the interest is in:

a. dissociation cross sections for the case of molecular ion injection;
b. ionization cross sections for the case of neutral particle injection, and

c. formation of excited states for the trapping of excited neutrals by Lorentz ionization.

Consequently, a knowledge of the ionization cross sections for light high energy projectiles in various gases is of significant value.

In containment of a plasma for a sufficient time to allow it to react efficiently, when it is already trapped, the main interest is in charge changing collisions in background gas, leading to loss of ions from the plasma. In addition, these cross sections enter into consideration of a number of upper atmospheric phenomena. The density of ions and electrons in the upper atmosphere is determined to some extent by ionizing and charge changing reactions for particles from space. The capture and loss mechanisms of the Van Allen radiation belts depend on these cross sections, as well as the operation of simple laboratory gas-filled particle detectors.

A fundamental theoretical value of these measurements is that they provide checks on calculations of the magnitudes and energy dependencies for the cross sections. In principle, quantum mechanical calculations could be made for any atomic collision process if a complete set of wave functions for the partners in a collision were known. However, detailed theoretical calculations have been made only for the simplest cases, i.e., those involving electrons, protons, neutral hydrogen atoms, and singly and doubly charged helium ions as projectiles incident on targets of atomic hydrogen, helium, and lithium. Even for most of these simple cases the calculations were difficult and involved approximations whose validity
is difficult to assess except by resort to comparison with experimental results.

Most of the existing calculations for ionization processes at high energies have been made in the Born approximation. A very valuable check on this approximation is possible in the present experiment, because the projectile energies extend well into the asymptotic region where the approximation is expected to be valid.

The early experimental investigations of ionization by fast ions and atoms prior to 1951 has been thoroughly surveyed by Massey and Burbury. The experimental work published up through the beginning of 1965 is well covered by the surveys of Allison, Allison and Garcia-Munoz, Fedorenko, McDaniel, and Nikolaev.

It should be noted that the present investigation is divided into two rather distinct phases, and the thesis is accordingly divided into Part A, which deals with the aspects common to both phases, and into Parts B and C, which deal with the separate phases of investigation. Part A (Chapters II-III) contains a general introduction to the phenomena associated with the passage of high energy particles through a gas, and specifically the methods employed to obtain the high energy particle beams used in this experiment. Part B (Chapters IV-V) deals with the measurement techniques, the apparatus, and the results for the total apparent cross sections, while Part C (Chapters VI-VIII) pertains to the techniques, apparatus, and results for the measurements of the partial ionization cross sections.

The present results for the total apparent ionization cross sections and the partial ionization cross sections represent an extension into a
hitherto unexplored energy range for the $H^0$, $He^0$, and $He^{++}$ projectiles. However, Soloviev, et al. have published measurements up to 0.18 MeV on these total and partial cross sections and they are shown for comparison with the present results in Chapters V and VIII. During the period of this investigation, Wexler performed some measurements on the partial ionization cross sections in the energy range 0.80 to 3.75 MeV. These results are also shown for comparison with the present measurements.

The results of the investigators mentioned thus far are the only measurements that compare with the directly observed quantities in this work. However, from the direct measurements of this investigation, the total apparent electron capture cross section for the ionic projectile, and the total apparent stripping cross sections for the atomic projectiles may be deduced as explained in Chapter II. The experimental results of Allison, Pivovar, et al., Barnett, et al., and Nikolaev, et al. on the electron capture and stripping cross sections, together, completely span the energy range of this work and serve as comparisons for the present data.

As was previously mentioned, theoretical calculations of these cross sections are available only for the simplest cases; those that are pertinent to this investigation are the following:

1. ionization of atomic hydrogen by $H^+$ (Bates and Griffing);
2. ionization of atomic hydrogen by $He^+$ (Boyd, et al.);
3. ionization of helium by $H^+$ (Mapleton);
4. stripping of atomic hydrogen projectiles in collision with helium, or conversely, ionization of atomic hydrogen by incident $He^0$ (Bates and Williams); and
5. stripping of atomic hydrogen on atomic hydrogen, or conversely, ionization of atomic hydrogen by atomic hydrogen (Bates and Griffing 19).

It should be noted, however, that the present investigation did not include an atomic hydrogen target. Consequently, all of the calculations on atomic hydrogen were approximately scaled to a molecular hydrogen target. The scaling procedure used is discussed in each case as it is presented.
CHAPTER II

PHENOMENA ASSOCIATED WITH THE PASSAGE OF A
FAST BEAM OF IONS OR ATOMS THROUGH A GAS

The passage of a fast beam of ions or atoms through a gas leads
to both elastic and inelastic collisions between the projectile and tar-
get particles. An elastic collision may be defined as one in which the
kinetic energy of the system is conserved. This implies that there is
no change in the total internal energy of the system. In contrast to
this type of interaction is the inelastic collision in which an exchange
of kinetic and internal energy occurs. This exchange of energy can as-
sume many forms, but it is possible to divide them, according to the
observed quantities, into two major groups:

(1) the excitation collision, which is characterized by a change
in the atomic state of one or more electrons, or a change in the vibra-
tional or rotational states of the system; and

(2) the charge changing collision, which occurs when the change
in internal energy of either particle is sufficient to lead to the ejec-
tion of one or more free electrons, or the transfer of electrons between
particles.

The latter type of collision involves the strongest of the two inter-
actions, and it is this type of collision with which the present investi-
gation is concerned.

For the purpose of this discussion, it should be noted that there
are three significantly distinct types of collisions that fall under the
general category of charge changing collisions as defined above. These
are:

(1) the ejection of free electrons from the target,
(2) the capture by the projectile of some of the electrons from
the target, and
(3) the ejection of free electrons from the projectile.

The cross section referring to interaction (1) will be designated
as "pure ionization," or more simply, "ionization"; the cross section for
(2) as "electron capture"; and the cross section for (3) as "stripping."
It is possible to have combinations of these three types of events, par-
ticularly when many electrons are being rearranged as in the case of col-
lisions between heavy particles.

To illustrate the multiplicity of events that may follow from high
energy collisions, the case of fast hydrogen atoms incident on helium was
chosen for discussion, because it is both simple and yet representative
of the interactions that occurred in this experiment. The heavier tar-
gets such as argon, of course, make the number of possible kinds of events
more numerous, simply because of the larger number of electrons that may
participate in the collision. A further increase in the multiplicity of
events arises when molecular targets are used, for these may lead to dis-
sociation fragments that may themselves be multiply ionized. Therefore,
to keep the discussion free of unnecessary details, a list of possible
reactions for the projectile-target combination of H\(^{+}\) on He is presented
in Equations 1-5 on the following page.
The interpretation of the symbols appearing in reaction equations is, from left to right, first the projectile and its charge state, and second the target, before the collision; following the arrow sign, the first symbol indicates the charge state of the projectile, and the remaining symbols, the character of the target molecule, after the collision. The cross section symbols that appear to the right will be explained shortly.

The projectile may or may not have experienced a change in its charge state as a result of the interaction, but in either case both theory and experiment show that it retains essentially all of its initial kinetic energy. However, the kinetic energy acquired by the target may be substantial, although it is small compared to that of the projectile, and as was previously mentioned, the target may be dissociated in addition to changing its charge state.

Reactions 1 and 2 are the only simple ionization events. Reaction 3 is the only simple stripping event. Reactions 4 and 5 represent combinations of the two preceding events. It should be noted that no electron capture event is shown for this projectile-target combination. It has

<table>
<thead>
<tr>
<th>Reactants</th>
<th>Reaction Products</th>
<th>Cross Section</th>
</tr>
</thead>
<tbody>
<tr>
<td>$H^0 + He^0$</td>
<td>$H^0 + He^+ + e$</td>
<td>$\sigma_{c1}$</td>
</tr>
<tr>
<td>$\rightarrow$</td>
<td>$H^0 + He^{++} + 2e$</td>
<td>$\sigma_{c2}$</td>
</tr>
<tr>
<td>$\rightarrow$</td>
<td>$H^+ + He^0 + e$</td>
<td>$\sigma_{c10}$</td>
</tr>
<tr>
<td>$\rightarrow$</td>
<td>$H^+ + He^+ + 2e$</td>
<td>$\sigma_{c11}$</td>
</tr>
<tr>
<td>$\rightarrow$</td>
<td>$H^+ + He^{++} + 3e$</td>
<td>$\sigma_{c12}$</td>
</tr>
</tbody>
</table>
been indicated\textsuperscript{20} that electron capture by $H^0$ to form $H^-$ is negligible in the energy range of the present investigation. In the investigation utilizing a \textit{He}$^{++}$ projectile, however, it was observed that the electron capture events accounted for a large fraction of the total number of reactions.

For the purpose of the present investigation, the concept of the collision cross section will be used as a means of expressing the probability that some particular event will occur. This concept permits the assignment to the target particle of an effective size, which is related to the probability of the occurrence of a specific event. In order to define a cross section, consider a parallel, monoenergetic beam of $N_p$ projectiles per second to pass through a target gas of density $m$ and thickness $L$ which are sufficiently small such that no projectile undergoes more than one collision. The number of particles per second $N$ undergoing collisions is proportional to the density of target particles, the number of projectiles, and the target thickness. Thus

$$N = \sigma mN_L$$

where $\sigma$ is the constant of proportionality, which has the dimensions of an area, and is defined as the cross section area per particle for the interaction considered. It is important to note that this cross section, or effective size, has no direct relation to the physical dimensions of either the target or projectile.

The cross section notation of Hasted,\textsuperscript{21} shown in the right hand column of the list of Equations 1-5, is arranged to convey all the infor-
mation concerning the reaction process that is contained in the reaction equation. The symbols \( \sigma_{abij} \) represent the cross section for a projectile of charge \( a \), incident on a target of charge \( b \), to undergo a reaction that leads to a final state of the projectile of charge \( i \), and of the target, of charge \( j \). The summation over all experimental values represented by a subscript is denoted in a given reaction by leaving the subscript unspecified.

Measurement of the cross sections characterizing the three fundamental reactions of electron capture, stripping, and ionization may be divided into two major categories as follows:

(a) observation of the charge states of the beam after it emerges from the collision region, and

(b) observation of the residual slow particles formed in the collision events.

Most experiments concerned with the measurement of electron capture and stripping cross sections have been of group (a), and involved the direct observation of the fast particle that underwent a change. In contrast, for the measurement of ionization cross sections, most experiments have been of group (b) because the particle that underwent a change was the target. As will be seen later, the experiments of group (b), to which the present experiment belongs, can often be used to obtain measurements on the stripping and electron capture cross sections also. However, the experiments of group (a) cannot be used to measure the ionization cross sections.

Later in this thesis, the results on stripping and electron capture cross sections, obtained in this investigation, will be compared with
those results of other investigators, most of which were measured by the methods of group (a). In order to better understand the significance of the comparisons, a brief description of the relevant experiments and techniques used by the other investigators will be presented here.

The first experiment of group (a) with which the results of this investigation can be compared is that of Allison\textsuperscript{22,23,24} at the University of Chicago. In 1956 and 1958 his group published results from one apparatus on both the total electron capture cross sections \( (20\sigma_{ij} + 20\sigma_{0j}) \) for He\textsuperscript{++} projectiles, and the total stripping cross sections \( (00\sigma_{ij} + 00\sigma_{2j}) \) for He\textsuperscript{0} projectiles in targets of helium, hydrogen, and air, over the energy range 100 to 450 keV. Results were also obtained, by modifying the apparatus, on the double capture and stripping cross sections \( 20\sigma_{0j} \) and \( 00\sigma_{2j} \), respectively.

The experimental procedure used by Allison's group was to prepare the He\textsuperscript{0} and He\textsuperscript{++} beam by passing the He\textsuperscript{+} beam produced by the accelerator through a gas cell in which it underwent charge changing collisions. In order to measure the total electron capture or stripping cross sections, the desired beam was passed into an evacuated collision chamber, which was located in a strong magnetic field. By means of this field the He\textsuperscript{++} could be deflected into a detector or the He\textsuperscript{0} beam could pass undeflected into the relocated detector. The total cross sections were then determined by observing the attenuation of the beam as the gas pressure in the chamber was increased.

The double electron capture cross sections and the double stripping cross sections were measured in a slightly different manner. In this case the He\textsuperscript{++} (or He\textsuperscript{0}) beam was passed through a collision chamber prior to
entering the magnetic analyzer. The cross sections were determined by observing the growth of the \( \text{He}^0 \) (or \( \text{He}^{++} \)) in the analyzer as the gas pressure in the collision chamber was increased. The range of gas pressure was sufficiently low such that multiple collisions by the projectile were negligible.

The second experiment of group (a) that is of interest for comparison purposes is that of C. F. Barnett\(^{12,13}\) (1958) at the Oak Ridge Laboratories. He and co-workers have directly measured the total stripping cross sections for \( \text{H}^0 \) (between 250 and 1000 keV), and \( \text{He}^0 \) (between 4 and 200 keV), which are denoted \( \sigma_\text{i,j} \) and \( (\sigma_\text{i,j} + \sigma_\text{f,j}) \), respectively. Their procedure was essentially that of Allison\(^{22,24}\) with the exception that a transverse electric field was applied inside the collision chamber, rather than a magnetic field, for the purpose of removing from the beam those projectiles that had undergone stripping reactions.

The third experiment of group (a) with which the results of the present investigation compare is that of Nikolaev, et al.\(^{25}\) (1961) at Moscow State University. He and co-workers measured the cross section \( \sigma_\text{i,j} \) for single electron capture by \( \text{He}^{++} \) in the targets of \( \text{He} \), \( \text{Ar} \), and \( \text{N}_2 \) over the energy range of the present experiment. The measurement procedure was essentially that of Allison,\(^{23}\) i.e., the beam was passed through a gas and then magnetically analyzed to determine the charge state distribution.

The most recent experiment of group (a) of direct interest is that of Pivovar, et al.,\(^{11}\) of the Physico-technical Institute U.S.S.R. He published results in 1961 for the single electron stripping cross section \( \sigma_\text{i,j} \) for \( \text{He}^0 \) projectiles, and the single electron capture cross section...
\( \sigma_{1j} \) for \( \text{He}^{++} \) projectiles over the energy range and target gases used in the present investigation.

The above data were not measured directly but were obtained in the following manner. A primary beam of singly charged helium ions produced in an electrostatic accelerator was passed through a chamber filled with the target gas. The gas pressure was sufficiently low so that multiple beam collisions were negligible, and of the events that did occur only those that led to electron capture or stripping of the projectile were directly observed. The \( \text{He}^0 \) and \( \text{He}^{++} \) thus formed were separated electrostatically and measured. In this manner the cross sections \( \sigma_{0j} \) and \( \sigma_{2j} \) were determined for the \( \text{He}^+ \) projectile.

One further series of measurements was necessary, however, to obtain the \( \sigma_{0j} \) and \( \sigma_{2j} \) cross sections. The collision chamber was modified, and a considerably higher target gas pressure was used to cause the beam to undergo a large number of collisions, in order that the rates of production and destruction of a given charge state of the projectile were in equilibrium. That is, the pressure was sufficiently high such that if it were increased the relative fractions of the beam in charge states \( \text{He}^0, \text{He}^+, \) and \( \text{He}^{++} \) would remain constant; these fractions, which are generally rather complicated functions of the individual cross sections, are known as "equilibrium fractions," and are designated as \( F_{00}, F_{10}, \) and \( F_{20}, \) respectively. After measuring the equilibrium fractions, it was necessary for Pivovar, et al., to make several simplifying assumptions, which will be discussed later, regarding these fractions in order that they may be used to relate the directly observed values for the \( \text{He}^+ \) projectile to the cross sections \( \sigma_{0j} \) and \( \sigma_{2j} \) for the \( \text{He}^0 \) and \( \text{He}^{++} \)
projectiles, respectively.

In 1962 Pivovar, et al.\textsuperscript{10} directly measured the cross sections $\sigma_{ij}$ and $\sigma_{0j}$ for a beam of He\textsuperscript{++} projectiles. These direct measurements were made in the same fashion as the previously discussed direct measurements on the He\textsuperscript{+} projectile. The point, that there is substantial difference in the quoted values for $\sigma_{ij}$ from the direct and indirect measurements, and the implications of this discrepancy are discussed in a later chapter.

Thus, the discussion of the general nature of the experiments that comprise group (a) is temporarily concluded.

It is now of interest to discuss the experiments of group (b), which are those that involve the observation of the residual slow collision products. It was previously stated that the present experiment belongs in this group. The only other experiment of this type that has produced results which may be directly compared to those of the present investigation is that of Solov'ev, et al.\textsuperscript{26,27} of the Leningrad Physicotechnical Institute. In 1961 his group published results on the total apparent ionization cross sections which will be explained shortly, and the stripping cross sections for H\textsuperscript{0} projectiles in the energy range from 10-180 keV. In 1964 results were published for the total apparent ionization cross section for He\textsuperscript{0} projectiles in the same energy range. Comparisons are made between the present results and those of Solov'ev, et al., wherever applicable.

In order to understand the manner in which cross sections are deduced in most experiments of group (b), the present experiment is used as an example.
In the present investigation the thin-target approach was used exclusively, i.e., the density of the target gas was sufficiently low such that the probability of multiple collisions by the projectile was negligible. The analysis of the slow collision products first performed consisted simply of total collection with a transverse electric field. This method served to indicate the total quantities of positive and negative charge that were left in the collision region by the passage of the projectiles. For some projectile-target combinations, a further analysis, consisting of a determination of the distribution in charge-to-mass ratios, was made of the slow positive ions.

The analysis utilizing only the collection field served to give the total apparent cross sections for the production of positive ions \( \sigma_+ \) and electrons \( \sigma_- \). The manner in which these cross sections were deduced from the measured quantities is discussed in Appendix II. The final expressions for \( \sigma_+ \) and \( \sigma_- \) for this atomic projectile are

\[
\begin{align*}
[\sigma_+]_{\text{He}} & = \frac{1}{\text{mL}} \frac{I^+}{I_n} \\
[\sigma_-]_{\text{He}} & = \frac{1}{\text{mL}} \frac{I^-}{I_n}
\end{align*}
\]

where

\( I^+ \), \( I^- \) = the positive ion and electron currents, respectively, to the collection plates,

\( m \) = the density of the target gas,
\( L \) = the length of the collection plates, and
\( I_n \) = the "current" of neutral projectiles.

It is evident that \( \sigma_+ \) and \( \sigma_- \) can be represented in terms of the cross sections listed in Equations 1-5 as follows:

\[
\sigma_+ = \sigma_{01} + \sigma_{11} + 2(\sigma_{02} + \sigma_{12})
\]  
\[
\sigma_- = \sigma_{01} + \sigma_{10} + 2(\sigma_{02} + \sigma_{11}) + 3\sigma_{12}
\]

Thus it is seen that \( \sigma_+ \) and \( \sigma_- \) are not simply the sums of the individual cross sections, but instead the measurement of \( \sigma_+ \) and \( \sigma_- \) weighs each individual cross section according to the quantity of charge it yields.

It should be noted that further insight into the contributions of the individual cross sections to the measured \( \sigma_+ \) and \( \sigma_- \) may be obtained by considering the difference in \( \sigma_+ \) and \( \sigma_- \). For this projectile-target combination this is

\[
\sigma_- - \sigma_+ = \sigma_{10} + \sigma_{11} + \sigma_{12}
\]

Now if one denotes the total apparent ionization cross section \( \sigma_i \) as the sum of those individual cross sections for which one slow positive ion is formed in the gas plus twice those cross sections that produce two slow positive ions, etc., then Equation 9 for the present case becomes

\[
\sigma_+ = \sigma_i
\]
Similarly, denote the total apparent stripping cross section $\sigma_s$ as the sum of those individual cross sections for which one electron is removed from the projectile plus twice those cross sections for removal of two electrons, etc., then Equation 10 becomes for this case

$$\sigma_\text{r} = \sigma_1 + \sigma_s$$  \hspace{1cm} (13)

Therefore, Equation 11 is

$$\sigma_- - \sigma_+ = \sigma_s$$  \hspace{1cm} (14)

Unless one wishes to make assumptions regarding the relative sizes of the individual cross sections, or use information that other investigators have obtained, this is as far as the present analysis can be pursued. However, as was mentioned previously in this chapter, one can make an analysis of the charge-to-mass ratios of the slow ions. This will produce additional information.

It should be noted that such an analysis was not performed for the $H^0$ on He projectile-target combination, because the most immediate interest in this analysis was to check out the recently constructed spectrometer, and comparison data were available for other collision pairs. (The results obtained with this spectrometer were in excellent agreement with the existing comparison data.) However, for the purpose of continuity, the application of the charge-to-mass analysis will be discussed here for the $H^0$ on He collision combination.

This type of analysis would distinguish between the two helium ions,
He$^+$ and He$^{++}$. Therefore, the relative cross sections $\sigma(\text{He}^+)$ and $\sigma(\text{He}^{++})$ for the formation of these two ions can be measured. These two cross sections can be represented in terms of individual cross sections as follows:

$$\sigma(\text{He}^+) = o_o o_1 + o_0 o_1$$  \hspace{1cm} (15)

$$= o_0 o_1$$

and

$$\sigma(\text{He}^{++}) = o_0 o_2 + o_0 o_2$$  \hspace{1cm} (16)

$$= o_0 o_2$$

These relative cross sections may then be normalized to the total apparent cross section for production of ions $\sigma_+$. This is the manner in which the total apparent cross sections were obtained in this investigation for $\sigma_+, \sigma_{e}, \sigma_{i}, \sigma_{s}$, and $\sigma_c$ (where $\sigma_c$ represents electron capture for the case of the He$^{++}$ projectile) for the projectiles He$^{++}$, He$^+$, and H$^+$ on the four target gases He, Ar, H$_2$, and N$_2$. Also, for the H$^+$ projectile on He and Ar, the partial ionization cross sections were measured.
CHAPTER III

APPARATUS AND TECHNIQUES EMPLOYED TO OBTAIN
ION AND ATOM BEAMS OF SPECIFIED CHARACTER

The source of the fast beams was a 0.15 to 1.0 MV Van de Graaff positive-ion accelerator, equipped with a beam analyzing and stabilizing system. Since the accelerator produced directly only the singly charged ions $H^+$ and $He^+$, a gas cell in which all the projectiles could undergo charge changing collisions was located further along the beam path. As the beams of mixed charge states emerged from the gas cell they were electrostatically separated. The remainder of the apparatus could then be aligned with the desired beam component.

The Beam Source and Energy Determination

The radio-frequency ion source of the Van de Graaff had two gas inlets, each equipped with a thermomechanical leak. When molecular hydrogen and helium gases were used, the ion source furnished about 50 to 100 microamperes total output current.

The beam from the accelerator was passed through a 90° sector magnetic field (see Figure 1), which analyzed the beam into its components according to the charge-to-mass ratios. When molecular hydrogen was used in the source, it was found that the principal beam component was $H^+$, with $H_2^+$ being about one-third as intense. For helium in the source, the beam was almost entirely $He^+$; $He^{++}$ was negligible.
Figure 1. Schematic View of Beam Preparation Apparatus.
The energy of the beam emerging from this analyzer was stabilized by electronic regulation of the accelerator voltage to maintain equal currents to two stabilizer slit edges. This procedure amounted to imposing a constant 90° deflection of the beam in the regulated magnetic field. (This was the standard stabilizing system provided by the accelerator manufacturer, the High Voltage Engineering Corporation. The nominal energy spread was ± 2 keV at 1 MeV.) Thus the beam energy was determined by the magnetic field, which had been calibrated prior to the present experiment by measuring the magnetic field corresponding to the 1.019 MeV threshold of the nuclear reaction H³(p, n) He³, using a tritium-zirconium target. Throughout the present investigation, a Harvey Wells (Model G-501) nuclear magnetic resonance gauss meter was used for the measurement of the magnetic field.

The Gas Cell

The magnetically analyzed beam was next directed through a gas cell in which it was allowed to undergo charge changing collisions. Both the nature and the pressure of the gas used in this cell were dictated by the yield of the desired output beam component. The choice of the gas was based on the equilibrium fractions of the various beam components. It was determined that, in this energy range, the gas that produced the largest fractions of He⁰ and H⁰ was helium. Similarly, for the production of He⁺⁺, molecular nitrogen was indicated. Figure 2 shows a plot of the required helium pressure in the gas cell in order that the components of He⁰ and H⁰ may reach 90 percent of the maximum intensities as indicated by equilibrium fractions.
Figure 2. Calculated He Pressures in Gas Cell as a Function of Beam Energy for H⁺ and He⁺ to Attain 90 Percent Maximum Intensity.
The usual pressure used in this cell of length 31 cm was about 7 to $20 \times 10^{-3}$ Torr. The gas was admitted continuously through an Edwards metering valve and was continuously pumped out through the apertures on both ends of the cell.

It was essential to confine the high pressure to the region of the gas cell as much as possible. If the gas emerging from the cell were allowed to produce a sufficient pressure rise in other parts of the system, then the beam passing through these regions would undergo additional charge changing collisions. A particularly undesirable region for this occurrence would be that following the electrostatic analyzer. High pressure in this region would cause the selected beam component to become contaminated with other charge states. If this were permitted, an error would be introduced in the experiment due to the uncertainty in beam composition. Figure 3 shows the computed maximum pressure in this region for which not more than one percent collisions of a charge changing nature would occur.

With the above considerations in mind, separately pumped chambers were installed on both ends of the gas cell for the purpose of more efficiently confining the gas to this region. The entrance aperture on the chamber preceding the gas cell and the exit aperture on the chamber following the gas cell were cylindrical channels of 1/8 inch I.D. and were 1-1/4 inches in length. These apertures were optically aligned with those of 1/16 inch I.D. and equal length mounted on either end of the gas cell. As expected, the higher impedance to the flow of gas provided by the cylindrical apertures proved very effective in producing a large pressure differential between the gas cell and adjacent chambers. With this arrangement of differentially pumped chambers and cylindrical apertures, a quite satis-
Figure 3. Calculated Pressures for Which Beams of $H^0$, $He^0$, and $He^{++}$ Will Undergo No More Than One Percent Collisions of a Charge Changing Nature.
factory pressure reduction between the gas cell and the remainder of the system was accomplished.

Figure 4 shows the relation of the pressure in the gas cell, as measured with a McLeod gauge, to that measured with an ion gauge, in the electrostatic analyzer following the second differential pumping chamber. The ion gauge reading was corrected for its low helium sensitivity. As is indicated in the figure, the base vacuum of the region is around $1 \times 10^{-6}$ Torr. The pressure rise associated with $20 \times 10^{-3}$ Torr of helium in the gas cell is only about $1.5 \times 10^{-7}$ Torr in the analyzer. This is considerably under the upper pressure limit as indicated in Figure 3.

The Electrostatic Analyzer

The beam that emerges from the gas cell contains several different components. For example, if the He$^+$ beam from the accelerator entered the gas cell, then the components that emerged from the cell would be He$^0$, He$^+$, and He$^{++}$. In order to separate the desired component, this mixed beam was passed into an electrostatic analyzer. This analyzer is described in the thesis of R. A. Langley, however, because it served a very important function in the present investigation, a description is included here also.

For clarity, in Figure 1, the electrostatic analyzer is shown rotated $90^\circ$ about the beam axis. That is, the beam deflections produced by the analyzer are actually in a horizontal plane, rather than vertical as it appears in the figure. The analyzer deflection plates were 17 cm in length and separated by 1.2 cm. These plates were mounted on a bracket that could be rotated about the beam axis with an external control. This
Figure 4. Relationship of Gas Cell Pressure to Pressure in Electrostatic Analyzer.
arrangement permitted the adjustment of the plane of deflection to coincide with the horizontal plane of beam detectors and the exit port located at the end of the analyzer. A high voltage power supply (Hamner Model N-413) was used to apply up to 5000 volts between the two deflection plates, one of which was grounded. A deflection voltage of about 2500 volts was used to separate the $\text{He}^0$, $\text{He}^+$, and $\text{He}^{++}$ components formed in the charge changing collisions of a 1 MeV $\text{He}^+$ beam. This voltage provided about two-centimeter horizontal separation of these components at the exit port of the analyzer.

Provisions were made although not often used to measure the intensities of all the separated components that emerged from the gas cell. Near the exit end of the analyzer section are three Faraday cups and a secondary-emission neutral detector. Each detector can be independently positioned horizontally by means of a lead screw to collect one of the separated beams. A frosted glass plate which was located in this region could be rotated into position to intercept all of the separated beams. This plate provided a visual indication of the beam locations by means of the fluorescence of the glass. This arrangement of detectors is shown in the insert in Figure 1. In order to obtain the beam component desired for cross section measurements, the appropriate detector is moved aside, then that component is allowed to pass out of the analyzer through the exit port.

A major concern in this experiment is the possibility that the fast neutral beams, $\text{H}^0$ and $\text{He}^0$, which are obtained through electron capture by $\text{H}^+$ and $\text{He}^+$ beams in the gas cell, contain an appreciable fraction of atoms in excited states. The magnitudes and even the ratios of the cross sections for most types of collisions would be different for such excited
atoms from those for ground state atoms.

As a check on the possibility of atoms excited to ordinary excited states reaching the collision chamber, the flight time from the gas cell to the collision chamber may be compared to the lifetimes of such states. Using available calculations and measurements, which relate the lifetime to the principal quantum number \( n \) of the excited state for hydrogen \(^{29}\) and for helium, \(^{30}\) one finds that all allowed states of hydrogen with \( n \leq 6 \) and of helium with \( n \leq 7 \), are too short lived to survive the transit even at the highest beam velocities used here. A separate calculation \(^{31}\) indicates that the probability of producing excited states with \( n > 7 \) does not exceed about 0.003. Therefore, it is not expected that ordinary states of excitation, i.e., other than metastable states, can cause any difficulties in this experiment.

However, \( \text{H}^0 \) and \( \text{He}^0 \) both have low lying metastable states which cannot decay by allowed transitions and have sufficiently long lifetimes to reach the collision chamber. In the case of \( \text{H}^0 \), it is expected \(^{32}\) that any atoms emerging from the gas cell in the 2s metastable states would be quenched by the electric field of the electrostatic analyzer; however, these fields would have little effect on \( \text{He}^0 \) metastables. In fact, no change in the cross section values, for either projectile, was observed when the analyzer field was varied from about 500 v/cm (minimum value for which charged particles were removed from the beam) to more than 4000 v/cm.

If there were indeed many non-ground state atoms in the beams, it would seem that the fraction of all beam atoms in such states should vary with the pressure and with the nature of the charge-exchange gas used in the cell. A search for such a dependence was made by observing the values
of the cross sections while the gases He, Ar, and N₂ were used, and the pressures were varied by a factor of more than 1000; however, no change in the cross sections was observed. Further indications of the absence of such excited states in the He⁰ neutral beam are presented in Chapter V. It should be noted that this evidence for the lack of excited states in the He⁰ beam is in confirmation of the work of Allison, 24 although Barnett, et al. 12 found evidence of the effects of excited states. He observed that the cross section values changed about 40 percent as the pressure in the gas cell was varied. However, the variation in gas cell pressure in the present experiment was over an even greater range than Barnett used, and it did not produce any change in the observed cross sections. Our conclusion was that the effects of excited states were unimportant in this investigation.
PART B
CHAPTER IV

APPARATUS AND TECHNIQUES EMPLOYED FOR THE MEASUREMENT OF THE
TOTAL APPARENT ION AND ELECTRON PRODUCTION CROSS SECTIONS

Figure 5 is a schematic diagram showing the entire apparatus. Attached to the electrostatic analyzer, which was previously discussed, is shown the portion of the apparatus that was used for the cross section measurements. As is suggested by the offset bellows shown in this figure, the entire apparatus following the electrostatic analyzer can be moved, by means of vertical and horizontal jack-screws, into alignment with the selected beam component.

When the apparatus is thus aligned, the beam passes through a three-aperture collimator, through the collision chamber, and into a beam detector. The collision chamber, which is represented in the figure as a rectangular box, although in reality it is a round enclosure, contains the target gas. As the beam underwent collisions with the gas molecules, free electrons and ions were produced. These slow collision products were collected on electrodes within the collision chamber and gave rise to the ion and electron currents used in the calculation of the cross sections (see Appendix II). Figure 6 is a photograph of the apparatus showing the electrostatic analyzer on the left and the collision chamber on the right.
Figure 5. Schematic Diagram of Apparatus Employed in the Measurements of the Total Apparent Cross Sections.
Figure 6. Exterior View of Electrostatic Analyzer and Collision Chamber.
The Collision Chamber and Associated Beam Collimator

The selected beam was passed through a three-aperture collimator, which is shown in Figure 7 before it entered the collision chamber. Prior to installation, this collimator was rigidly and carefully aligned as a unit, optically, with the aid of the telescope of a Gaertner (Model 911) cathetometer.

The beam incident on this collimator was diverging from the 1/8 inch diameter exit aperture of the gas cell, some two meters away. The primary geometrical collimation of the diameter and divergence of the beam was established by the first aperture ("a" in Figure 7), a knife-edged round hole of 4/64 inch diameter, the smallest of the three apertures. Aperture "b" was a round hole of 5/64 inch diameter, large enough not to further intercept the main beam defined by the preceding apertures. Its function was to intercept particles scattered from the edge of aperture "a" and from the residual gas, but its own edge was kept clear of the main beam so as not to serve as a further source of such scattered particles.

Among the scattered particles of concern here were first, of course, fast heavy beam particles which, having suffered a scattering collision, might also have suffered a change in their charge, so that they would now represent a contaminant in the beam. Possibly even more important, however, were fast "knock-on" electrons traveling with the beam with speeds of the same order of magnitude as the heavy particles. Previous experience with a less carefully designed collimator had shown that such electrons, entering the collision chamber with the beam, could be most troublesome in this experiment. More will be said on this matter later, in the discussion of saturation currents to the collecting electrodes in the col-
Figure 7. Schematic Diagram of Beam Collimator and Collision Chamber Components Employed in the Measurements of the Total Apparent Cross Sections.
The third and last aperture ("c" in Figure 7) was the largest in diameter of the three, being a cylindrical channel of 1/8 inch diameter and about 5/8 inch long, with a knife-edged lip of 6/64 inch diameter at the end on which the beam is incident. Similar to aperture "b", the edges of "c" stood clear of the main beam defined by preceding apertures, so that it served the purpose of further skimming off scattered particles, without serving as a source of such particles itself. The main function of aperture "c", however, was to define the boundary between the evacuated beam tube and the target gas in the collision chamber. This boundary must be as sharply defined and as close to the measurement region as feasible in order to minimize the amount of gas the beam passes through before it reaches the measurement region. If this requirement were not satisfied to the greatest practicable degree, the charge composition of the beam incident on the measurement region could have been significantly altered by charge changing collisions in the preceding gas. To accomplish this function, aperture "c" was located in the entrance of the channel mentioned above, which projected into the collision chamber almost to the edges of the guard electrodes immediately preceding the measurement region. Pumping of the region of the beam tube between apertures "b" and "c" was accomplished through three large off-center holes in the plate that supported aperture "b", by the two-inch oil diffusion pump, with a water-cooled baffle, connected to the collimator tube between "a" and "b".

When the collision chamber was evacuated, the pressure in the collimator was about $1 \times 10^{-6}$ Torr; however, with the target gas at a pressure of about $5 \times 10^{-4}$ Torr, the pressure in the collimator between
apertures "a" and "b" was about $8 \times 10^{-8}$ Torr as measured on a Veeco (Type RG-75) ionization gauge. A calculation based on the conductances of the slits and the pressures listed above indicated the pressure between slits b and c to be about $2 \times 10^{-5}$ Torr. Since only about one percent of the projectiles underwent charge changing collisions in the chamber at $5 \times 10^{-4}$ Torr, it was expected that a negligible number of such collisions occurred in the collimator.

One further feature was incorporated into this collimator assembly to deal with the problem of fast electrons in the beam, which has served to verify the efficacy of the careful geometrical design described above. A small pair of electrostatic deflector plates was installed in the region between apertures "b" and "c", to deflect away from aperture "c" any electrons coming through "b". Application of up to 600 volts to this deflector, calculated to be more than enough to deflect out electrons with the same velocity as the heavy beam particles, was found to have no noticeable effect on the electron current collected from the measurement region, or on the saturation curves for this current. It was concluded that the present careful design of the collimator has essentially eliminated the problem of fast electrons in the beam. Since the deflector had no effect, it was evidently not required and it was not further used except for this test.

The collision chamber was of stainless steel and the flanges were sealed with neoprene O-rings. The chamber was evacuated by a four-inch liquid nitrogen-trapped oil diffusion pump. A separate liquid nitrogen trap was suspended in the collision chamber above the ion and electron collection electrodes to assist in the removal of condensable vapors.
The collection electrodes were so oriented that the cold trap could not be seen from the beam path in order to reduce the temperature perturbation in the collision region. The base vacuum in the chamber, with the internal trap warm, was about $2 \times 10^{-6}$ Torr as indicated on the ionization gauge. However, with the trap filled with liquid nitrogen the base vacuum increased to $1 \times 10^{-7}$ Torr. This indicated that condensable gases made a substantial contribution to the background gas in the chamber. The significant benefit of operating with the trap cold was in the reduction of the electron and ion currents from ionization of the background gas. These currents, which will be discussed later, were reduced, by a factor greater than 20, to a negligible value compared to the ionization currents produced in the target gas.

In order to determine whether or not the cold trap significantly altered the temperature distribution of the target gas, cross section measurements were made with and without the trap being cooled. When the measurements made with the trap at room temperature were corrected for the background contributions, the two sets of cross section values were equal. Therefore, it was concluded that no systematic errors were introduced by the use of the cold trap. This conclusion was expected because the average path from the cold trap to the measurement region involved several encounters with the room temperature walls of the collision chamber. Therefore, a molecule that had lost energy to the cold surface of the trap usually had regained it before reaching the measurement region.

A cold-trapped McLeod gauge was employed for the measurement of the target gas pressure. This gauge was connected to the collision chamber with a tube that pointed directly to the collision region between the ion
and electron collection electrodes. A modified CEC (Model GM-110) McLeod
gauge was used for these measurements. (Details of the gauge, operational
techniques, and associated errors are discussed in detail in Appendix III.)

A Veeco (Type RG-75) ionization gauge was also attached to the chamber,
which provided a convenient means for preliminary measurement of the gas
pressure. However, the ionization gauge could not be operated at the time
that the ion and electron currents were being measured because consider-
able numbers of ions were repelled out of the operating ionization gauge
and were attracted to the ion collection electrode.

For some of the projectiles used in this investigation, such as
He$^0$ and particularly H$^0$, the cross sections were small, and in order to
obtain satisfactory ion and electron currents to the electrodes, it was
necessary to use a rather high target gas pressure - around 1 x 10^{-3} Torr.

In order to accomplish this, the gate valve B55 of Figure 5 was used as
a throttling valve. This reduced the pumping speed to the chamber, and
thereby the gas throughput. A large throughput could give rise to pres-
sure gradients in the collision chamber and consequent uncertainties in
the gas density in the collision region. Tests were made to insure that
no detectable gradients were present.

The target gas pressure was maintained by a continuous input through
a cold trap and an Edwards metering valve. The pressure was varied over
the working range from about 3 x 10^{-5} to 1 x 10^{-3} Torr simply by adjust-
ing the input rate and the constriction presented by the gate valve. The
four-inch diffusion pump was operated continuously to maintain the back-
ground pressure in the chamber at a constant value, independent of the tar-
get gas pressure. In the course of this experiment, the contribution to
the measured cross sections from the background gas was always less than one percent of the total cross sections.

**The Fast Beam Detector**

The beam detector used in this investigation was designed to totally trap the beam and to provide for three observations: 1. the net current delivered by the beam; 2. secondary emission current from the beam target foil; 3. total power of the beam, through observation of the temperature rise of the target foil, by means of a thermocouple.

A diagram of this detector is shown in Figure 8 and its operating principles are contained in the following description. The charged beam was passed into the detector and impinged on the copper foil. This foil was supported by four copper wires of diameter 0.003 inch, which served as electrical connections to the brass heat sink. When the beam struck the foil, secondary electrons were ejected, which produced an apparent increase in the beam current. The sleeve on the detector, which was electrically insulated from the foil, was designed to collect all of these electrons. Therefore, in order to measure the net current delivered by the beam, which is listed as observation number one, leads from the heat sink and from the sleeve were connected together outside of the chamber, and the net current was measured by means of a Keithley (Model 415) pico-ammeter.

The second observation listed above, which was that of secondary emission current from the beam target foil, was accomplished simply by measuring only the current to the sleeve. In this measurement, the same electrometer or a Keithley (Model 410) pico-ammeter was used.
Figure 8. Schematic Diagram of the Fast Beam Detector.
Observation three, the total beam power, permitted the measurement of a beam of neutral particles. The target foil on which the beam impinged was designed and mounted such that it would be heated by the power deposited in it by the beam. The foil which was 0.28 inch in diameter and 0.002 inch thick was of small thermal capacity, and its temperature was measured by means of a copper-constantan thermocouple. One thermocouple junction was spot-welded to the back of the foil and the other was attached to the brass heat sink which served as the reference temperature. The copper wires that supported the foil were used as one leg of the thermocouple. Both ends of the constantan leg (the constantan lead from the center of the foil and the constantan lead from the heat sink) were passed out of the chamber and to a Keithley nano-voltmeter, which served to measure the emf generated in the circuit. By means of this arrangement, the temperature rise of the foil could be measured as the beam impinged on it.

The calibration procedure required is described in detail in Appendix I; however, the principles involved are briefly discussed in the following. It was verified using a beam of singly charged particles that the emf response of the thermocouple was directly proportional to the total beam power impinging on the foil, within the range of this experiment. The beam power was taken to be the product of the Van de Graaff voltage and the net beam current as measured in the detector. This calibration with the charged particle beam served to establish the proportionality constant between the beam power and the emf of the thermocouple. With this information, it was simple to deduce that the "current" of a neutral beam was just the product of this proportionality constant and the observed emf, divided by the accelerator voltage.
In a calibration of the above type, it was necessary to assure that the singly charged ion beam was not appreciably contaminated with neutral particles causing the true beam power to be greater than was calculated from the net current. After the emf generated in the thermocouple element of the detector had been measured for the charged beam, the beam was electrostatically deflected, and the emf was again read. The latter reading, which corresponded to the neutral contaminant of the beam striking the detector, amounted to only about 0.1 percent of the former reading, which in this experiment was negligible.

In performing cross section measurements with the neutral beams, it is similarly necessary to assure that the neutral beam is not appreciably contaminated with charged particles. Since most of the cross sections being measured are several times as large for charged particles as for neutrals, the possible effects of a given degree of contamination would be magnified. To test for this possibility, it was only necessary to measure the net current delivered to the detector by the nominally neutral beam. A typical test indicated that the percentage of charged projectiles present in the neutral beam was less than 0.1 percent. Thus, for the purpose of the present investigation, it was concluded that the neutral beams were not significantly contaminated with charged particles.

Considerable effort went into optimizing the design of this neutral beam detector in order to obtain both a satisfactory sensitivity, which was dictated by the low neutral beam intensity, and to produce a reasonable response time, which in turn was dictated by the rate of fluctuation of the beam intensity. The results of several tests and computations indicated that the sensitivity (equilibrium temperature rise of the foil per
unit of input beam power) was approximately equal to the inverse of the conductive power $K$ per unit temperature of the wires supporting the foil target, i.e.,

$$\text{sens. } \left( \frac{\circ C}{\text{cal/sec}} \right) = \frac{1}{K \left( \frac{\text{cal}}{\text{sec} \circ C} \right)} \quad (17)$$

This result indicated that thermal radiation from the foil was a negligible factor. It was also indicated that the time constant (the time required to reach $1/e$ of the final temperature) for the thermal function of the foil was approximately given by

$$\tau (\text{sec}) \approx \frac{[Q_f + Q_w] \left( \frac{\text{cal}}{\circ C} \right)}{K \left( \frac{\text{cal}}{\text{sec} \circ C} \right)} \quad (18)$$

in which $Q_f$ and $Q_w$ are the heat capacities of the foil and wires, respectively.

As is indicated in Equations 17 and 18, reducing $K$ in order to increase the sensitivity also causes an increase in the time constant, which must be countered by reducing the heat capacities. In practice, the foil itself could be made small enough so that a significant portion of the total heat capacity was contributed by the supporting wires. Optimization of the detector performance thus depended on a minimal value of the ratio of the specific heat to the thermal conductivity of the supporting wire material, as well as on a large thermoelectric power coefficient of a thermo-
couple, that could be formed using these wires for one side of the circuit. It was on the basis of these considerations that copper was selected for the support wires, with constantan for the other leg of the thermocouple circuit, in preference to other pairs of metals that would have provided a thermocouple of greater sensitivity.

Calculations were made on the basis of Equations 17 and 18 to determine the optimum diameter for the copper support wires. However, in the final experimental evaluation, several sizes were tried and the final choice was made empirically. With the 0.003 inch diameter selected for the copper and constantan wires, and the 0.28 inch diameter by 0.002 inch thick copper foil, the sensitivity obtained was about 3 °C/milliwatt, or in terms of the thermocouple emf, about 0.1 millivolt/milliwatt. The time constant was about 13 seconds.

The next interesting feature of this detection scheme is the "shadow" electrode in front of the detector in Figure 8. It was designed, by making the aperture in the electrode smaller than the detector aperture, which it preceded, to serve two purposes.

The primary purpose was to suppress the escape of secondary electrons from the interior of the detector, by maintaining this electrode at a negative potential with respect to the detector. It was found that a potential of -20 volts or more was sufficient to cause the measured beam current to saturate. The convenient battery voltage of 67-1/2 volts was used throughout the present investigation.

The other purpose of the shadow electrode was to intercept any projectiles that had been scattered through large angles in the gas and thus prevent them from striking the outside surface of the detector. If
such projectiles were not intercepted, they would cause the emission of secondary electrons from the detector. These electrons (sometimes an average of three or four per particle) would create a false beam current to the detector. That is, electrons leaving the detector produce a current in the same sense as positive ions going to the detector. In this manner the effect of large angle scattered projectiles is magnified. However, with the low target gas pressures used in this experiment, less than three percent of the projectiles underwent any sort of ion producing collision, and on the basis of cross section measurements with various sized apertures, it was concluded that the number of projectiles that underwent large angle scattering was negligible.

The final aperture sizes selected were 0.6 cm for the shadow electrode, and 0.7 cm for the detector.

The Ion and Electron Collection Electrodes

The collection electrodes employed in this portion of the experiment were the same ones used in the apparatus described in the thesis of R. A. Langley. A plane view of the collection electrode structure is shown in Figure 7. A photograph of the entire assembled ion and electron collection structure and the beam detector is shown in Figure 9, in which the projectile beam passes from left to right through the structure and into the beam detector. The ion and electron collection assemblies each had five plates which were separately mounted on a rigid Teflon block. All five plates of each structure were maintained at the same potential so that an equipotential surface was defined, and hence a uniform collection field was established in the collision region. Also shown in Figure 9 is
Figure 9. Slow Ion and Electron Collection Structure, and Fast Beam Detector.
a grid which was placed in front of the positive ion collector. The grid
was biased negatively with respect to the ion collector to suppress the
emission of secondary electrons. The suppressor grid and the electron
collection assembly were each one-quarter inch from the beam path, and
the ion collection assembly was mounted the same distance behind the grid.
The center plate (see Figure 7) of each structure was machined to a length
of 1.106 ± 0.001 inches in the beam direction, and all plates were spaced
0.010 inch apart. Since only the ion current (or electron current) to
this center plate was used in the cross section measurements, the other
plates served only as guards, to establish a uniform field in front of the
active plate. Thus, the effective length of the collision region over
which the electron and ion currents were sampled was 1.116 inches (the
plate length plus the plate spacing). End effects at the leading edge
of this plate which were due to any average forward momentum of the slow
ions should have been exactly compensated by the same effects at the other
end.

A fraction of the "slow" ions produced by the fast projectiles
might have substantial energies, and their initial motion might, of course,
be directed toward the wrong collection assembly. In experiments utilizing
heavier projectiles than were used in this investigation, Afrosimov \textsuperscript{33}
observed "slow" ions with several hundred electron volts energy. Therefore,
a substantial collection field across the collision region was required to assure that all of the particles would reach the proper collector.
This collection field was established by the potentials of the suppressor
grid and the electron collection assembly. These were maintained at equal
but opposite potentials so that the beam path would be in the zero poten-
tial plane. The magnitude of these voltages will hereinafter be denoted as $V_c$. The positive ion collection assembly was positive with respect to the suppressor grid by an amount designated as $V_s$ in order to suppress the emission of secondary electrons from the ion collector. A convenient and satisfactory value of $V_s$ was found in the test procedures described below to be $V_c/3$, and it was so maintained during the course of this experiment.

There were two necessary requirements that the voltages $V_c$ had to meet before it could be felt that the ions and electrons were being efficiently collected. The first was that both electron and ion currents must show saturation with increasing values of $V_c$; and second, the present results must verify the well established equality of the electron and ion currents for the case of 1 MeV protons on argon. The empirically verified equality is to be expected because, for incident protons,

$$
\sigma_+ - \sigma_- = \sigma_c
$$

where $\sigma_c$ is the electron capture cross section. Barnett, et al. have measured $\sigma_c$ for 1 MeV protons in argon, and it is completely negligible compared to $\sigma_+$.

Until the beam entrance collimator had been modified and realigned as described previously, there had been considerable difficulty in obtaining proper saturation behavior in the collected current. The ion current saturated, but the electron current continued to increase as $V_c$ was raised. The collimator had originally been constructed with equal 1/16 inch diameter apertures at "a" and "b" (Figure 7) and a third 3/32 inch diameter
aperture at "c" and had been only rather crudely aligned, optically, by means of only the unassisted eye. It has been concluded that the resulting poor alignment was the cause of the difficulty with the collected electron current. Beam particles striking the edges of the apertures could cause electrons to be ejected and to pass into the collision chamber.

These electrons would, of course, have various energies and directions of motion, but some would be collected on the electron collector plate. It seemed reasonable that the current to the electron collector would continue to increase with applied voltage, up to quite large voltages, until all such electrons were being collected.

This had evidently been the trouble, because with the collimator modifications previously described, designed to minimize the number of such electrons scattered into the chamber, and with better alignment of the apertures, proper saturation currents were obtained for both electrons and ions. Sample curves are shown in Figure 10, and it appears that saturation has occurred for the $V_c$ greater than about 250V. It should be mentioned again that once the collimator had been well aligned with the beam, no noticeable effect of the small electron deflector inside the collimator could be detected, even when potentials up to 600V were used. This observation was considered to indicate that there were no appreciable numbers of electrons present in the beam.

The second requirement on the saturation curves was that they must verify the established equality of electron and ion currents for the $1\text{ MeV H}^+$ on Ar. Reference to Figure 10 indicates that the saturated electron current was about two percent greater than the ion current. This difference could be attributed to the effective opacity of the grid that
Figure 10. Response of the Ion and Electron Currents, Produced by H\(^+\) + Ar, to the Collection Voltage.
was mounted in front of the ion collector. It had been expected that the actual effective opacity would be at least as great as the four percent geometrical opacity, because of the focusing effects of the fields about the grid wires. This discrepancy was not resolved. Because it is known that the electron and ion currents should be equal, it was felt that more weight should be attached to this fact than to the expected value of the grid opacity. Therefore, the empirical value of two percent effective opacity was used for the adjustment of the observed ion currents throughout this experiment.

As an overall check of the apparatus and procedures, the measurements of $c_+$ and $c_-$ by Hooper for $H^+$ on Ar were repeated, using collection potentials $V_c$ of 350V. The results of single measurements at each energy point over the range from 0.2 to 1.0 MeV were within two percent of the average values obtained by Hooper. With this excellent agreement, the collimator, the detector, and the collection assembly were considered to be sufficiently tested to produce reliable results. As a double check, however, for all projectile-target combinations, it was verified that both the electron and the ion currents did saturate properly. Such a set of curves for He$^{++}$ on argon is shown in Figure 11.

The two Keithley (Model 410) pico-ammeters used for the collected current measurements were insulated from laboratory ground and were operated with their frames at the potentials of the collectors. Figure 12 shows a schematic diagram of the electrical connections. The internal feed-back arrangement of these electrometers limited the potential difference between the input and the frame to a few millivolts for any value of the input current so that the active central plate had essentially the
Figure 11. Response of Ion and Electron Currents, Produced by He$^{++} + \text{Ar}$, to the Collection Voltage.
Figure 12. Schematic Diagram of the Electrical Connections to the Collection Assembly.
same potential as the guard plates. These instruments were enclosed in a well-grounded wire cage so that the pick up of ac noise in the laboratory would be minimized. AC power to the electrometers was supplied through isolation transformers which were also mounted in the shielded cage. The dc potentials were supplied to the collision chamber by shielded batteries, which also were in the cage, because any ripple or noise in this supply would be capacitively coupled into the electrometer inputs. The electrical connections from inside the collision chamber were passed through the chamber walls by means of kovar-glass seals. Each of the leads from the outside end of the seals to the electrometer cage was passed through cables with double coaxial shields. Only the outer shields were grounded. The inner shields were maintained at the same potential as their central current leads to reduce leakage. Similar guard arrangements through the chamber wall with triaxial shields would have further reduced leakage, but they were not required.

With this arrangement for the measurement of the electron and ion currents, the total background current (noise plus leakage) in the absence of the beam was about $1 \times 10^{-13}$ amps, which was less than one percent of virtually all of the currents measured in this experiment. The background ionization currents produced when the beam was passed through only the background gas in the collision chamber were always less than one percent of the currents obtained when the target gas was admitted.

A Keithley (Model 415) pico-ammeter was used for the measurement of the net beam current, and for neutral beams a Keithley (Model 149) nano-voltmeter was used to measure the voltage output of the thermal beam power detector (refer to Appendix I for details). The pico-ammeters were
nominally calibrated by the manufacturer to ± 4 percent absolute uncertainty on the scales used in this experiment. A further calibration of their readings was made in this laboratory to ± 2 percent by means of a Gyra Electronics current source (Model CS-57).

In order to reduce the scatter of the data caused by beam fluctuations, RC damping was provided in the meter circuits of the electrometers which measured the electron and ion currents; however, the fast beam electrometer was undamped. All three instruments were located in close physical proximity to permit the investigator to read their scales in rapid succession. With this arrangement, the beam electrometer was observed until it chanced that there was a period of several seconds over which the fluctuations were at a minimum; then all three electrometers were quickly read. This procedure was repeated several times until several sets of self-consistent readings were obtained.
CHAPTER V

EXPERIMENTAL RESULTS FOR THE CROSS SECTIONS $\sigma_+$ AND $\sigma_-$

Summary of Experimental Procedures and Discussion of Errors

The beams of $\text{H}^+$ and $\text{He}^+$ in the energy range from 0.150 to 1.00 MeV were obtained directly from a Van de Graaff accelerator. The energy of these beams was determined by $90^\circ$ deflection in a calibrated magnetic field by means of an accurate NMR gauss meter. The nominal energy spread of the beams was $\pm 2$ keV at 1 Mev. The $\text{H}^0$, $\text{He}^0$, and $\text{He}^{++}$ projectiles that were used in the present experiment were obtained from the $\text{H}^+$ and $\text{He}^+$ beams through charge changing collisions in a gas cell. The beam components emerging from the gas cell were electrostatically separated, and the desired component was passed into the collision chamber. As the beam traversed the collision chamber, it underwent ion and electron producing collisions with the target gas. These slow residual ions and electrons were collected on a set of collection electrodes located in the chamber. Also located in the collision chamber was the beam detector, which was designed to totally trap the beam. The slow ion and electron collectors were supplied with potentials of 300 to 400 volts to assure essentially 100 percent collection efficiency for these slow particles. An appropriately biased grid was provided to suppress secondary electron emission from the ion collection electrode.

The slow ion and electron currents were measured by means of sensitive electrometers that were absolutely calibrated to $\pm 2$ percent, and
these electrometers were frequently interchanged to reduce systematic errors. The electronic noise, the leakage currents from the collection electrodes, and the currents produced by ionization of the background gas always totaled less than one percent of the signal for the He$^{++}$ and He$^o$ projectiles. For the H$^o$ projectile, these currents were usually less than one percent, although in the upper part of the energy range (above 250 keV) the noise sometimes reached ± 6 percent. It was estimated that noise of even this magnitude was averaged, by making five or six measurements, to an effective value of only ± 4 percent. It is important to note that in a given measurement sequence several scales on each electrometer were used and, in addition, the roles of the two electrometers were interchanged. Therefore, even though the error associated with an individual scale on an electrometer is systematic, this measurement procedure made these errors essentially random, and they will be so designated in the following tables.

The charged beam He$^{++}$ was measured by collection in a Faraday cup, using an electrometer that was calibrated to ± 2 percent in this laboratory. The neutral beams of H$^o$ and He$^o$ were measured by means of a thermal beam power detector, which required calibration. It is estimated that the absolute error in this calibration did not exceed ± 5 percent, and it was observed that the calibration was reproducible within about ± 3 percent from day to day. This detector could be operated in two fashions. In the first, the directly observed quantity was the emf generated in a thermocouple by the heat produced by the impinging neutral beam, and in the second, the observed quantity was the secondary emission current produced by the beam. The nano-voltmeter and the electrometer used
for these measurements were each absolutely calibrated to ± 2 percent. The noise in the nano-voltmeter and thermocouple circuit was always less than one percent of the signal for the He⁰ projectiles. However, in the upper part of the energy range for the H⁰ projectile, the noise sometimes reached ± 8 percent, but this also was estimated to be reduced, by multiple readings, to only ± 5 percent.

The largest and only known systematic error that was present in these measurements was in the determination of the target gas density. The mean temperature of the chamber which contained the gas was measured by means of thermocouples which indicated the temperature to be 299°K with a variation of about ± 1 degree over a period of weeks (depending on the ambient laboratory temperature). The target gas pressure was measured by means of a McLeod gauge, which is discussed in Appendix III. The possible error limits associated with the pressure determination are shown (on the last page of that appendix) to vary from one percent high to three percent low for hydrogen, and increasing with the weight of the gas up through argon, for which the pressure errors range from one percent high to 14 percent low.

The last measurement that entered the calculation of the cross sections for σ⁺ and σ⁻ was the effective lengths of the collector plates, which were believed to be determined to considerably better than one percent.

Table 1 summarizes the random errors associated with an individual cross section measurement for the three projectiles, He⁺⁺, He⁰, and H⁰, used in this experiment. It is shown that the total error in the measurement of the individual quantities is less than the observed spread. This
Table 1. Estimated Random Errors (%) in \( \sigma_+ \) and \( \sigma_- \)

<table>
<thead>
<tr>
<th>Measured Quantities</th>
<th>Projectiles:</th>
<th>( \text{He}^{++} )</th>
<th>( \text{He}^0 )</th>
<th>( \text{H}^0 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Slow Ion or Electron Current</td>
<td>± 2</td>
<td>± 2</td>
<td>± 6</td>
<td></td>
</tr>
<tr>
<td>( \text{He}^{++} ) Beam Current</td>
<td>± 2</td>
<td>---</td>
<td>---</td>
<td></td>
</tr>
<tr>
<td>((\text{He}^0,\text{H}^0)) Beam Power</td>
<td>---</td>
<td>± 2</td>
<td>± 7</td>
<td></td>
</tr>
<tr>
<td>Detector Calibration</td>
<td>---</td>
<td>± 5</td>
<td>± 5</td>
<td></td>
</tr>
<tr>
<td>Gas Pressure (Random)</td>
<td>± 1</td>
<td>± 1</td>
<td>± 1</td>
<td></td>
</tr>
<tr>
<td><strong>Totals</strong></td>
<td>± 5</td>
<td>± 10</td>
<td>± 19</td>
<td></td>
</tr>
<tr>
<td>Observed Spread in Individual Data Points</td>
<td>± 8</td>
<td>± 12</td>
<td>± 30</td>
<td></td>
</tr>
<tr>
<td>Standard Deviation of Observed Values</td>
<td>± 5</td>
<td>± 8</td>
<td>± 19</td>
<td></td>
</tr>
</tbody>
</table>
is attributed to random errors in the measurement of the ratios of the ion and electron currents to the beam current, due to beam fluctuations, and the time required to observe the three measuring instruments. The last row in Table 1 represents the standard deviation of the observed cross section values. If one assumes that the spread of the data points obeys a normal distribution, then 68 percent of all the values fall within the limits set by the standard deviation.

Table 2 summarizes the total estimated error in the cross section measurements for each projectile-target combination. These errors represent the sum of the standard deviation and the maximum estimated systematic McLeod gauge errors discussed in Appendix III.

Present Results and Comparisons with Other Experimental and Theoretical Results

Presented in Table 3 and Figures 13-16 are the measured total apparent cross sections for the production of positive ions, $\sigma_+$, and electrons, $\sigma_-$, by fast doubly charged helium ions in targets of helium, argon, hydrogen, and nitrogen, respectively.

For the He$^{++}$ projectile, $\sigma_-$ is the total apparent ionization cross section $\sigma_i$, and the difference ($\sigma_+ - \sigma_-$) is the total apparent electron capture cross section $\sigma_c$. The values of the latter quantity from the present measurements are presented separately for the same four cases in Figures 17-20. Also shown for comparison are the $\sigma_c$ measurements of Pivovar, et al.,$^{10}$ of Allison, $^{22}$ and Nikolaev, et al.$^{14}$ It should be recalled from Chapter II that the experiments of this group of investigators$^{10,22,14}$ all have been based upon the direct observation of the change in charge state
Table 2. Total Estimated Errors (%) in $\sigma_+$ and $\sigma_-$

<table>
<thead>
<tr>
<th>Projectile</th>
<th>Target:</th>
<th>He</th>
<th>Ar</th>
<th>H$_2$</th>
<th>N$_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>He$^{++}$</td>
<td>-7</td>
<td>-17</td>
<td>-6</td>
<td>-15</td>
<td></td>
</tr>
<tr>
<td></td>
<td>+5</td>
<td>+5</td>
<td>+5</td>
<td>+5</td>
<td></td>
</tr>
<tr>
<td>He$^+$</td>
<td>-11</td>
<td>-21</td>
<td>-10</td>
<td>-19</td>
<td></td>
</tr>
<tr>
<td></td>
<td>+8</td>
<td>+8</td>
<td>+8</td>
<td>+8</td>
<td></td>
</tr>
<tr>
<td>H$^+$</td>
<td>-22</td>
<td>-32</td>
<td>-21</td>
<td>-30</td>
<td></td>
</tr>
<tr>
<td></td>
<td>+19</td>
<td>+19</td>
<td>+19</td>
<td>+19</td>
<td></td>
</tr>
</tbody>
</table>
Table 3. Apparent Cross Sections for Production of Positive Ions $\sigma_+$ and Electrons $\sigma_-$ by an Incident Beam of He$^{++}$. (All Cross Sections are in Units of $10^{-16}$ cm$^2$ per Molecule.)

<table>
<thead>
<tr>
<th>Projectile Energy (keV)</th>
<th>Helium $\sigma_+$</th>
<th>Helium $\sigma_-$</th>
<th>Argon $\sigma_+$</th>
<th>Argon $\sigma_-$</th>
<th>Hydrogen $\sigma_+$</th>
<th>Hydrogen $\sigma_-$</th>
<th>Nitrogen $\sigma_+$</th>
<th>Nitrogen $\sigma_-$</th>
</tr>
</thead>
<tbody>
<tr>
<td>180</td>
<td>5.55</td>
<td>1.37</td>
<td>-----</td>
<td>-----</td>
<td>-----</td>
<td>-----</td>
<td>25.2</td>
<td>13.7</td>
</tr>
<tr>
<td>200</td>
<td>5.50</td>
<td>1.55</td>
<td>26.3</td>
<td>16.3</td>
<td>11.7</td>
<td>6.20</td>
<td>24.5</td>
<td>14.3</td>
</tr>
<tr>
<td>250</td>
<td>4.98</td>
<td>1.93</td>
<td>24.3</td>
<td>16.8</td>
<td>10.5</td>
<td>6.70</td>
<td>23.2</td>
<td>14.9</td>
</tr>
<tr>
<td>300</td>
<td>4.61</td>
<td>2.21</td>
<td>22.6</td>
<td>17.2</td>
<td>9.35</td>
<td>6.85</td>
<td>21.4</td>
<td>15.0</td>
</tr>
<tr>
<td>350</td>
<td>4.28</td>
<td>2.44</td>
<td>21.4</td>
<td>17.3</td>
<td>8.65</td>
<td>6.97</td>
<td>20.4</td>
<td>15.2</td>
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<tr>
<td>400</td>
<td>3.93</td>
<td>1.47</td>
<td>20.4</td>
<td>17.3</td>
<td>7.92</td>
<td>6.85</td>
<td>19.4</td>
<td>15.2</td>
</tr>
<tr>
<td>500</td>
<td>3.48</td>
<td>2.51</td>
<td>18.7</td>
<td>16.7</td>
<td>6.90</td>
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<td>14.9</td>
<td>5.01</td>
<td>4.91</td>
<td>14.3</td>
<td>13.2</td>
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<tr>
<td>900</td>
<td>2.40</td>
<td>2.19</td>
<td>14.8</td>
<td>14.3</td>
<td>4.67</td>
<td>4.59</td>
<td>13.5</td>
<td>12.7</td>
</tr>
<tr>
<td>1000</td>
<td>2.24</td>
<td>2.06</td>
<td>14.2</td>
<td>13.7</td>
<td>4.23</td>
<td>4.17</td>
<td>12.9</td>
<td>12.2</td>
</tr>
</tbody>
</table>
Figure 13. Total Apparent Cross Sections for Production of Positive Ions, \( \sigma_+ \), and of Free Electrons, \( \sigma_- \), for \( \text{He}^{++} \) Ions Incident on Helium.
Figure 14. Total Apparent Cross Sections for Production of Positive Ions, $\sigma_+$, and of Free Electrons, $\sigma_-$, for He\textsuperscript{++} Ions Incident on Argon.
Figure 15. Total Apparent Cross Sections for Production of Positive Ions, $\sigma_+$, and of Free Electrons, $\sigma_-$, for He$^{++}$ Ions Incident on Molecular Hydrogen.
Figure 16. Total Apparent Cross Sections for Production of Positive Ions, $\sigma_+$, and of Free Electrons, $\sigma_-$, for He$^{++}$ Ions Incident on Molecular Nitrogen.
Cross Correlation Between the Total Apparent Ion and Electron Production Cross Sections, and the Charge Changing Cross Sections for He$^{++}$ Ions Incident on Helium (Fig. 17) and on Argon (Fig. 18). Key to References: P.T.N.(62), Pivovar, et al., (Reference 10); A(58), Allison, (Reference 22); N.D.F.T.(61), Nikolaev, et al., (Reference 14).
Cross Correlation Between the Total Apparent Ion and Electron Production Cross Sections, and the Charge Changing Cross Sections for He$^{++}$ Ions Incident on Molecular Hydrogen (Fig. 19) and on Molecular Nitrogen (Fig. 20). Key to References: P.T.N.(62), Pivovar, et al., (Reference 10); A(58), Allison, (Reference 22); N.D.F.T.(61), Nikolaev, et al., (Reference 14).
of the beam. Therefore, the $\sigma_c$ determined from the above experiments involved measurements that were quite different from those of the present experiment, in which the net excess positive charge deposited in the gas by the fast beam was measured.

The cross section values measured in the present investigation are presented without correction for the Gaede effect (refer to Appendix III). Instead, the possible errors from this effect are incorporated into the error limits assigned to these results. The fractional accuracy of the difference cross sections is generally less than that of the individual cross sections. In the upper energy range $(\sigma_+ - \sigma_-)$ is fractionally small compared with either $\sigma_+$ or $\sigma_-$, and, therefore, random errors in the differences are proportionately larger than in $\sigma_+$ and $\sigma_-$ individually. The systematic errors are, however, the same in both the difference and individual cross sections.

The indicated errors in the comparison results of Pivovar, et al., Allison, and Nikolaev, et al. were all about ± 10 percent. Each of these workers, however, employed a McLeod gauge as a pressure standard; consequently, there were some uncertainties with regard to systematic errors. In fact, from the comparison of the results of these workers, notably Pivovar and Allison, it is seen that they in some cases differ by more than 75 percent. The extent of this disagreement is significantly outside of their combined error limits.

It may be noted that the measurements made in this laboratory generally fall between those of Pivovar and of Allison, and the agreement generally improves for increasing energy. This is a surprising observation because random errors in $\sigma_+$ and $\sigma_-$ measurements are proportionately
larger in \( (\sigma_+ - \sigma_-) \). In fact, for \( \text{He}^{++} \) on \( \text{H}_2 \) the difference in \( \sigma_+ \) and \( \sigma_- \) at 1 MeV is only about two percent and the random error in the difference is about \( \pm 3 \) percent. The agreement with Pivovar at this energy therefore serves to indicate that \( \sigma_+ \) and \( \sigma_- \) are relatively determined to better than one percent. This agreement provides strong confirmation of the validity of both the present total ion production and charge changing cross sections.

For the noble target gases He and Ar, it is noted that the agreement with Pivovar persists within 10 percent to the lowest projectile energies. However, for the molecular targets of \( \text{H}_2 \) and \( \text{N}_2 \), the present results fall as much as 50 percent below those of Pivovar at 180 keV, which is outside of the combined error limits of these two experiments. It is seen in Figures 17-20 that Pivovar's results are higher in all the gases studied than the measurements of this laboratory. It is possible that a systematic error was present in Pivovar's results due to the entrance and exit channels on his collision chamber. In his experiment, which was described in Chapter II, the projectiles were passed through a gaseous target, the thickness of which directly entered the cross section calculation. Long narrow channels, comparable to the length of the collision chamber, of large pumping impedance were used to help confine the gas to the chamber. Because of the pressure gradient down the axis of these channels, the effective thickness of the target gas was not a simple quantity to evaluate, and perhaps led to a systematic error. Certainly, if this effective increase in the length of the collision chamber were not accounted for, the result would be a falsely large cross section measurement.

Finally, it is important to note that the departure from good agree-
ment with the results of Pivovar at low energies brings the present results into better agreement with those of Allison, which extend to an even lower energy.

The total apparent ion and electron production cross sections by fast incident neutral helium atoms, in the same four target gases, helium, argon, hydrogen, and nitrogen, are presented in Table 4 and Figures 21-24. Also shown for comparison are the similar measurements of Solov'ev, et al., extending up to only 0.18 MeV.

As was discussed in Chapter II, Solov'ev's experiment is essentially the same as the present experiment. That is, he collected the slow residual collision products left in the gas by the passage of the fast beam. Specifically, he measured \( \sigma_+ \) and \( \sigma_- \) in the same fashion as was done in this investigation. However, Solov'ev published only his \( \sigma_+ \) results, for which the stated possible error was ±15 percent. It is noted that the two sets of results are in rather good agreement, well within their combined error limits. For neutrals at these high energies, the probability is very small that the projectiles will capture electrons to form negative ions. Therefore, the measured total apparent positive ion production cross section \( \sigma_+ \) is identical to the total apparent ionization cross section \( \sigma_i \). Similarly, the difference between the total apparent electron production cross section and the total apparent positive ion production cross section is just the total apparent stripping cross section \( \sigma_s \) for the fast neutrals. This difference is also plotted in each figure; for comparison there is also shown the total stripping cross sections of Allison, of Barnett and Stier, and the single stripping cross section of Pivovar, et al. It is immediately evident that the present results are
Table 4. Apparent Cross Sections for Production of Positive Ions $\sigma_+$ and Electrons $\sigma_-$ by an Incident Beam of He$^0$
(All Cross Sections are in Units of $10^{-16}$ cm$^2$/molecules.)

<table>
<thead>
<tr>
<th>Projectile Energy (keV)</th>
<th>Helium $\sigma_+$</th>
<th>Helium $\sigma_-$</th>
<th>Argon $\sigma_+$</th>
<th>Argon $\sigma_-$</th>
<th>Hydrogen $\sigma_+$</th>
<th>Hydrogen $\sigma_-$</th>
<th>Nitrogen $\sigma_+$</th>
<th>Nitrogen $\sigma_-$</th>
</tr>
</thead>
<tbody>
<tr>
<td>150</td>
<td>1.22</td>
<td>2.51</td>
<td>8.47</td>
<td>13.1</td>
<td>2.64</td>
<td>4.23</td>
<td>8.18</td>
<td>13.7</td>
</tr>
<tr>
<td>180</td>
<td>1.26</td>
<td>2.56</td>
<td>8.37</td>
<td>13.4</td>
<td>2.72</td>
<td>4.45</td>
<td>7.98</td>
<td>13.7</td>
</tr>
<tr>
<td>200</td>
<td>1.26</td>
<td>2.56</td>
<td>7.95</td>
<td>13.1</td>
<td>2.66</td>
<td>4.39</td>
<td>7.82</td>
<td>13.8</td>
</tr>
<tr>
<td>250</td>
<td>1.27</td>
<td>2.55</td>
<td>7.85</td>
<td>13.5</td>
<td>2.50</td>
<td>4.17</td>
<td>7.52</td>
<td>13.7</td>
</tr>
<tr>
<td>300</td>
<td>1.22</td>
<td>2.47</td>
<td>7.52</td>
<td>13.3</td>
<td>2.40</td>
<td>4.03</td>
<td>7.45</td>
<td>13.7</td>
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<td>7.33</td>
<td>13.2</td>
<td>2.26</td>
<td>3.84</td>
<td>7.20</td>
<td>13.5</td>
</tr>
<tr>
<td>400</td>
<td>1.14</td>
<td>2.28</td>
<td>6.91</td>
<td>12.7</td>
<td>2.16</td>
<td>3.68</td>
<td>6.82</td>
<td>12.9</td>
</tr>
<tr>
<td>500</td>
<td>1.05</td>
<td>2.09</td>
<td>6.34</td>
<td>12.0</td>
<td>1.93</td>
<td>3.32</td>
<td>6.50</td>
<td>12.5</td>
</tr>
<tr>
<td>600</td>
<td>0.99</td>
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<td>3.01</td>
<td>6.05</td>
<td>11.9</td>
</tr>
<tr>
<td>700</td>
<td>0.91</td>
<td>1.81</td>
<td>5.36</td>
<td>10.5</td>
<td>1.56</td>
<td>2.68</td>
<td>5.62</td>
<td>10.9</td>
</tr>
<tr>
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<td>0.86</td>
<td>1.68</td>
<td>5.05</td>
<td>9.76</td>
<td>1.40</td>
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</tr>
<tr>
<td>1000</td>
<td>0.73</td>
<td>1.43</td>
<td>4.26</td>
<td>8.24</td>
<td>1.17</td>
<td>2.01</td>
<td>4.60</td>
<td>9.46</td>
</tr>
</tbody>
</table>
Figure 21. Total Apparent Positive Ion and Electron Production Cross Sections, and the Total Apparent Stripping Cross Sections, for Fast Neutral $\text{He}^0$ Atoms Incident on Helium. Key to the Results of Other Investigators: S.I.O.F.(63), Solov'ev, et al., (Reference 7); P.T.N.(61), Pivovar, et al., (Reference 11); B.S.(58), Barnett and Stier, (Reference 12); A(58), Allison, (Reference 24).
Figure 22. Total Apparent Positive Ion and Electron Production Cross Sections, and the Total Apparent Stripping Cross Sections, for Fast Neutral He\(^+\) Atoms Incident on Argon. Key to the results of other investigators: S.I.O.F.\(^{(63)}\), Solov'ev, et al., (Reference 7); P.T.N.\(^{(61)}\), Pivovar, et al., (Reference 11); B.S.\(^{(58)}\), Barnett and Stier, (Reference 12).
Figure 23. Total Apparent Positive Ion and Electron Production Cross Sections, and the Total Apparent Stripping Cross Sections, for Fast Neutral He\(^{0}\) Atoms Incident on Molecular Hydrogen. Key to the results of other investigators:

- S.I.O.F. (63), Solov'ev, et al., (Reference 7);
- P.T.N. (61), Pivovar, et al., (Reference 11);
- B.S. (58), Barnett and Stier, (Reference 12);
- A (58), Allison, (Reference 24).
Figure 24. Total Apparent Positive Ion and Electron Production Cross Sections, and the Total Apparent Stripping Cross Sections, for Fast Neutral He$^0$ Atoms Incident on Molecular Nitrogen. Key to the results of other investigators:

S.I.O.F. (63), Solov'ev, et al., (Reference 7);
P.T.N. (61), Pivovar, et al., (Reference 11);
B.S. (58), Barnett and Stier, (Reference 12);
A(58), Allison, (Reference 24).
systematically some 40 percent higher than those of the last three investigators, who are in fairly good agreement with each other. It should be noted, however, that the present result is not precisely the same physical quantity as theirs. Since in this investigation all of the electrons formed in the target were collected, the measured total apparent stripping cross section $\sigma_s$ was the single-stripping plus twice the double-stripping cross section, i.e., $\sigma_s = \sum_{j=1}^{2} j \left( \sigma_{00j} \sigma_{jk} \right)$. (Recall that the unspecified subscript $k$ denotes a summation over the full range of charge states it represents.) In contrast, Allison and Barnett have measured the total attenuation of the neutral fast beam by both single and double stripping, with no attempt to distinguish these; hence, their result is simply $\sum_{j=1}^{2} \sigma_{00j}$. The observed differences then imply that

$$\sum_{j=1}^{2} j \left( \sigma_{00j} \sigma_{jk} \right) \approx 1.4 \sum_{j=1}^{2} \sigma_{00j} \sigma_{jk}$$ (19)

$$\sigma_{02k} \approx 2/3 \sigma_{01k}$$ (20)

However, this inference is in contradiction to the separate findings of Allison and Solov'ev et al. that $\sigma_{02k}$ is not more than five percent of $\sigma_{01k}$. The agreement between the results of Pivovar and the other two workers, which is shown in Figures 21-24, also suggests that the double-stripping cross section is small.

It was mentioned in Chapter II that these $\sigma_{01k}$ results of Pivovar
are rather suspect, for the following reasons. Both $oo\sigma _{1k}$ for the $He^0$ beam and $2o\sigma _{1k}$ for the $He^{++}$ beam were determined indirectly from the direct measurements of the charge changing cross sections for a $He^+$ beam, namely $10\sigma _{2k}$ and $10\sigma _{Ok}$, combined with measurements of the equilibrium fractions $F_{0\omega}$, $F_{1\omega}$, and $F_{2\omega}$. Pivovar assumed that all double electron capture and double stripping cross sections were negligible in order to drop terms from the equilibrium fractions expressions. This is clearly not justified, because even though those cross sections may be small (≤ five percent) they are multiplied in the equations by other very sizable cross sections. Nevertheless, he did make those assumptions to arrive at the following relations

\begin{equation} \tag{21}
2o\sigma _{1k} = 10\sigma _{2k} \frac{F_{1\omega}}{F_{2\omega}}
\end{equation}

and

\begin{equation} \tag{22}
oo\sigma _{1k} = 10\sigma _{Ok} \frac{F_{1\omega}}{F_{0\omega}}
\end{equation}

for which the experimental errors were ± 24 percent and ± 34 percent, respectively.

It should be noted that in a later paper, Pivovar directly measured $2o\sigma _{1k}$ in Equation 21 above, using a $He^{++}$ beam and obtained results that were as much as 40 percent larger than his own earlier determination. The conclusion to be drawn from this discussion is that even though the cross sections in Equation 21 were measured more accurately than those of Equation 22, the direct measurement of the cross section in Equation 21 changed the value some 30 to 40 percent. It appears quite likely, there-
fore, that the cross sections in Equation 22, with which the present investigation is concerned, may be in even greater error.

In light of the above facts it seems almost fortuitous that Pivovar's results agree so well with those of Allison and Barnett, et al., both of which were believed to have been less than ± 10 percent in error.

The conclusions regarding the discrepancies in the variously measured stripping cross sections for He$^0$ are the following:

1. two experiments that observe the residual slow collision products have measured $\sigma_+$ and agree within ten percent;

2. in both of these experiments, checks on the equality of measuring efficiency in $\sigma_-$ and $\sigma_+$ were satisfactorily made (this will be further discussed for the present experiment);

3. $\sigma_- - \sigma_+ = \sum_{j=1}^{2} j (oo\sigma_{jk})$ was, therefore, accurately determined within ± 3 percent;

4. two experiments were performed elsewhere that directly observed the projectile beam after it had traversed the collision region, and their results for $\sum_{j=1}^{2} oo\sigma_{jk}$ agreed with each other within ten percent;

5. the $\sum_{j=1}^{2} j (oo\sigma_{jk})$ results were about 40 percent greater than the $\sum_{j=1}^{2} oo\sigma_{jk}$ results;

6. if both results were correct, then $oo\sigma_{2k} \approx 2/3 oo\sigma_{1k}$; however, this was shown to be false. Therefore, the final conclusion is that

7. there is a basic measurement error, attributable to $oo\sigma_{1k}$, which is common to one or the other of the two types of experiments.
After thoroughly testing the present apparatus, it is believed that the results obtained with it are accurate within the quoted error limits. Therefore, the discrepancy remains unresolved.

As was discussed in Chapter III, a major concern in this experiment is the possibility that fast neutral beams, which were obtained through electron capture by fast singly charged ions in a gas cell, might be appreciably contaminated with atoms in metastable excited states. Tests were described, however, that gave no evidence for the presence of such metastable states in either $^1 \text{H}_o$ or $^1 \text{He}_o$ beams. An important further verification of the absence of the effects of excited states in the neutral $^1 \text{He}_o$ beam is found in the data of Figure 21 for He neutrals into He target gas. Since the target and projectile particles are identical in this case, the cross sections for the total apparent ionization of the target and the total apparent stripping of the projectile should be equal, provided that both are in the same initial atomic state. The latter is surely the ground state for the room temperature target gas atoms. It is evident in Figure 21 that $$(\sigma_- - \sigma_+)$$ and $\sigma_+$ are in fact equal within the experimental errors and the small deviations from complete agreement are probably not significant.

In Table 5 and in Figures 25-28 are shown the total apparent ion production cross sections $\sigma_+$ and the total apparent electron production cross sections $\sigma_-$ for $^1 \text{H}_o$ incident on He, Ar, $^2 \text{H}_2$, and $^2 \text{N}_2$, respectively. The difference cross sections $$\sigma_- - \sigma_+$$ for these cases are also shown in the figures.

It should be noted that the energy range over which an $^1 \text{H}_o$ beam of satisfactory intensity could be obtained was restricted to 150 to 400 keV.
Table 5. Apparent Cross Sections for Production of Positive Ions $\sigma_+$ and Electrons $\sigma_-$ by an Incident Beam of $^3$H$^0$.
(All Cross Sections are in Units of $10^{-16}$ cm$^2$/molecule.)

<table>
<thead>
<tr>
<th>Projectile Energy (keV)</th>
<th>Helium</th>
<th></th>
<th>Argon</th>
<th></th>
<th>Hydrogen</th>
<th></th>
<th>Nitrogen</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\sigma_+$</td>
<td>$\sigma_-$</td>
<td>$\sigma_+$</td>
<td>$\sigma_-$</td>
<td>$\sigma_+$</td>
<td>$\sigma_-$</td>
<td>$\sigma_+$</td>
<td>$\sigma_-$</td>
</tr>
<tr>
<td>150</td>
<td>0.40</td>
<td>1.1</td>
<td>3.0</td>
<td>6.9</td>
<td>0.91</td>
<td>1.9</td>
<td>3.0</td>
<td>6.6</td>
</tr>
<tr>
<td>180</td>
<td>0.39</td>
<td>1.1</td>
<td>2.9</td>
<td>6.6</td>
<td>0.85</td>
<td>1.7</td>
<td>2.8</td>
<td>6.1</td>
</tr>
<tr>
<td>200</td>
<td>0.39</td>
<td>1.0</td>
<td>2.9</td>
<td>6.7</td>
<td>0.82</td>
<td>1.6</td>
<td>2.7</td>
<td>6.2</td>
</tr>
<tr>
<td>250</td>
<td>0.35</td>
<td>0.95</td>
<td>2.5</td>
<td>6.0</td>
<td>0.71</td>
<td>1.4</td>
<td>2.2</td>
<td>5.3</td>
</tr>
<tr>
<td>300</td>
<td>0.31</td>
<td>0.80</td>
<td>2.1</td>
<td>5.2</td>
<td>0.62</td>
<td>1.2</td>
<td>1.9</td>
<td>4.5</td>
</tr>
<tr>
<td>350</td>
<td>0.29</td>
<td>0.75</td>
<td>1.9</td>
<td>4.8</td>
<td>0.54</td>
<td>1.1</td>
<td>1.9</td>
<td>4.5</td>
</tr>
<tr>
<td>400</td>
<td>0.27</td>
<td>----</td>
<td>1.8</td>
<td>4.6</td>
<td>0.50</td>
<td>1.0</td>
<td>1.7</td>
<td>4.3</td>
</tr>
</tbody>
</table>
Figure 25. Total Apparent Positive Ion and Electron Production Cross Sections, and the Stripping Cross Sections, for H\textsuperscript{0} Atoms Incident on Helium. Key to the results of other investigators: S.I.O.F.(62), Solov'ev, et al., (Reference 8); B.R.(58), Barnett, et al., (Reference 13); B.W.(57), Bates, et al., (Reference 18).
Figure 26. Total Apparent Positive Ion and Electron Production Cross Sections, and the Stripping Cross Sections, for H\(^0\) Atoms Incident on Argon. Key to the Results of other Investigators: S.I.O.F. (62), (Reference 8); B.R. (58), Barnett, et al., (Reference 13).
Figure 27. Total Apparent Positive Ion and Electron Production Cross Sections, and the Stripping Cross Sections, for H\textsuperscript{+} Atoms Incident on Molecular Hydrogen. Key to the Results of Other Investigators: S.I.O.F. (62), (Reference 8); B.R. (58), Barnett, et al., (Reference 13); B.G. (55), Bates, et al., (Reference 19).
Figure 28. Total Apparent Positive Ion and Electron Production Cross Sections, and the Stripping Cross Sections, for $H^0$ Atoms Incident on Molecular Nitrogen. Key to the Results of Other Investigators: S.I.O.F. (62), Solov'ev, et al., (Reference 8); B.R. (58), Barnett, et al., (Reference 13).
This restriction was due to the very rapid fall-off of the electron capture cross section of $H^+$ with increasing energy. The sensitivity of the neutral beam detector was insufficient to maintain an acceptable signal-to-noise ratio with the beam intensities available above 400 keV. At 400 keV, the noise was $\pm 8$ percent of the beam current and rapidly increased with higher energies. Also, about this same energy the electron and ion currents had decreased to the point that the noise was about $\pm 6$ percent.

It was clear that the only significant way to extend these measurements to higher energies was to obtain a larger beam current from the accelerator. It was considered more important, for the present however, to progress on to the next phase of the cross section measurements.

Shown for comparison in Figures 25-28 are the measurements of Solov'ev, et al. $^8$ for $\sigma_+$ and $(\sigma_- - \sigma_+)$, in which the stated maximum errors were $\pm 15$ percent. It is seen in the figures that these $\sigma_+$ measurements are usually some 20 to 30 percent lower than the present values. However, with the exception of the hydrogen target, the results are still within the combined error limits of the two experiments. Reasons will be discussed later for the belief that the present $\sigma_+$ results are more accurate than those of Solov'ev. Also, it is seen that the energy dependence of Solov'ev's $\sigma_+$ is somewhat steeper than the present results. Since the difference cross section $(\sigma_- - \sigma_+)$ is identical to the stripping cross section $\sigma_s$ for the $H^0$ projectile, a comparison is also made with the $\sigma_s$ cross section measured by Barnett and Reynolds $^{13}$ in their fast beam attenuation experiment (discussed in Chapter II). It is seen that their value, which was indicated to be less than $\pm 10$ percent in error, falls between
the present results and those of Solov'ev, in both absolute value and energy dependence.

For the target gases, helium and hydrogen (Figures 25 and 27), a comparison is also made with theoretical values of $\sigma_s$. Figure 25 shows the Bates and Williams\textsuperscript{18} calculation of $\sigma_s$ using the full Born approximation for the reaction

$$H(1s) + He(1s^2) \rightarrow H^+ + e + \sum \text{He}(n'1', n''1'')$$

in which the summation includes an integration over the continuum. This calculated $\sigma_s$ falls between the present and Barnett's result for $\sigma_s$, and, therefore, it is well within the error limits of these experiments. Also, the energy dependence of all three curves appears to be about the same above 250 keV.

A comparison is also shown in Figure 27 with the Bates and Griffing\textsuperscript{19} calculation of $\sigma_s$, using the full Born approximation, for the stripping reaction of $H^0$ on the atomic target $H^0$

$$H(1s) + H(1s) \rightarrow H^+ + e + \sum \text{He}(n1)$$

In this investigation, the target is molecular hydrogen $H_2$. It is reasonable to suppose, however, that in the stripping reaction a hydrogen target molecule is approximately equivalent to two hydrogen atoms. Therefore, for comparison with the present results in Figure 27, the calculated values for the atomic target have been multiplied by a factor of two. As
has been previously observed for other cases, it is seen that this scaling procedure yields a cross section that is greater than any of the experimental values for $\sigma_s$. In fact, it is beyond the error limits of all the experimental results except those of the present experiment. However, since the hydrogen molecule is not exactly equivalent to two hydrogen atoms, the uncertainty in the scaling procedure does not allow any firm conclusion regarding the relatively better agreement of theory with the present results than with those of Barnett.

For convenience in comparing the relative sizes of the ion producing cross sections $\sigma_+$ in the different target gases, Figures 29-31 each shows this cross section for all four target gases for projectiles of He$^{++}$, He$^0$, and H$^0$, respectively. In all cases, the helium target yields the smallest $\sigma_+$ followed by the molecular hydrogen target. It is seen that the ion producing cross section is uniformly larger in argon than in nitrogen for the He$^{++}$ and H$^0$ projectiles, while for He$^0$, the nitrogen cross section curve crosses the argon curve to become the higher one at the upper end of the energy range. However, no particular significance is attributed to this curve crossing. One can also see (by comparing the three figures) that the $\sigma_+$ cross sections successively increase for the projectiles in the order of H$^0$, He$^0$, and He$^{++}$, respectively.

Figures 32-34 are also summary figures, and each shows the electron production cross sections $\sigma_-$ in the four target gases for the He$^{++}$, He$^0$, and H$^0$ projectiles, respectively. These figures show that $\sigma_-$ increases for the target gases in the order helium, hydrogen, nitrogen, and argon, with the exception that argon falls below nitrogen for the case of the He$^0$ projectile. It is seen also that the $\sigma_-$ cross sections increase for
Figure 29. Total Apparent Cross Sections for the Production of Positive Ions of He, H₂, N₂, and Ar by Incident He⁺⁺ Ions.
Figure 30. Total Apparent Cross Sections for the Production of He, H$_2$, N$_2$, and Ar Ions by Incident He$^+$ Atoms.
Figure 31. Total Apparent Cross Sections for the Production of Positive Ions of He, $H_2$, $N_2$, and Ar by Incident $H^\circ$ Atoms.
Figure 32. Total Cross Sections for the Production of Free Electrons in He, $\text{H}_2$, $\text{N}_2$, and Ar by the Impact of $\text{He}^{++}$ Ions.
Figure 33. Total Cross Sections for the Production of Free Electrons in He, H₂, N₂, and Ar by the Impact of He° Ions.
Figure 34. Total Cross Sections for the Production of Free Electrons in He, H₂, N₂, and Ar by the Impact of H₂O Atoms.
the projectiles in the order \( \text{H}^0 \), \( \text{He}^0 \), and \( \text{He}^{++} \), with the exception of \( \text{He}^{++} \) at energies less than 0.4 MeV for which \( \sigma_+ \) falls off more rapidly for \( \text{He}^{++} \) than for the other projectiles, particularly for the \( \text{He} \) target. This indicates that the total apparent ionization cross section \( \sigma_\perp (= \sigma_-) \) for \( \text{He}^{++} \) incident on \( \text{He} \) peaks at a higher energy for this than for the other projectile-target combinations.

The next comparisons of interest are those between the experimental and theoretical results for the ionization cross sections. Of particular interest are those comparisons between the results obtained with various projectiles that are predicted by the form of the theory to be in agreement.

As is well known, ionization cross sections cannot be exactly calculated even for the simplest case of protons incident on hydrogen atoms, although the wave functions for the unperturbed \( \text{H} \) atom are known completely and analytically. An infinite set of coupled differential equations would have to be solved to obtain \( \sigma_\perp \) exactly, so approximate methods must be used.

One of the most useful approximations is that due to Born.\(^{37,38}\) The basic assumption in this approximation is that the potential energy of interaction is small, so that the interaction between the particles may be treated as a perturbation. A sufficient, but not necessary, condition, therefore, is that the interaction energy be much smaller than the total energy of the projectile. This condition is evidently obeyed for sufficiently fast projectiles.

Calculations of simple ionization cross sections in the full Born approximation have been made for only a few of the simplest cases. Among
these, the cases of interest for comparison purposes include those two previous calculations of the stripping reactions of $H^0$ incident on $He^0$ (Equation 23) and $H^0$ (Equation 24); these reactions can be viewed either as stripping of the incident $H^0$ or, conversely, ionization of the $H^0$ by incident $He^0$ and $H^0$, respectively. Other cases of interest include $H^+$ incident on $H^0$ (Reference 15) and $He^0$ (Reference 17), and $He^+$ incident on $H^0$ (Reference 16). These theoretical values of the cross sections will be used for comparison with the absolute magnitudes and energy dependences of the measured values.

Before presenting the above comparisons, it is useful to consider a further approximation, developed by Bethe\textsuperscript{37,38,40} which produces results with a simpler mathematical form. Cross sections calculated in the Bethe-Born approximation tend to the more general results of the full Born treatment for very high impact velocities. The main feature of the Bethe approximation is the assumption that there is very little contribution to the cross section for values of the projectile momentum change $K$, greater than a certain value $K_0$, which is much less than the maximum value allowed by the conservation laws. With this assumption, an integral over $K$ that occurs in the formulation is terminated at the upper limit $K_0$. A factor $\exp(ikz)$ in the integrand can then be expanded, and only the first term which produces a nonvanishing contribution to the integral need be retained for the case of very high impact velocities. With this approximation, the following result for a point charge projectile incident on a stationary target may be obtained.

\begin{equation}
\sigma_i = AZ^2 \frac{M}{E} \log_e \left( \frac{BE}{M} \right) \tag{25}
\end{equation}
where $E$ is the kinetic energy of the incident ion, $Z$ is the charge number of the incident ion, and $M$ is its mass in units of the proton mass. The constants $A$ and $B$ are characteristic of the target atom and do not depend on the nature or the energy of the incident ion. Therefore, an empirical evaluation of $A$ and $B$ for a given target atom from experimental measurements of $\sigma_i$ for any one type of projectile can be used in Equation 25 for two purposes: first, to extrapolate the measured $\sigma_i$ for the given target atom and projectile to energies outside the experimental range in particular to higher energies, and second, to estimate $\sigma_i$ for the given target atom and some other projectile with a different value of $Z$ and/or $M$. Both of these purposes will be employed in the comparisons.

It is worthy of note that the quantities $M$ and $E$ appear in Equation 25 only in the ratio $E/M$, so that the expression predicts that various projectiles of equal $Z$ but different $M$ will have equal cross sections for equal velocities. This is a well known feature of the theory, which is also displayed by the full Born approximation.\textsuperscript{15,37,38}

It should be emphasized that all of the discussion of Equation 25 above applied only to the cross sections for simple ionization events, in which the projectile ion suffers no change in its charge state. However, as was seen in Chapter II, the observed ionization cross sections $\sigma_i$ are not restricted to these simple ionization events. In addition, the relationships discussed here should apply, strictly speaking, only to point-charge projectiles, i.e., to electrons or bare nuclei. An incident ion carrying bound electrons might, however, be expected to be equivalent in the simple ionization process to a partially screened point charge having an "effective" charge $Z e$ lying somewhere between its actual net charge and
its nuclear charge. The value of $Z$ for a given ion, and indeed the validity of the whole concept of an effective projectile charge, can for the present be evaluated only be experimental test. The concept will be useful only if $Z$ for a given projectile ion can be shown to be independent of the target-atom type and of the collision energy, or at least asymptotically so at high energies.

The preceding discussion enumerated the following four separate types of comparisons to be made between the theoretical and experimental results:

1. comparison of absolute magnitudes and energy dependence;

2. comparison between cross section measurements that are predicted to be equal when the projectiles are scaled to be equicharge and equivelocity;

3. comparison of cross sections which are extrapolated by means of the constants $A$ and $B$ outside of the energy range of the measurement; and

4. comparison of the effective charge of various equivelocity projectiles.

In Figures 35-38 the total apparent ionization cross sections $\sigma_i$ for $\text{He}^{++}$, $\text{He}^+$, and $\text{H}^+$ in the target gases hydrogen, helium, argon, and nitrogen are plotted together with the previously published results$^{35,39,41-44}$ for $\text{H}^+$ and $\text{He}^+$ that were measured in this laboratory. The energy axis is shifted a factor of four, according to Equation 25, to compare the hydrogen with the helium projectiles of equal velocity.

In order to compare the experimental results on molecular hydrogen targets with the theoretical predictions for atomic hydrogen, a scaling
Figure 35. Total Apparent Ionization Cross Sections $\sigma_i$ for H and He Ions and Atoms Incident on Molecular Hydrogen, Compared with the Calculated Curve: $\sigma_i = AZ^2M/E \ln(BE/M)$ with A and B Evaluated from Corresponding $H^+$ Data (Reference 34), for $Z = 1$ and $Z = 2$. Also Shown Are Theoretical Calculations for Atomic Hydrogen Targets, Scaled to Molecular Hydrogen Targets, for Incident $H^+$ (BG 53, Bates and Griffing, Reference 15) for $Z = 1$ and $Z = 2$, for Incident $H^0$ (BG 55, Bates and Griffing, Reference 19), for Incident He$^+$ Ions (BMS 57, Boyd, Moiseiwitsch, and Stewart, Reference 16), and for Incident He$^0$ Atoms (BW 56, Bates and Williams, Reference 18).
Figure 36. Total Apparent Ionization Cross Sections $\sigma_i$ for H and He Ions and Atoms Incident on Helium, Compared with the Calculated Curve $\sigma_i = AZ^2 M/E \ln(BE/M)$ with $A$ and $B$ Evaluated from Corresponding Proton Data (Reference 34), for $Z = 1$ and $Z = 2$. Also Shown Is the Theoretical Calculation for Equivelocity Protons on Helium (Reference 17) for $Z = 1$ and $Z = 2$. 
Figure 37. Total Apparent Ionization Cross Sections $\sigma_i$ for H and He Ions and Atoms Incident on Argon, Compared with the Calculated Curve $\sigma_i = \frac{A}{Z^2 M/E} \ln(BE/M)$ with A and B Evaluated from Corresponding Proton Data (Reference 34), for $Z = 1$ and $Z = 2$. 
Figure 38. Total Apparent Ionization Cross Sections $\sigma_i$ for H and He Ions and Atoms Incident on Molecular Nitrogen, Compared with the Calculated Curve $\sigma_i = [AZ^2M/E] \ln(BE/M)$ with A and B Evaluated from Corresponding Proton Data (Reference 34), for $Z = 1$ and $Z = 2$. 
procedure was employed. This procedure, suggested by Bates and Griffing, allows for the difference in ionization potential between the atomic and molecular targets. It was applied to the theoretical case of $H^+$ incident on $H_2^+$ to compare with the observed values in Figure 35. The solid portion of the $Z = 1$ curves labeled "calculated" in each figure represents the plot of the proton results referred to as the "equivelocity proton energy" abscissa. The dashed portion of each "calculated" curve is extrapolated outside the data range by means of Equation 25. The curve labeled BG 53 is the calculation for $H^+$ incident on $H_2^+$ scaled from the atomic to the molecular case as discussed previously. It is seen that the agreement is rather good throughout the experimental energy range; the experimental results average about ten percent larger than the theoretical values. The energy dependencies of the two results are essentially the same.

The scaling procedure used for the preceding comparisons strictly applies only to a point charge projectile ion with no bound electrons. For projectiles with bound electrons, there are more terms in the interaction and the form of the dependence of the results on the projectile energy and ionization potential is consequently more complex. It is not evident that the same simple scaling procedure should have any validity. Nevertheless, it was tried for $He^+$, $He_2^+$, and $H_2^+$ projectiles, and for the case of $He^+$ incident on $H_2^+$ good agreement was obtained.

The curve labeled BMS 57 in Figure 35 represents the theoretical calculation for $He^+$ incident on $H_2^+$, scaled to $H_2^+$ as previously discussed. It may be noted that the agreement with the estimated ionization cross sections from the $He^+$ measurements is excellent. However, this agreement should be regarded with some reservation because the evaluation of $\sigma_1$ for
the He$^+$ projectile is complicated by the fact that the projectile can undergo both electron capture and stripping reactions. Therefore, in order to arrive at a value for $\sigma_i$, it was necessary to estimate the relative sizes of several cross sections.

The results for He$^0$ and H$^0$ scaled in the above manner, however, were lower than the experimental values by about 30 percent and 50 percent, respectively, and they are not shown in the figure. Instead, the results obtained by simply doubling the atomic cross sections are presented and are seen to be in substantially better agreement with experimental values. The curve in Figure 35 labeled BG 55 represents the theoretical value for H$^0$ incident on H$^0$ multiplied by a factor of two. It is seen to lie about ten percent above the measured values and to have essentially the same energy dependence. Also shown in this figure is the theoretical calculation of He$^0$ incident on H$^0$, multiplied by a factor of two and labeled BW 56. This curve is about 14 percent below the measured values, and in the upper part of the energy range, as has been observed to be the usual case, the two results have about the same energy dependence.

Although no explicit calculation is available in this energy range for He$^{++}$ incident on these four gases, the form of Equation 25 predicts that the proton measurements multiplied by $Z^2 = (2)^2$ for He$^{++}$, and scaled to be equivelocity with He$^{++}$, should have the same cross section for sufficiently high velocity. The "calculated" curve in Figure 35 labeled $Z = 2$ represents the proton results scaled in the above manner. It is observed that the He$^{++}$ results demonstrate quite precisely the expected behavior, i.e., they are just four times the proton results, for
the higher energies used in this experiment. Also scaled according to Equation 25 is the theoretical calculation for H\(^+\) incident on H\(^0\), scaled to H\(\alpha\). It is also seen to provide good agreement with the observed values at the highest energies used in this investigation.

In Figure 36, the same type of experimental curves discussed in the preceding paragraphs is shown. The only available calculation for ionization of the helium target is shown as the curve labeled M 58 for incident H\(^+\), and good agreement is obtained between the calculated and measured values. Both of these curves, scaled according to Equation 25 and labeled \(Z = 2\), are seen to be in generally good agreement with the He\(^{++}\) measurements for the highest energies, particularly the theoretical curve.

For the heavier target gases, argon and nitrogen, shown in Figures 37 and 38, respectively, it is seen that the He\(^{++}\) results appear to be approaching the scaled proton results at some higher energy, perhaps two or three MeV.

The final comparison to be made with these measurements is to determine whether or not the concept of the effective charge is valid for the non-point charge projectiles. The requirement for this concept to be valid is that the cross section curve for the non-point charge projectile be uniformly separated from that of a true point charge projectile such as H\(^+\) or He\(^{++}\), at least asymptotically so at high energies.

A comparison of the He\(^+\), H\(^0\), and He\(^0\) results with the H\(^+\) results indicates that: the previously measured He\(^+\) curves are roughly about a factor of 1.5 above the H\(^+\) curves; the H\(^0\) curves are uniformly lower than the H\(^+\) curves by about a factor of 0.64 in the upper energy range; and the He\(^0\) curves are approximately equal to the H\(^+\) curves for both the
lightest and heaviest targets, i.e., hydrogen and argon, and are about a factor of 1.2 above the H⁺ results for the other two cases—this amount of variation is outside of the error limits for the He⁰ projectile. It is concluded, therefore, that He⁺ and H⁰ projectiles do possess an effective charge, according to Equation 25, of $\sqrt{1.5} = 1.2$, and $\sqrt{0.64} = 0.80$, respectively. However, it appears that this effective charge concept is not applicable to the He⁰ projectile.

**Conclusions**

The experimental values of the total apparent cross sections for productions of ions, $\sigma_+$ and of electrons, $\sigma_-$, were measured for the cases of He⁺⁺, He⁰, and H⁰ incident on the target gases He, Ar, H₂, and N₂.

For the cases involving He⁺⁺ projectiles, the only comparison data that were available were total charge changing cross sections for the capture of electrons by the projectile, which were equivalent to the difference $(\sigma_+ - \sigma_-)$ in the present data. It was noted that the agreement was excellent, which provided a strong confirmation of the validity of both the apparent ion production and the total charge changing cross section measurements.

For the cases involving an atomic helium beam, comparison data were available for $\sigma_+$ and were in reasonably good agreement. The present results for $(\sigma_- - \sigma_+)$ were seen to be about 40 percent greater than was expected from certain related results of the other investigators, which all involved the observation of the change in beam composition as it passed through the target gas. It is pointed out that one other investigator, who measured the residual slow collision products (as in the present experi-
ment) also obtained results that were some 40 percent greater than those referred to above. Unfortunately, these results, which were apparently in agreement with the present values, were not published and no response was received to a request for those data. It was concluded from the present results for $\sigma_+$ that it was not very meaningful to define an "effective charge" for He$^0$ that represented the charge of a hypothetical point-charge ion of the same mass, that has the same cross section for simple ionization at high energies.

The data for $(\sigma_- - \sigma_+)$ obtained for the H$^0$ projectile were usually in rather good agreement with the comparison data; however, the agreement of the present $\sigma_+$ cross sections with the comparison values varied considerably among the various target gases. Also, in some cases the present and comparison results for $\sigma_+$ displayed a considerably different energy dependence. Confidence in the present results for $\sigma_+$ was considerably enhanced when it was noted that, for all four target gases, the H$^0$ and H$^+$ ionization cross sections, $\sigma_\parallel = \sigma_\parallel^\parallel$, were displaced a constant amount from each other above about 300 keV. It appeared that this close correlation, although not expected a priori, would be highly unlikely to occur in all four target gases if there were serious random errors present in the results of the individual gases. It was, therefore, concluded that the excellent correlation was testimony to the accuracy of the present $\sigma_+$ results for the H$^0$ projectile.

From the form of the cross section in the Bethe-Born approximation (Equation 25), this constant offset in the H$^0$ and H$^+$ ionization cross sections implied that the "effective charge" concept could be applied to the
H° projectile. The calculated value of the effective charge was 0.80 e.

It is interesting to note that the "effective charge" concept was applicable to the hydrogen projectile H° and the hydrogenic projectile He⁺; however, it was not deemed applicable to the He° projectile in this experiment. No explanation of this observation is offered at present.

It was observed that generally good agreement was obtained between the experimental and theoretical cross sections, even those that were scaled from atomic to molecular hydrogen. It is concluded, therefore, that the theory pertaining to the high energy cross sections measured in this work is substantially correct for relative velocities above about $5 \times 10^6$ m/sec (≈ 0.5 MeV helium; ≈ 0.1 MeV hydrogen), and in some cases that the theory appears to be valid at lower velocities.
APPARATUS AND TECHNIQUES EMPLOYED IN THE MEASUREMENTS OF THE PARTIAL IONIZATION CROSS SECTIONS

Discussion of Some Fundamental Design Considerations for This Apparatus

In order to subdivide the individual cross sections that comprised the total apparent ion production cross section, into groups that correspond to the cross sections for the formation of ions of specified charge states, some type of ion spectrometer must be used. The initial concept of this spectrometer was predicted on the assumption that no significant fraction of the slow ions would be formed with initial kinetic energies in excess of perhaps 100 eV. The analyzer was to be mounted so as to sample at 90° to the direction of the fast beam. Its entrance slit was to be cut in the "active" ion collector plate of the parallel plate collision region. The electric field normally applied to sweep to the active plate all of the slow positive ions formed in a well defined collision volume, would simply sweep some of these ions into the spectrometer entrance slit. If the width of the slit were made an accurately known fraction of the length of the active plate, this same fraction of all the ions formed in the collision volume should be swept to the slit. It was intended that analysis and measurement of the ion stream through the slit would be made simultaneously with measurement of the total current collected to the plate. Comparison of the ratios of these currents to the
geometrical ratio would be a direct check on the collection efficiency of the analyzer, and the simultaneous measurement of the already well established total ion production cross sections would provide a continuous check on several of the more important factors in the measurement.

Before any detailed design was begun, however, further study was given to the adequacy of the underlying assumptions. The main aspects of these deliberations will be detailed below; the result was, however, a major decision to discard the concept of a fixed-angle spectrometer with a collection field in favor of a spectrometer that is movable in angle, and which samples with a narrow angular acceptance from a field-free collision region.

The principal technical reason for this change of plans was mounting evidence that a significant fraction of the recoil ions, particularly the multiply-charged recoil ions, are formed with substantial initial energies. Such energies would then require equally substantial values for the collection field voltages to assure that all of the ions formed in a well defined collision region would reach the spectrometer entrance slit. Furthermore, the details of the angular distribution of the initial motion could influence the transmission efficiency of the ion optics of the spectrometer and require the use of still higher collection fields. Quite apart from any other difficulties this might entail, a large collection field would have the serious disadvantage of distorting the initial energy distribution. The incident beam has a finite spatial width; thus recoil ions would be formed over a region across which the electrostatic potential varies, and they would be given variable amounts of energy by the field as they were accelerated to the slit. Thus, a recoil energy
spectrum analysis would be complicated by the use of a collection field.

It was felt that some indication that the ions possessed substantial recoil energies was shown in Figures 10 and 11. On very careful examination, it has been determined that the slow ion current collected to the "active" plate of the ion collection assembly (discussed in Chapter IV) as a function of the voltages applied to the plates does not really "saturate" and become constant until the equal plus and minus voltages approach 200 volts or more. The few percent increase between 100 volts and 200 volts was small enough to be partially masked by the random errors in a single test, but the pattern of the increase over a large accumulation of data was unmistakable. It was felt that this slight increase in ion current indicated that a small but significant fraction of the slow ions is formed with energies of more than 100 eV. It appeared that the fraction having energies above 200 eV was too small to have a significant effect on the accuracy of the total apparent ion production cross sections. However, from this observation it did not follow that a similarly small fraction of all of the multiply-charged ions formed also had energies less than 200 eV, if the multiply-charged ions represented only a small fraction of the total ion current in the first place. Indeed, there is much evidence to the contrary.

The energy and momentum conservation equations, that are applicable to the inelastic ionizing collisions of this experiment, can be used to give the relation between the energy imparted to the target $T_2$ and the other important collision parameters, according to Afrisomov, as follows:
\[ T_2 = \frac{m_1 m_2}{(m_1 + m_2)^2} T_0 \left( \cos \theta \pm \sqrt{\cos^2 \theta - \frac{(m_1 + m_2) Q}{m_2 T_0}} \right)^2 \]

where \( m_1 \) and \( m_2 \) are the projectile and target mass, respectively; \( T_0 \) is the initial kinetic energy of the projectile; \( \theta \) is the recoil angle of the target, and \( Q \) is the inelastic energy loss by the collision partners. It should be noted that for a given recoil angle \( \theta \) the recoiling targets will in general have two different energy components and the more energetic ions will be found at smaller values of \( \theta \). The existence of these two energy groups is another very important reason that one should be extremely careful, when using a collection field, to assure that both groups are efficiently collected. It is conceivable that an investigator that used weak to moderate collection fields (sufficient for the low energy ions) might overlook the presence of the energetic component.

Afrosimov and Federenko \(^{46}\) have used a magnetic slow-ion analyzer which is rotatable about a field-free collision region and has a direction-defining collimator, to study the relative production of each slow ion charge state, differential in the recoil angle. The instrument had sufficient momentum resolution to provide a low resolution measurement of the recoil ion energy, and this was supplemented by a retarding potential feature for independent energy determinations. In studies of \( \text{Ne}^+ \) and \( \text{Ar}^+ \) ions up to 0.18 MeV in neon and argon targets, they found that quite appreciable fractions of the higher charge state recoil ions had initial energies of more than 200 eV. In fact, it was observed that virtually all of the \( \text{Ar}^{5+} \), produced from an Ar target gas by incident \( \text{Ar}^+ \) projec-
tiles, had energies greater than 1 keV. They remarked that earlier studies made in their own laboratory of the same collision partners, with a fixed angle analyzer and a collection field such as we had contemplated, were significantly in error for the recoil ions that were more than triply charged, particularly when the mass of the projectile was of the same order as the target mass.

Morgan and Everhart have also studied the energy distribution of the recoil ions in Ar on Ar collisions, at selected recoil angles that were well forward from 90°, corresponding to very hard collisions. They did indeed find recoil particles at these angles, particularly those of the higher charge states, with the energies of 1 keV and more expected for these angles. This particular paper gives no absolute figures on the intensities of the recoils, as a function of the recoil angle, to permit estimation of the relative contribution of such hard collisions to the total cross section, but it does verify that there are measurable numbers of recoils, particularly for the higher charge states, at these forward angles.

The evidence cited thus far for energetic recoil ions has in each case involved a heavy incident ion. The case of incident protons, which were used in the present experiment, has been studied with fixed-angle spectrometers using a collection field by Solov'ev, et al. and by Wexler. The measurements of Solov'ev, et al., cover energies only up to 0.18 MeV, while those of Wexler ranged from 0.80 to 3.75 MeV. Both groups have studied protons on He, Ne, Ar, and Kr targets. While their energy ranges do not overlap, a comparison of sorts can be made by extrapolation. There is an appearance of good agreement for the low charge states of the
slow ions, but this actually results from the fact that neither set of measurements was absolute. Solov'ev's group normalized to their own total ion production measurements, while Wexler normalized to previous measurements made in this laboratory on total ion production cross sections.\textsuperscript{41,42}

The apparent agreement for the ions of low charge state thus really reflects only the rather good agreement between these two sets of total ion production measurements. Significantly, the agreement does not appear to be as good for some of the higher charge states of the recoil ion; in fact, for some cross sections, the extrapolated comparisons disagree by more than a factor of eight.

The suggested conclusion is that measurements of absolute or even only relative cross sections for the production of multiply charged slow ions, using a fixed angle spectrometer and relying on collection of the ions to the entrance slit by an electrostatic field, can be substantially in error in some circumstances. Therefore, it was considered essential to include the capability of a field-free angular measurement and yet not preclude the use of a collection field when desired. It is not indicated that either of these collection methods is individually sufficient for the general case, but rather that a combination of the two methods is necessary. A spectrometer movable in angle, capable of collecting within a well defined angular interval from a field-free collision region, would produce results differential in the recoil angle. Integration of the results over the recoil angles to get the total production cross section for a given charge state should be more reliable than the simpler measurement, because the ion collection efficiency would be purely geometrical.
However, when the recoil ion energies are low, collection difficulties are produced by weak stray fields in the chamber. Even though evidence has been presented for the presence of energetic recoil ions, the fact still remains that most ions of lower charge states have energies of only a few electron volts, and their collection efficiency can be seriously disturbed by stray fields. Therefore, it appears that the use of a collection field to measure the cross sections leading to production of low energy ions, and the field-free collision environment to measure the cross sections for production of energetic recoils should be a satisfactory combination of techniques.

A Nier-type magnetic deflection spectrometer, with electrostatic preacceleration was selected for this investigation. Two of the advantages of this type of spectrometer are that it can be used to provide a charge-to-mass analysis of ions with a large range in energy, and that it will provide a momentum analysis of each charge state of the more energetic ions. One of the difficulties associated with this type of spectrometer is that the magnet is a potential source of stray fields in the vicinity of the collision chamber. However, the magnet can be shielded, even though it is sometimes difficult.

Also relevant to the overall design decision was the fact that it was desirable to construct this analyzer to be fully compatible with later evolution of a coincidence experiment, in which the final charge states of both of the partners from a single collision will be determined. Originally, the coincidence experiment had been conceived in terms of fixed-angle spectrometers and a collection field. As such, the results would still be subject to the same possible errors due to hard collisions as
described in the preceding discussion. An experiment with movable spectrometers, differential in both the scattering and the recoil angles, would avoid this difficulty, while producing a more detailed result of intrinsic interest. In addition, if there is sufficiently good angular resolution, the inelastic energy loss in each collision is unambiguously determined from these two angles. The only atomic collision coincidence experiments that have been published thus far have in fact been designed with emphasis on study of details of the inelastic energy loss.\textsuperscript{51-53} While the primary interest in the program of this laboratory will be in the measurement of cross sections, it was concluded that a doubly-differential apparatus would be of sufficiently greater general utility as to represent the clearly preferable choice.

Thus, the new apparatus was designed to perform measurements that are differential in the recoil angle and have sufficient momentum resolution to provide a moderate resolution scan of the energy spectra of the recoil ions.

The general mechanical quality of this apparatus, such as the machining, the precision rotation bearings, and the number of adjustments provided, are all directly connected with the aiming accuracy of the fast beam, the recoil ion spectrometer, and a future fast beam spectrometer. In the present investigation of the angular distribution of the recoil ions, it was desirable to have an angular resolution of about ± 0° 30’ which, in the geometry of the spectrometer collimator, necessitates the use of rather narrow apertures (of the order of 0.020 inch). Since the size of the collision region viewed by the spectrometer is defined by the intersection of the beam and spectrometer collimators, it is important to
maintain a high degree of aiming precision as the spectrometer is rotated in angle.

The later evolvement of a coincidence experiment through the addition of a fast beam spectrometer will place considerably greater requirements on the accuracy and constancy of the aiming of the spectrometers. In fact, more than twice as great an angular resolution will be required of each spectrometer for the determination of inelastic energy losses. Consequently, the accuracy with which they must be aimed at a common point in the beam path, as they are rotated in angle, is correspondingly increased. The apparatus used to achieve this general level of aiming accuracy is described in the following sections.

General Description of Apparatus

An overall view of the new apparatus is shown in Figure 39. The apparatus is connected to the electrostatic beam analyzer following the gas cell by means of a flexible bellows, which permitted alignment with the beam emerging from the analyzer. In the new apparatus the beam was passed through a collimating cone and into the collision chamber in which it underwent ion producing collision with the target gas. Also inserted into the collision chamber was the incident beam detector and the slow ion collimator cone of the spectrometer, both of which were mounted such that they could be rotated about a fixed point in the collision region. The spectrometer, which was rigidly connected to the slow ion collimator, employed a system of electrodes for ion acceleration and focusing and an electromagnet to analyze the ion beam. An electron multiplier was employed for the detection of the ions as they emerged from the analysis
Figure 39. Overall Drawing of Apparatus Employed for the Measurements of Partial Cross Sections.
region.

All of the components mentioned thus far are mounted on supports (shown in Figure 39) that are mechanically attached to a vertical support column, or spindle, whose axis passes through the center of the collision chamber. The lower end of the spindle is securely seated and locked in a machined housing located in the center of the tripod base that supports the entire apparatus. The supports for the beam detector and slow ion spectrometer are rigidly bolted to separate bearing housings, each of which rotates on ultra-precision bearings about the common spindle. (In this experiment, however, the rotation feature of the fast beam detector was not used except to assure that the detector was centered in the $\theta = 0^\circ$ position.) On the side of the bearing housing opposite the spectrometer there is located a second support which serves two purposes. First, it provides a mechanical attachment for an angle indicator for the spectrometer. The angle scale, which is divided into five minute increments, is mounted near the circumference of the large diameter steel plate which, itself, is bolted to the top of the tripod base. The second purpose of the support is that it provides a position for a spectrometer counterweight. Even though calculations indicate that the 200 pound weight of the spectrometer is insufficient to produce a significant deflection of the spindle, the precision to be required on the coincidence experiment is more easily guaranteed if the spectrometer is counterbalanced.

There are two complete sets of alignment adjustments. Those referred to as internal adjustments are the vertical and horizontal adjustments located on the supports for the beam collimator, the beam detector, and the slow ion analyzer. These adjustments and the precision machining
in this apparatus are to assure that these components rotate in the same plane (normal to the spindle axis) and about the same point (within 0.001 inch) in the collision region. The procedure for attaining this alignment is described in Appendix IV.

The second set of adjustments referred to as external adjustments are located on the base of the apparatus and are the adjustments used for alignment of the apparatus with the Van de Graaff beam. The jack screws in each leg of the tripod provide elevation and tilt, and the angular rotation of the apparatus is accomplished by means of a jack screw in a separate rotation plate, which is located beneath the plate on which the tripod rests.

The entire apparatus, with the exception of the tripod base, was constructed from nonmagnetic materials.

The Beam Collimator

For the purpose of the present discussion, a more detailed view of the beam and slow ion handling system is shown in Figure 40.

The beam emerging from the electrostatic analyzer following the gas cell entered the apparatus at the top right portion of the figure and passed through the collimator, through the collision chamber, and into the detector.

The beam collimator has provisions for three apertures. The first aperture position is in the flange connection between the bellows and the "T-shaped" pipe to which the two-inch cold-trapped mercury diffusion pump is attached. However, on the basis of the results obtained in the old apparatus, which were previously discussed, it was decided that a two slit
Figure 40. Detailed Drawing of Collision and Analysis Regions.
collimator would be sufficient for the present work. Therefore, the first aperture of the collimator through which the beam passed was located in the base of the "beam collimator cone," and the second was in the narrow end of the cone which protruded into the chamber.

All the apertures were machined in small brass "buttons" of 0.40 inch diameter and about 0.005 inch thick in the end with the aperture. The first collimating aperture was of 0.025 inch diameter and the button was fitted in a three-inch diameter plate located in the base of the cone. Six holes of 5/8 inch diameter removed most of the metal in this mounting plate to provide good pumping speed at the small end of the cone which contained the final 0.035 inch diameter aperture. However, it was found necessary (as will be discussed) to drill a 0.20 inch hole in the base of the collimator cone in order to provide sufficient pumping speed in the collision chamber. With this arrangement, it was observed that when the collision chamber was evacuated, the pressure in the entrance to the collimator was about $4 \times 10^{-7}$ Torr, as measured on a Veeco (RG-75K) ionization gauge; when the chamber was filled with the target gas to a pressure of about $1 \times 10^{-4}$ Torr, the pressure at the collimator entrance was less than $5 \times 10^{-8}$ Torr. It will later be demonstrated that this collimator pressure is sufficiently low so that charge changing collisions by the beam are unimportant in this investigation.

The difficulties associated with fast electrons in the beam were not as important in this as they were in the old apparatus, because here the electron current was not to be measured, and hence the fast electrons were collected in only the beam detector. Therefore, the only errors these electrons could cause were either through ionization of the target
gas, or by being collected with the beam. It was demonstrated in the old apparatus that even when the collimator was poorly aligned the fraction of electrons in the beam corresponded to considerably less than one percent. It is generally true, as will be shown in later figures, that electrons, regardless of their energies, have ionization cross sections less than those of the ions in this (0.15 to 1.00 MeV) energy range. The conclusion is that the fast electrons will not cause any appreciable error in the measurements.

The Beam Detector

As the beam emerged from the small end of the collimator cone, it passed through the target gas, with which the collision chamber was filled, for about one inch before it entered the beam detector. The purpose of the short path in the target gas was to minimize the change in beam composition, through charge changing collisions, before the beam passed the relatively short (0.025 inch) portion of the path viewed by the spectrometer collimator.

The design of the beam detector was determined primarily by the desire to maintain the collision region as free of stray fields as possible. It is generally acknowledged\(^{54}\) that one of the most effective schemes for the measurement of the current delivered by a high energy beam of particles is to trap the beam in a deep cup in which the entrance aperture subtends a small solid angle at the beam impact point. The purpose of the small solid angle is to minimize the probability that a particle ejected by the beam impact will escape the detector. Since, however, the emission of particles such as secondary electrons and sputtered target atoms does not fol-
low an isotropic distribution, it is difficult to associate the size of
the solid angle with the efficiency with which these particles are con-
tained in the detector. To further increase the efficiency of contain-
ment, an appropriately biased suppression grid or electrode is normally
employed.

Both the small solid angle and the suppression grid were used in
the present detector. It is obvious at once, however, that the electric
field from the voltage applied to a grid in the detector might very well
penetrate into the collision region and thereby cause an appreciable change
in the transmission of the spectrometer collimator. In order to minimize
the disturbance of the conditions in the collision region, a long narrow
entrance tube was provided on the entrance to the detector to suppress
the penetration of the electric field.

The detector is shown in Figure 40. The beam passes down the rather
long grounded entrance tube and through the grid which is spot welded to
its base. Immediately following this grid is the suppression grid, which
is followed by the beam collector. It was found that a suppressor grid
potential in excess of about -15 volts was sufficient to cause the measured
beam current to saturate. A potential of about -30 volts was used for
these measurements. The current to the electric field suppressor tube was
measured and found negligible compared to the beam current.

The current from the beam detector was measured by means of a Keith-
ley (Model 410) pico-ammeter. However, on the occasions when the analyzed
ion counts (discussed in the following) were accumulated over periods of
several minutes, it was difficult to estimate the average beam current
over that period. This difficulty was avoided by integrating the signal
over the measurement period through use of a dc voltage-to-frequency con-
verter (Dymec Model DY 2210). This V-to-F converter was connected to the
recorder output of the pico-ammeter and was adjusted to produce about 1000
pulses per second for full scale deflection of the pico-ammeter. These
pulses were then fed into a 100 kC scaler, and in this manner the integrated
beam current over a given period of time could be determined.

The Collision Chamber

The collision chamber was constructed from thick-walled stainless
steel tubing and is attached to the beam collimator, the beam detector, and
the spectrometer collimator by means of three welded stainless steel bel-
lows. These bellows are welded to the chamber on one end and on the other
end of each is welded a rotatable flange (for use with aluminum gaskets).
The 20° offset in the side of the chamber, through which the beam colli-
mator protrudes, was designed to allow the maximum angular rotation of the
spectrometer before either of the two collimators would contact the chamber
wall and thus stop the rotation. The analyzer rotation was further in-
creased by permitting the chamber itself to rotate, as described in the
following paragraphs. Both the top and bottom covers of the chamber are
removable six-inch diameter Con-Flat flanges (for use with copper gaskets)
manufactured by Varian Associates. The bottom flange had a 3/8 inch dia-
meter hole drilled one inch deep into a boss in its center. A matching
hole was drilled in the top of the spindle on which the bottom flange of
the chamber rests. A slightly undersized stainless steel pin was fitted
into these two holes to keep the vertical axis of the chamber aligned with
the spindle axis. This retaining pin was loose enough to permit the cham-
ber to rotate into equilibrium about its vertical axis under the influence of the bellows forces as the spectrometer was rotated.

On the top flange to the chamber was mounted a rotatable cross fitting, which was also manufactured by Varian Associates. The three flanges of this cross were employed to connect such things as an ionization gauge (Veeco RG-75K) or a McLeod gauge (CEC GM 110), an electrical feed through, and an eight liter-per-second Vac-Ion pump (Varian 911-5000) to the collision chamber.

It should be recalled that one of the prime concerns with this collision chamber and the spectrometer collimator was to minimize the presence of stray fields. The beam detector was designed with this in mind, and it should be noted that only metal gaskets are used on the collision chamber. Elastomer gasket materials such as neoprene and Buna-N have been observed to outgas substantial quantities of hydrocarbons which, it was feared, would coat such critical surfaces as the spectrometer collimating apertures. If these insulating deposits were allowed to form and acquire an electrostatic charge, a stray field would be established, which probably would disturb the transmission of the collimator, particularly for the low energy ions. A further advantage of the stainless steel chamber with metal gaskets was that it could be heated, which helped remove condensable deposits on the surfaces. The heating to temperatures around 110°C was accomplished by means of a number of heating tapes which were wrapped around the chamber and the adjacent components.

It should also be noted that cold-trapped mercury diffusion pumps were used and for the same reasons as given above. Even with well designed cold traps, some creepage of the pumping fluid of oil diffusion pumps is
usually observed, because oil wets all trap surfaces and, therefore, can migrate along the surface into the system. However, mercury does not wet stainless steel, the material of which the present traps were constructed, consequently the mercury does not creep. It should be noted, however, that even if mercury did creep into the system, a thin conducting film of mercury is clearly preferred over that of oil.

There is still one source of stray fields that has not been discussed yet, and that is contact potentials between dissimilar metals in the chamber. To minimize the effect of this, the entire collision chamber, flanges, collimators, apertures, and the beam detector, were rhodium plated. Rhodium was chosen because it is a noble metal that does not oxidize or amalgamate. Therefore, should a substantial quantity of mercury get into the chamber, it could very simply be cleaned off of the surfaces.

A Vac-Ion pump, which operates by ionizing and "gettering" the gas, was employed to directly evacuate the collision chamber prior to the measurement of cross sections. With this and the diffusion pumps on the beam collimator and the spectrometer working, the chamber pressure was about $3 \times 10^{-7}$ Torr after bake-out, as measured on an ionization gauge. However, the Vac-Ion pump employed a 1000 gauss magnet, which had a substantial fringe field in the collision chamber. Therefore, this pump was not operated during cross section measurements, and the magnet was removed from the vicinity of the chamber. Even without the aid of the Vac-Ion pump, a satisfactory low background pressure of $1 \times 10^{-6}$ Torr was obtained. However, before the previously mentioned 0.20 inch hole was drilled into the collimator base, the equilibrium pressure was about $1 \times 10^{-5}$ Torr, which, as will be seen later, is about ten percent of the target gas pressure.
The target gas was obtained from a standard high pressure cylinder. It was first passed through a high pressure regulator and then through a vacuum regulator, which, because it was more sensitive to small pressure fluctuations, considerably improved the pressure regulation. Next, the gas was passed through a copper coil immersed in a dry ice and acetone mixture (-79°C) which served to remove some of the condensable impurities. Following this cold trap, the gas was passed through an Edwards metering valve and into an adapter that screwed into the base flange of the beam collimator. This flange contained a radial hole 1/16 inch in diameter (shown in Figure 40) that made a right angle turn and emerged from the flange face next to the base of the cone. Following this route, the target gas emerged inside the collision chamber.

**The Spectrometer**

Two different types of measurements, which required different collimator extensions, were performed with this spectrometer. The first measurements involved the use of a field-free collision region and observation of the angular distribution of the recoil ions. The second type of measurement involved the collection with an electric field of the ions formed along a portion of the beam path, regardless of their original directions of recoil.

The two different collimator extensions that were used in these measurements are shown in Figure 41 and Figure 42. These two figures are photographs of the collision chamber with the top removed. In each figure can be seen the beam collimator cone protruding into the left side of the chamber and diametrically opposite is the entrance to the beam detector.
Figure 41. Plan View of the Field-Free Collision Region.
Figure 42. Plan View of Collision Region with Repeller Electrode Installed.
The only difference in the two figures is the attachment on the spectrometer collimator. The simple cylindrical extension in Figure 41 is a rhodium plated aperture (0.025 x 0.040 inch tall) that was used for the field measurements of the angular distribution of the recoiling ions. The more complicated attachment on the collimator in Figure 42 is the repeller electrode which is shown in greater detail in Figure 43. This electrode was used for the measurement of the cross sections for the production of He\(^+\) ions and, separately, of He\(^{++}\) ions regardless of their original directions of recoil.

The actual electrode to which the repeller potential was applied was a thin (0.010 inch) sheet of phosphor bronze that was shaped to wrap around three sides of the beam path. It was attached with insulating spacers to the grounded aperture extension which was fitted into the end of the cone.

The second aperture of the collimator was in the first electrode of the spectrometer, which was located in a recess in the base of the cone. It was anticipated that a greater angular resolution than ± 0° 30', which was obtained with the present apertures, would be required in later experiments. Therefore, provisions were made to mount a separate and smaller aperture 1/16 inch in front of the present aperture.

The recess, in which the electrode structure was mounted, was machined concentric and parallel to the small end of the collimator cone that contained the entrance aperture button. Also located in this recess were four drilled and tapped holes and four accurately milled holes. Into the tapped holes were screwed four rods of about four-inch length on which the analyzer accelerating and focusing electrode structure was mounted.
Figure 43. Isometric Drawing of Repeller Electrode.
The electrodes were separated from each other and the mounting rods by a series of machined Supramica insulators. The alignment of these electrodes with the collimator axis was obtained by assembling the entire structure on four jig rods that were inserted into the milled holes in the collimator base. Once the structure was assembled and lock nuts had been placed on the mounting rods, then the jig rods were removed.

The basic focusing geometry of this electrode structure was designed from the information presented in Terman’s *Radio Engineer’s Handbook*. The entire electrode structure (shown in Figure 40) consists of six elements which serve to accelerate and focus the beam before it is passed into the spectrometer vacuum enclosure, which itself is at the full acceleration voltage. The first element was a thin (0.010 inch) rhodium plated disc that contained a 1/16 inch diameter aperture and was electrically grounded. It served as the second collimating aperture and to prevent the electric fields from the following acceleration electrodes from penetrating into the field-free region of the collimator.

The second element of the lens system was a rhodium-plated centering electrode. Its function was to center the beam in the electrode structure that followed (if by some chance the jig alignment was not adequate). This electrode consisted of two insulated halves that could be used individually to push or pull the beam from side to side, or both halves could be used together to retard the beam. The latter feature could be used to furnish information on the energy of the recoiling ions. Tests showed, however, that the jig alignment of the assembly was sufficient, and therefore the centering feature of this electrode was not employed. In fact, both sides were operated at ground potential to minimize the field penetration of the
following acceleration and focusing electrode into the region of the second collimator aperture.

The geometry of the following two electrodes was selected according to the information and evaluation of focusing characteristics presented by Terman, according to which this lens could be used to focus the beam at any location between the last electrode and the end of the spectrometer. The third element, which comprised the first half of the focusing lens, was 0.25 inch in diameter and 0.35 inch long, and the second half of the lens (the fourth electrode) was 0.45 inch in diameter and also of 0.35 inch length. The latter electrode established the terminal acceleration of the lens system, which was typically one to two kilovolts.

The next element (fifth electrode) was similar in design to electrode number two and provided a convenient means of deflecting the beam after it had been accelerated and focused.

The primary function of the sixth electrode was to serve as the entrance aperture to the magnetic analyzer geometry, i.e., this electrode was located at the focal point of the magnet and, therefore, its aperture served as an object of the focusing magnetic field. The size of this aperture, which was one of the primary determinants of the spectrometer resolution, was 0.10 inch in diameter. This value was selected because it was slightly larger than the diameter of the unfocused beam at that location and yet it was smaller than the width of the spectrometer exit slit (to be discussed). Thus, it served as an acceptable upper limit on the beam diameter as it entered the magnetic analyzer.

The last electrode also marks the beginning of the electric field-free region of the magnetic selector of momentum/charge. To serve this
function, it must, because of protruding points at ground potential in the rest of the assembly, have a "shroud" on the back side of the electrode.

The beam diverging from a focus at the final slit of the electrode assembly passed through a Nier-type 60° sector magnetic field, which re-focused it on the 1/8 inch wide exit slit of the spectrometer. The magnetic focusing, however, was only in the plane of Figure 40; there was no focusing in the vertical plane. In order to allow for the lack of vertical focus, the spectrometer collimator and the hole through which the beam passed in route to the exit slit were so designed that the beam would not strike any surface before the exit slit, even if there were no focusing.

In Figure 40 is shown a 1/4 inch baffle that precedes the exit slit. The purpose of this baffle was to reduce the transmission, through the exit slit to the detector, of detuned beam components that were reflected from the walls.

The 60° deflection geometry had a five-centimeter radius of curvature in the magnetic field. A current of 1.1 amperes was required in the magnet coil to supply the 1.8 kilogauss field necessary to analyze a one kilovolt He⁺ ion.

A rather low resolving power, about ten, was used in this experiment because the interest in the present work was not in high resolution, but rather in the attainment of flat-topped peaks as the analyzed ion beam was swept across the exit slit. This mode of operation required the use of a rather wide exit slit and a corresponding sacrifice of resolution. The resolving power of ten was, however, more than adequate for the present work. As will be demonstrated later, the focusing ability of this instrument is sufficient to produce a resolving power of 50 if the 1/8 inch
exit slit were replaced with a 1/32 inch slit, and the resolving power could be approximately doubled, to 100, by using a smaller (1/32 inch) slit in the end of the collimating cone.

In order to minimize the fringe field in the vicinity of the "field-free" regions of the collision chamber and the spectrometer collimator, a 3/8 inch thick mild steel plate was mounted about 5/8 inch from the pole face of the magnet. With this shield, the fringe field (normal to the ion path) with 1.8 kilogauss in the magnet gap, was less than one gauss in the collision chamber and less than two gauss in the collimator. Although the magnet would supply a field greater than eight kilogauss, later tests on the recoil energy of the ions demonstrated that large fields were unnecessary and, therefore, only small fields were used in order to minimize the fringing into the collision chamber.

With the full accelerating potential on the spectrometer vacuum housing, it was necessary to insulate it from all the grounded components that were connected to it. The magnet was insulated by two 1/64 inch sheets of Teflon which were inserted in the gap between the magnet and spectrometer housing.

The grounded collimator cone was insulated from the spectrometer housing by means of two accurately ground alumina spacers, which are shown as wide black lines in Figure 40. One spacer was used to align the collimator axis parallel to the axis of the spectrometer, and the other was used to assure that these two axes were the same.

A two-inch cold-trapped mercury diffusion pump was used to evacuate the spectrometer, from which it was insulated by a thin (1/16 inch) Nylon washer. With this pumping arrangement (shown in Figure 40) the spec-
trometer pressure was maintained at less than $8 \times 10^{-7}$ Torr (as measured on a Veeco RG-75K ionization gauge) even when the collision chamber was filled to the working pressure with target gas. In order to increase the pumping speed to the region behind the first aperture of the collimator, all of the electrodes that were solid discs were perforated by six 5/8 inch diameter holes, and the two deflection electrodes had four somewhat larger holes drilled in them. A calculation, based on the conductances of the collimator and electrodes, indicated that a pressure drop of about 100 could be expected between the collision chamber and small end of the cone.

As an extra precaution, to decrease the penetration of the acceleration fields through these pumping holes into the field-free collimator, a very thin grid (rhodium plated) was spot-welded across the holes. This grid was 97 percent transparent and the wire was about 0.002 inch in diameter. Therefore, the grid was expected to serve as a good equipotential surface and to have a negligible pumping impedance. Such a grid was also used to cover the pumping port on the side of the spectrometer; it was intended to prevent the grounded elbow to the pump from disturbing the field inside the spectrometer.

**The Ion Detector**

Mounted on the end of the spectrometer and spaced about one inch from the exit slit was a 14 stage copper-beryllium electron-multiplier detector (DuMont SPM-03-314).

This multiplier permitted the detection of individual ions that passed through the spectrometer. In Figure 40 it is seen that an ion entering the multiplier strikes the first of a series of 14 curved metallic
(CuBe) surfaces; these are referred to as dynodes. When the ion strikes the first dynode, secondary electrons are ejected; they are swept by an electric field to the next dynode where the process of secondary emission is repeated. Thus the electrons multiply in number as they are swept down the series of dynodes by successively higher positive voltage. The current gain of the present tube was estimated to be greater than $10^6$ electrons/ion.

In this experiment, it was desirable to detect the analyzed ions with an efficiency of around 99 percent. The achievement of such a high efficiency required that about 99 percent of all incident ions eject at least one secondary electron from the first dynode. It was explained by Deitz$^{58}$ that the expected frequency distribution for producing $n$, $n = 0, 1, 2, \ldots$, secondary electrons is given by the Poisson distribution $(\gamma^n/n!) \exp (-\gamma)$, where $\gamma$ is the average secondary emission coefficient. In the same paper, he verified that this was a good approximation to the actual situation. Therefore, according to the above distribution, it is necessary that $\gamma = 5$ in order that 99 percent of all the ions eject at least one secondary electron. The relation between the mass and energy of an ion to the secondary emission coefficient for typical multiplier surfaces has been demonstrated by Akishin,$^{59}$ and according to the figures he presented, an ion energy considerably greater than ten keV is required to attain $\gamma = 5$ for the light helium ions. Therefore, to achieve these ion energies, a high postanalysis voltage was employed to accelerate the ions into the detector. However, this entire acceleration voltage was not wanted across the multiplier because the secondary emission coefficient by electrons, which determined the gain of the detector, peaked around 300 to 400 electron volts; consequently, a potential difference greater than
about 400 volts per dynode, which implies an overall detector voltage of about 6500 volts, would produce a decrease in detector gain. Therefore, the circuit which is shown in Figure 44 was arranged to drop a variable fraction of the postanalysis acceleration voltage across the detector.

As is indicated in Figure 44, the postanalysis acceleration potential into the first dynode was supplied directly from the high voltage source. The ten henry coil and the 0.005 μF capacitor were installed to filter out high frequency switching transients from the rectifiers in the supply. Normally about a five kilovolt drop was maintained across the multiplier resistor string, which established a 350 volt interdynode potential. The remainder of the accelerating voltage was dropped across the lower variable resistor string, which, of course, was comprised of high voltage and high power resistors. Because of the limit on the voltage and power ratings in commercially available resistors, it was necessary to choose these values such that only a few tenths of a milliamp passed through the resistor string.

The two paralleled capacitors (500 pF and one μF) were installed for the purpose of bypassing the noise at the end of the dynode string to ground, rather than permit it to be coupled into the signal circuit. The 500 pF capacitor was used because it was suggested that it had better high frequency qualities than the large capacitor.

When the electron avalanche initiated by the incoming ion reaches the anode of the tube, a current pulse is passed through the 100 kΩ load resistor, which develops the voltage pulse that is passed by the isolation capacitor into the preamplifier. Following the preamplifier, the signal was passed through an amplifier (Oak Ridge National Laboratory, Model ALD)
Figure 44. Wiring Diagram of Particle Multiplier.
and into a scaler (Systron-Donner 1034) in which the individual pulses were recorded.
CHAPTER VII

EXPERIMENTAL PROCEDURES FOR THE MEASUREMENT
OF PARTIAL IONIZATION CROSS SECTIONS

Evaluation Tests of Apparatus

Prior to the measurements of cross sections the performance of the new apparatus was evaluated. In order to facilitate this procedure, the repeller electrode was used in the collision chamber to provide a substantial ion current through the spectrometer.

The projectile-target combination of protons incident on helium was selected because of its simplicity, i.e., the only two likely charge states of the target are He$^+$ and He$^{++}$.

To begin this series of tests, the proton beam was passed through the helium gas and into the detector, then the spectrometer was adjusted to produce a maximum count rate in the multiplier circuit.

Test 1. Determination of the optimum gain of the multiplier. This was accomplished by using the high voltage power supply to establish a ten kilovolt acceleration into the first dynode. The lower resistor string (Figure 44) was used to vary the voltage drop across the multiplier from about two to seven kilovolts. In this fashion, the response curve of Figure 45 was obtained. It should be noticed that the counting rate appeared to saturate above about five kilovolts, i.e., about 350 volts per dynode. Therefore, in this experiment a multiplier voltage of around 5.5 kilovolts was chosen.
Figure 45. Response of Ion Count Rate of Multiplier to Interdynode Voltages.
Test 2. Evaluation of the response of the multiplier count rate to the ion accelerating voltage. It was of particular interest to demonstrate that the ion counting efficiency was near 100 percent. For the reasons discussed in Chapter V, it was believed that when the ion acceleration potential reached a sufficiently high value to produce an average secondary yield of five or more electrons per incident ion, then the detection efficiency would be approximately 100 percent. It was also desirable to demonstrate that under the above conditions the signal pulses were clearly separated in amplitude from noise pulses.

The above two conditions are related and were tested in the following manner. For a series of increasing values of the acceleration voltage into the multiplier, pulse height spectra were obtained through the use of the pulse height discriminator on the amplifier. It was found that the noise was usually negligible compared to the signal, even when the lowest discriminator settings were used. Unfortunately the low discriminator settings necessary to include the smallest signal pulses (those pulses corresponding to $\gamma = 1$ on the first dynode) were unreliable and some scatter was obtained in the data. However, it was found (even with that discriminator setting) that as the acceleration voltage was increased, the count rate also increased up to a point and thereafter remained constant as the voltage was further increased. This saturation in count rate was interpreted to indicate that all of the real signal pulses were above that discriminator setting and therefore equal and near 100 percent detection efficiency was obtained at the acceleration voltages for which the count rate saturated. In this manner, Figure 46 was obtained for both helium ions. It should be noticed that, although the acceleration poten-
Figure 46. Response of Multiplier Ion Count Rate to Ion Acceleration Voltage.
tial at which the He$^{++}$ saturated was 12 kV, its energy was 24 keV, and therefore greater than the 14 keV energy for which He$^+$ saturated. The saturation curves were not extended beyond 22 kV at this time because at that point the noise was observed to being a rapid increase. The curves of Figure 8 were taken before the large one μF capacitor was added in parallel to 500 pF bypass capacitor shown in Figure 44. The later addition of the large capacitor served to reduce the noise at 20 kV by a factor greater than 50, which permitted the extension of the saturation plateaux up to about 25 kV for He$^+$ and about 21 kV for He$^{++}$. However, at 25 kV the noise again became comparatively large ($\frac{\text{sig}}{\text{noise}} \approx 8$) and, indeed, great care was required in providing adequate insulation between the various circuit elements in order to even reach the total 30 kV acceleration potential without electrical discharges. For the preceding reasons, a postanalysis acceleration voltage of around 16 to 18 kV was selected for the helium ions in this investigation.

Test 3. The purpose of this test was to determine the optimum acceleration and focusing voltages of the spectrometer. This test was performed separately with the repeller electrode and with the rhodium plated aperture for field-free measurements in the collision chamber.

Without a repeller field it was found that optimum focusing and transmission occurred for about 800 volts acceleration, i.e., the profile of the count rate, as the beam was magnetically swept across the 1/8 inch exit slit of the spectrometer, was flat topped. For this condition, the potential on the focus electrode was about 150 volts. It was found that flat-topped peaks were maintained for spectrometer potentials up to and including 1700 volts; such a profile is shown in Figure 47 for 1100 volts.
Figure 47. Profile of Count Rate as Beam Was Swept Across the Spectrometer Exit Slit.
acceleration.

When the repeller field was applied, which gave the ions substantial energies, the focusing conditions were different. It was found that optimum focusing was obtained for a ratio of repeller potential $V_r$ to spectrometer potential $V_a$ such that

$$\frac{V_r}{V_a} \leq \frac{1}{3}$$

A count rate profile is shown in Figure 47 for this case also. It should be noted that the flat top is somewhat narrower than that of the zero repeller potential case. This is believed to be due to the increased difficulty in focusing energetic ions.

Test 4. When the repeller electrode was used, it was necessary to know at what voltage it should be operated to insure equal collection efficiencies for all ions. Figure 48 shows the relation between the ion count rate to the repeller potential for both helium ions with all the previously discussed parameters properly tuned. The occurrence of saturation in count rate versus repeller field was interpreted to indicate that the repeller field was sufficiently strong to cause both He$^+$ and He$^{++}$ ions to very nearly follow the lines of electric force to the collimator aperture. Therefore, the only requirement to assure equal collection efficiencies for these ions was a sufficiently large collection field, which was apparently satisfied above about 300 volts on the repeller; a value of 350 volts was selected for this work, which dictated a spectrometer potential of 1000 to 1400 volts.
Figure 48. Response of Ion Count Rate of Multiplier to Repeller Voltage.
Test 5. This test was to determine the pressure range over which thin-target conditions existed. The quantity plotted on the ordinate of Figure 49 is proportional to the measured cross section for production of these two helium ions. Therefore, from the figure it is seen that the measured cross sections are constant as the target gas pressure (indicated by an ionization gauge) is increased up to a value of about $2 \times 10^{-4}$ Torr.

Test 6. It was necessary to determine whether or not a significant fraction of the two helium ions, which were formed by the beam collisions with the target gas, underwent secondary charge changing collisions in the gas before they entered the evacuated collimator. Of particular concern was the resonance charge exchange process \( \text{He}^+ + \text{He} \rightarrow \text{He} + \text{He}^+ \), which could completely destroy the $\text{He}^+$ recoil angular distribution, and it is expected to be the largest charge changing process operative at these ion energies of around 200 eV (impacted by the repeller electrode). In addition, it was necessary to determine the effect of the pressure in the collimator on the ion abundances.

The test designed to detect the resonance process was based on the following reasoning. The $\text{He}^+$ ions that are formed in the gas receive an acceleration to the collimator aperture by the repeller field. The energy that the ion had acquired when it arrived at the collimator was proportional to the distance through which it traveled in the repeller field. If there were no charge changing collisions experienced by the ion in traveling from the point of creation in the beam to the collimator, then the average ion energy would correspond to the acceleration potential at the beam axis. The energy spread about this value would correspond to the spatial width of the beam in the repeller field, and it should be approxi-
Figure 49. Limiting Pressure for Thin-Target Conditions.
mately symmetric. When a low acceleration potential is used in the spectrometer, the profile of the ion peak (count rate) at the exit slit should be directly related to the energy spread of the ions emerging from the collision chamber.

If resonance charge exchange did play an important part, however, some of the original He$^+$ ions would be neutralized at some point between the beam and the collimator, and the newly created He$^+$ ion would be accelerated on to the collimator. These new ions would be different in at least two respects from the original ions. First, they would not have the angular distribution characteristic of the high energy beam collision, and second, their energy acquired from the repeller field would be less because of the shorter distance through which they were accelerated.

As was previously mentioned, the importance of resonance charge exchange in this experiment is that it destroys the angular distribution of the recoil ions; however, the test for the presence of this effect was based on the energy difference of the ions. Specifically, evidence for this effect would be found in the energy profile of the ion peak at the exit of the spectrometer. If the peak were skewed to low ion energies as the target gas pressure was increased, then the presence of resonance charge exchange would be considered affirmed.

As the test was performed and the pressure was varied over the range from about $5 \times 10^{-6}$ to $5 \times 10^{-4}$ Torr, no evidence was found for the secondary charge changing collisions in the collision chamber.

The same type of test was employed to detect charge changing collisions in the collimator. If, for example, the He$^+$ were neutralized in the
collimator, it would not reach the detector, of if it were converted to He$^{++}$, its energy would be about one-half that of the He$^{++}$ ions which originated in the collision chamber. The neutralization of He$^{+}$ would manifest itself in a reduction of peak height, and the change of He$^{+}$ to He$^{++}$ would cause the ion peak to be skewed.

The indicated test was performed by varying the pressure in the spectrometer (and therefore the collimator) by about a factor of 20 with no noticeable effect on the ion peaks.

The conclusions from this series of tests are as follows:

1. a constant and equal fraction of the two helium ions formed in the target gas are repelled into the spectrometer by $V_r \geq 300$ volts, and $V_a$ adjusted to satisfy the condition that $1/4 \leq \frac{V_r}{V_a} \leq 1/3$;

2. maximum detector gain is obtained for about 350 volts interdynode potential;

3. constant and near 100 percent detection efficiencies are obtained for both ions for postanalysis acceleration (acceleration into the detector) in excess of about 15 kilovolts, and

4. no significant effect from charge changing collisions in either the collision chamber or the collimator is present in this experiment in the collision chamber pressure range $5 \times 10^{-6}$ to $5 \times 10^{-4}$ Torr.

Procedures for Relative Cross Section Measurements

Prior to any measurements, the collision chamber and spectrometer were evacuated to about $5 \times 10^{-7}$ Torr. When this was attained, the Vac-Ion pump was turned off and its magnet was removed. Normally the chamber pressure would equilibrate around $1.5 \times 10^{-6}$ Torr with only the two mer-
cury diffusion pumps operating.

The H\(^+\) beam would then be directed into the chamber and the beam detector. The current was measured directly on a Keithley (Model 410) pico-ammeter, the output of which was used to drive a Dymec (DY-2210) voltage-to-frequency converter, which in turn produced pulses at a rate proportional to the signal on the recorder output of the pico-ammeter. These pulses were counted on a 100 KC scaler. (Checks were made to assure that the output of the V-to-F converter was not sensitive to the high frequency modulations of the Van de Graaff beam.)

Next, the target gas was admitted to the chamber and the pressure was set at 1 \(\times\) 10\(^{-4}\) Torr, as indicated on the ionization gauge. It was noted, in contrast to the total apparent cross section experiment, that in this work the operation of the ionization gauge did not affect the measurements. This was due to the gauge being mounted on one of the horizontal arms of the "cross" on the top of the chamber. In such a mounting configuration, it would be difficult for ions from the gauge to reach the collision region.

When the repeller field was used, its potential was normally set by means of batteries after the target gas was admitted into the chamber.

The next step was to tune the spectrometer and detector. The spectrometer voltage was furnished and adjusted to about 1000 volts by means of a Hamner (Model N-413, 0-5kV) high voltage and highly regulated supply. The magnet current was obtained from a Harrison (Model 6263A) 10 amp, 18 volt current supply. The postanalysis acceleration potential was adjusted to about 18 kV by means of a Sorensen (Model 5030-4) 30 kV supply. The interdynode potential was set at approximately 350 volts.
When the magnetic field was used to scan the charge-to-mass spectrum, it was found that the only observable peaks were at \( q/m = 1/4 \) (He\(^+\)), and \( 1/2 \) (He\(^{++}\)). However, early in the testing stages of the apparatus, small peaks were observed that corresponded to heavier ions such as H\(_2\)O\(^+\) and N\(_2\)\(^+\), but these diminished as the collision chamber vacuum improved.

With the preceding arrangement, the output pulses from the multiplier were passed through the preamplifier and amplifier and into the 100 mc scaler.

The procedure described thus far applies to both collection with and without the repeller field.

When the field-free collision arrangement was employed, the spectrometer was rotated about the collision region. It was expected that the more energetic recoil ions would have a rather distinct angular dependence. However, as the spectrometer was rotated from about 92° to within less than 70° of the beam direction, no angular dependence was observed—the ion count rate remained constant. It was then observed that the count rate slowly decreased with time. A series of tests indicated that this difficulty was associated with surface charging problems which were affecting the ion transmission. An attempt to clean the rhodium surfaces of the beam and spectrometer collimators with emery paper and acetone produced no noticeable effect.

It was suggested, on the belief that low energy electrons would be attracted to and neutralize any positively charged surface in the collision region, that this difficulty might be remedied by operating a filament in the chamber. Although this did not prove to be the case, some important information on the ion energies was obtained from that test.
The test was the following. A filament was suspended near the top of the collision chamber (about two inches from the collision region). When it was operated at about two microamperes emission, the ion count rate in the spectrometer decreased by a factor of about 100. This was believed to be due to recoil ions being attracted to the negative potential which was produced by the electron space charge around the filament. Next, a self-biasing resistor was installed in the filament circuit such that an emission of two microamperes raised the dc filament potential to about plus two volts. This procedure would also raise the potential of the space charge region. It was observed that in this arrangement the ion counting rate of the spectrometer did not change, which indicated that the space charge potential was not now sufficient to influence the ions.

The surprising conclusion drawn from this test is that virtually all of the ions created from the helium target by the proton beam had energies less than about two electron volts (perhaps considerably less). With ions of such low energy, the angular distribution could be substantially distorted by surface potentials in the millivolt range, but even so, it might have been supposed that some sort of distorted angular distribution would be observed. However, Everhart\textsuperscript{60} recently pointed out that the effects of the thermal motion of the target atoms are sufficient to substantially broaden even a rather sharp angular distribution. Adapting the results of his analysis to the present energy range and collision pairs, indicates that the half-width of the peak (due to thermal motion alone) would be 10\textdegree~to 20\textdegree~or more for recoil angles around 90\textdegree. Therefore, from the observation in this investigation that the helium ion energies are very low (\(\ll 2\text{ eV}\)) and from Everhart's analysis, it is not
surprising that no angular distribution was observed.

The conclusion, based on the preceding observations, is that a detectable angular distribution will be obtained in the total energy spectrum of a given ion only for those collision partners for which there is substantial energy transfer (at least several electron volts).

The Rutherford scattering expression indicates that the energy transfer to the target is proportional to the square of the product of the atomic numbers of the collision partners. Therefore, in order to produce an appreciable energy transfer, a heavy projectile-target combination should be used.* With this last observation, the search for an angular distribution for the recoil ions was discontinued for the H⁺ on He projectile-target combination.

The results of the preceding tests demonstrated that satisfactory results could be obtained with the repeller field for this particular collision combination. It should be noted that this conclusion is not valid for every projectile-target combination. In fact, the attempts at field-free measurements were necessary in order to prove that a collection field could be efficiently employed for the total ion collection. With this conclusion, therefore, the repeller electrode was installed and used to obtain the cross sections for production by protons of He⁺ and He⁺⁺ ions, irrespective of their recoil angles.

With the apparatus tuned as previously described, the spectrometer was set at an angle near 90° with respect to the beam direction. The ion  

*In confirmation of this conclusion, a very pronounced angular distribution has been obtained in this apparatus, at the time of this writing, by other investigators who used the relatively heavy neon on argon projectile-target combination.
count rate was measured as the spectrometer and the attached repeller electrode were rotated several degrees about this position. As expected for these low energy ions, there was no noticeable change in count rate over this angular range, and the spectrometer returned to the 90° position for the remainder of the measurements.

A check was made to assure that the counting rates of the electronics were linear over the wide range employed in this experiment. It was found that the AID amplifier became nonlinear for a random pulse rate exceeding \(2 \times 10^4\) counts per second.

The He\(^+\) peak was first tuned in the spectrometer and both this count rate and the count rate produced by the V-to-F converter, which was proportional to the beam current, were accumulated simultaneously over several ten-second intervals, as set on the scaler-timers.

This procedure was repeated at each incident beam energy throughout the range of the experiment. It should be noted that the tuning of the spectrometer was not altered in an energy scan. This was done to more accurately determine the energy dependence of the cross sections. After one complete sweep of the energy range, the He\(^{++}\) peak was tuned and the measurement procedure was repeated.

At the conclusion of the above, the collision chamber was evacuated and the background contribution to the He\(^+\) and He\(^{++}\) peaks was evaluated. It was found that the background contribution to the He\(^+\) peak was about 0.02 percent and the contribution to the He\(^{++}\) was about 40 percent. This large contribution to the He\(^{++}\) peak was about thirty times the normal background noise level (including that of the He\(^+\) peak). From the measurements with the chamber filled with target gas, it was observed that
the \( \text{He}^+ \) ions were about one hundred times more abundant than those of the \( \text{He}^{++} \). On this basis, it was concluded that the 40 percent background contribution to the \( \text{He}^{++} \) peak was not \( \text{He}^{++} \), but some other ion with a \( q/m = 1/2 \), such as \( \text{H}_2^+ \). It was concluded that a very probable source of such an ion was the \( \text{H}^+ \) beam itself. It had been observed that when the beam was directed into the collision chamber, the indicated background pressure had a sustained increase of almost \( 1 \times 10^{-6} \) Torr. This was believed to be due to the evolvement of deposited hydrogen from the detector, under beam impact conditions.

The He target gas pressure employed was about \( 1 \times 10^{-4} \) Torr (uncorrected ionization gauge reading) and the observed \( \text{He}^{++} \), as was mentioned was about a hundred times less intense than \( \text{He}^+ \). Therefore, if the \( \text{H}_2 \) gas liberated from the beam detector had an ionization cross section comparable to that of helium (which it does), then the presence and magnitude of the \( \text{H}_2^+ \) background peak is explained. The \( \text{H}^+ \) peak was not observed because it was about a factor of 50 less intense than that of \( \text{H}_2^+ \) and, therefore, was not distinguishable from the noise. However, in the measurement procedure, the \( \text{H}_2^+ \) peak was observed to determine its stability and energy dependence, then its contribution at each energy was subtracted from the \( \text{He}^{++} \) peak. In the above manner, the relative cross sections for the production of \( \text{He}^+ \) and \( \text{He}^{++} \) were evaluated throughout the energy range from 0.15 to 1.00 MeV. That is, the present experimental results determined both the energy dependencies

\[ 10\sigma_{j1} (\text{He}^+) \propto f_+(E) \]  

(26)
and

\[ 10 \sigma_{j2} (\text{He}^{++}) \propto f_{++}(E) \]  

(27)

of the individual cross sections, as well as

\[ \frac{10 \sigma_{j1} (\text{He}^+)}{10 \sigma_{j2} (\text{He}^{++})} = k(E) \]  

(28)

where \( k(E) \) is a function of the beam energy.

**Calculation of the Absolute Cross Sections**

In order to determine the above cross sections absolutely, it is only necessary to determine either \( 10 \sigma_{j1} (\text{He}^+) \) or \( 10 \sigma_{j2} (\text{He}^{++}) \) absolutely at one energy.

This procedure can be accomplished through use of a relation discussed in Chapter II. Namely, that the total apparent ionization cross section \( \sigma_1 \) is the weighted sum of the individual cross sections, e.g.,

\[ \sigma_1 = 10 \sigma_{j1} (\text{He}^+) + 2 \times 10 \sigma_{j2} (\text{He}^{++}) \]  

(29)

Substitution of Equation 28 into Equation 29 yields

\[ 10 \sigma_{j2} (\text{He}^{++}) = \frac{\sigma_1}{2 + k(E)} \]  

(30)

The one value chosen for \( \sigma_1 \), from which the absolute values of \( 10 \sigma_{j1} (\text{He}^+) \) and \( 10 \sigma_{j2} (\text{He}^{++}) \) may be determined at any energy, is that mea-
sured in this laboratory at an energy of 1.00 MeV by Hooper. This energy was chosen because the charge exchange cross section is negligible, and the total apparent ion production cross section $\sigma_+$ measured by Hooper should be simply the total apparent ionization cross section $\sigma_i$.

The normalization procedure for obtaining the absolute cross sections was performed and the results are presented in Chapter VIII.
CHAPTER VIII

EXPERIMENTAL RESULTS FOR PARTIAL IONIZATION CROSS SECTIONS

Present Results and Comparison with Other Experimental Data

The absolute cross sections for the production of He$^+$ and He$^{++}$ ions by H$^+$ and electrons are shown in Table 6 and Figure 50. The solid triangles represent the present results over the proton energy range from 0.15 to 1.00 MeV. One point which was previously discussed should now be reemphasized and that is that only one energy point (1 MeV) was used to normalize the relative cross sections in order to obtain these absolute values. Both the absolute separation and slopes of these two cross sections are characteristic of the present data only and in no way reflect the normalization procedure.

The present data give an excellent fit to a straight line on a log-log plot throughout the energy range investigated. The data, therefore, correspond to an expression of the form

$$\sigma = A E^{-c}$$

(31)

where $E$ represents the proton energy. These two cross sections can then be represented as

$$10^6 \sigma_j (\text{He}^+) = 2.07 E^{-0.75} \times 10^{-17} \text{ cm}^2/\text{atom}$$

(32)
Table 6. Cross Sections for Production of He\(^+\) and He\(^{++}\) Ions in Helium Gas by Incident Protons

<table>
<thead>
<tr>
<th>Proton Energy (keV)</th>
<th>Measured Relative Cross Section (\frac{10^{-12}}{10^{-14}})</th>
<th>Calculated Absolute Cross Sections ((10^{-18}) cm(^2)/atom)</th>
</tr>
</thead>
<tbody>
<tr>
<td>150</td>
<td>90.7</td>
<td>88.0 0.970</td>
</tr>
<tr>
<td>200</td>
<td>106</td>
<td>71.8 0.678</td>
</tr>
<tr>
<td>300</td>
<td>143</td>
<td>51.0 0.356</td>
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<tr>
<td>400</td>
<td>177</td>
<td>42.9 0.242</td>
</tr>
<tr>
<td>500</td>
<td>199</td>
<td>35.0 0.176</td>
</tr>
<tr>
<td>600</td>
<td>215</td>
<td>31.4 0.146</td>
</tr>
<tr>
<td>700</td>
<td>239</td>
<td>27.3 0.114</td>
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</tr>
<tr>
<td>900</td>
<td>274</td>
<td>22.7 0.0828</td>
</tr>
<tr>
<td>1000</td>
<td>283</td>
<td>20.7 0.0732</td>
</tr>
</tbody>
</table>
Figure 50. Partial Cross Sections for Production of He$^+$ and He$^{++}$ Ions by Incident Protons. Key to the Results of Other Investigators: S.I.O.F.(62), Solov'ev, et al., (Reference 8); W.(64, 66), Wexler (Reference 9); G. & R.(64), Golden, et al., (Reference 62); H.(56), Harrison, (Reference 63).
Shown for comparison with the present results are the proton data of Solov'ev, et al. below 180 keV and that of Wexler above 0.80 MeV. It is seen that excellent agreement is obtained with the overlapping measurements below 180 keV; in fact, the data are essentially the same. For comparison with the data above 0.80 MeV, it should be noted that Wexler also measured only relative cross sections and normalized these to the same $\sigma_1$ measurements of Hooper that were used in the present experiment. One can regard this as normalization of only the $\sigma_{\text{lo},l}^j$ (He$^+$) cross section, because at 1 MeV energy the $\sigma_{\text{lo},l}^j$ (He$^{++}$) is only 0.35 percent of the $\sigma_{\text{lo},l}^j$ (He$^+$) cross section. Therefore, the present He$^+$ measurements and those of Wexler are in forced agreement at the 1 MeV energy point. Consequently, the only comparison to be made between the two measurements of the $\sigma_{\text{lo},l}^j$ (He$^+$) cross section is in the energy dependence, which Wexler observed to be slightly steeper (about $E^{-0.82}$) than the present value of $E^{-0.75}$.

The comparison between the present results for He$^{++}$ and those of Wexler does not reflect the normalization procedure, and their absolute agreement is significant. Here also the energy dependencies are slightly different: Wexler's results demonstrate an $E^{-1.2}$ dependence as compared with the present value of $E^{-1.4}$.

One very significant point should be made regarding the experimental apparatuses used by Solov'ev and Wexler. Both of these investigators used electrometers to measure their ion currents and certainly there was
no ion discrimination involved, in possible contrast to the electron multiplier detector employed in the present experiment. Even though tests had indicated that the electron multiplier was also being operated without ion discrimination, it was very gratifying to receive apparent verification of this fact in the form of excellent agreement on the measured cross section values among these several laboratories.

Also shown for comparison purposes are the cross sections for production of these two helium ions by electrons that are of the same velocity as the protons. If one recalls the discussion of the Bethe-Born approximation of Chapter V, it was pointed out that so far as simple ionization events by point charge projectiles were concerned, the cross section depended only on the charge and velocity of the projectile. Therefore, the simple ionization cross sections should be equal for equivelocity protons and electrons. It is seen in Figure 50 that this prediction is fulfilled for $^{10}\sigma_{11} (\text{He}^+)$ at proton energies above about 1 MeV. However, for the more violent collisions that produce $\text{He}^{++}$, there is a substantial difference in the electron and proton cross sections even for the highest energies shown. This discrepancy is believed significant because there is considerable agreement (± 5 percent) on these electron cross sections by other investigators, and those that disagree are usually higher and, consequently, in worse agreement with the proton results.

A recent literature search failed to reveal any quantum mechanical calculations pertaining to collisions of this nature, and a "classical" Gryzinski-type calculation produced results in poor agreement with the present results, both in absolute magnitude and energy dependence. Speci-
fically, the calculated proton cross sections at 1 MeV are more than a factor of two greater than the experimental values, and the two results are diverging with increasing energy in this range.

At the conclusion of the preceding experiment, the Van de Graaff accelerator was not scheduled to be used for two days. Consequently, this time period was used to make some preliminary measurements on the partial cross sections for the production of argon ions by impact with fast electrons. The cross sections for the first six argon ions were measured. However, only the cross sections for the first four ions were considered reliable (± 50 percent), simply because insufficient time was available to thoroughly test and tune the apparatus for this ion species.

The argon results are presented in Table 7 and Figure 51. The same type of comparison cross sections as in the previous figure are shown with the argon results. The data of Solov'ev, et al. are presented for energies up to 180 keV and those of Wexler for energies above 0.80 MeV.

It should be noted that the results of both these investigators agree rather well with the present results with the exception of $^{10}\sigma_{j3}$ $(Ar^{3+})$ by Solov'ev. It is seen that this cross section is about a factor of eight greater than the value predicted by extrapolating Wexler's $^{10}\sigma_{j3}$ $(Ar^{3+})$ curve to this energy and about a factor of ten less than the value indicated by the present measurements. The extent of this disagreement is clearly outside of the ± 15 percent error of Solov'ev and the ± 20 percent quoted by Wexler.

Also shown for comparison are the cross sections for production of these argon ions by equivelocity electrons. These electron results are in substantially better agreement with the proton cross sections in argon than
Table 7. Preliminary Cross Sections for Production of Ar^{n+}, n = 1, 2, 3, and 4 in Argon Gas by Incident Protons

<table>
<thead>
<tr>
<th>Proton Energy (keV)</th>
<th>Absolute Cross Sections $(10^{-17} \text{ cm}^2/\text{atom})$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$10^\sigma_{j1}$</td>
</tr>
<tr>
<td>180</td>
<td>37</td>
</tr>
<tr>
<td>400</td>
<td>30</td>
</tr>
<tr>
<td>600</td>
<td>19</td>
</tr>
</tbody>
</table>
Figure 51. Partial Cross Sections for Production of $\text{Ar}^{n+}$ ($n = 1, 2, 3,$ and 4) by Incident Protons. Key to the Results of Other Investigators: S.I.O.F. (62), Solov'ev, et al., (Reference 8); W. (64), Wexler (Reference 9); B. (30), Bleakney (Reference 69) - Normalized to G. & R. (64), Golden, et al., (Reference 62).
they were in helium. Perhaps this indicates that the Born approximation is satisfied at a lower energy for heavy targets, such as argon, than for the light helium targets.

Discussion of Errors

In this experiment the assignment of error limits is simplified because only relative cross sections were measured. The only significant source of error is in the relative collection and detection efficiencies of the two helium ions, and it was the purpose of the series of tests in the beginning of the previous chapter to assure that these efficiencies were equal. Because most of the possible sources of systematic relative errors lie in the evaluation of these tests, the final assignment of error limits is necessarily somewhat subjective.

It is the judgment of the author that the maximum error in the relative magnitudes of these two helium cross sections is not more than ±10 percent, and the error is probably not more than ±4 percent.

In order to assign error limits to the absolute cross sections, it is necessary to include the ±6 percent (probable) error in the $\sigma_i$ measurement of Hooper used for normalization. It should be noted that no consideration was given to the Gaede effect (Appendix III) in the error assigned to $\sigma_i$, and for helium this is believed to cause a zero to +3 percent error. Thus, it is estimated that the probable error in the absolute cross sections for production of He$^+$ and He$^{++}$ is less than +13 to -10 percent, most of which is due to the normalization procedure.
Conclusions

The experimental results of this investigation demonstrated that the helium ions produced in helium gas, by the passage of a beam of protons in the energy range from 0.15 - 1.00 MeV, were of energies considerably less than two electron volts. The effects of thermal motion of the target molecules and the very small stray fields in the collision region were sufficient to cause the angular distribution of the low energy recoil ions to appear to be isotropic. It was concluded that these low energy helium ions were collected with equal efficiencies by the repeller field.

The results of the evaluation tests and cross section measurements indicated that the electron multiplier was operated without ion discrimination and with nearly 100 percent detection efficiency.

The results for the cross sections for production of the two helium ions by protons were in excellent agreement with those of other investigators. However, the comparison cross sections for He⁺⁺ production by electron impact, scaled according to the Born approximation, failed to produce agreement with the proton results within the combined experimental errors. The extent of this disagreement suggests a deficiency in the application of the Born approximation to the case of double ionization of helium by protons and electrons. Although there are serious discrepancies among the results for the production of variously charged argon ions by fast protons, it appears that the scaled electron cross sections are generally in better agreement than was observed for the case of the helium target.
APPENDICES
APPENDIX I

DETERMINATION OF THE NEUTRAL BEAM INTENSITY

The neutral beam detector, described in Chapter IV, is an assembly which totally traps the beam and has three functions, i.e., provisions to make the following three observations: (1) net current of the beam $I_i$; (2) secondary emission current from the beam target foil $I_i'$; (3) total power of the beam $P$, through observation of the temperature rise of the target foil by means of a thermocouple.

The calibration scheme depends on calibration of the beam power $P$ in terms of the net current $I_i$, using a single charged ion beam, whose intensity is directly measurable absolutely by function (1), and applying this calibration to the neutral beam. The secondary emission current $I_i'$ can then be calibrated for the neutral beam in terms of the beam power $P$, so that either $I_i'$ or $P$ can be used for measurement of the neutral beam intensity, as is convenient.

The only critical assumption is that the beams of neutral and charged particles deposit equal amounts of energy in the target foil. This assumption was verified by the direct measurements of Mahadevan, in which he found, for heavier projectiles such as Ne at energies above about 2 keV, that ions and atoms deposited equal amounts of energy into the metallic surface. Evidence was also presented that the equality of energy deposition was reached at lower energies for lighter projectiles. Therefore, the assumption that essentially the full power of both the
ionic and atomic beams is deposited thermally in the foil, for the energy range under investigation, is clearly justified. To further substantiate this assumption, it has been shown for the \( \text{H}^+ \) and \( \text{He}^+ \) ion beams that the thermocouple emf is directly proportional to the beam power, independent of the beam energy, throughout the range of beam energy and intensity utilized in this experiment. Figure 52 shows the relationship of the thermocouple emf to beam power in the case of the \( \text{He}^+ \) projectile at two different energies.

Because of the beam fluctuations, it was essential that the calibration of any one function in terms of another be accomplished by simultaneous observations of both functions. With the physical arrangements employed, it was possible to observe \( I_i \) and \( I_i' \) simultaneously and to observe \( I_i' \) and \( P \) simultaneously, but unfortunately it was not possible to observe \( I_i \) and \( P \) simultaneously. A simultaneous observation of \( I_i \) and \( P \) would have required that the nano-voltmeter be "floated" off ground as part of the input circuit of the electrometer which measured the total net current. This arrangement was unsuitable because the resultant pickup, stray currents, and capacitance thus introduced into the electrometer input circuit rendered its readings quite meaningless. Similarly, a switching arrangement to switch rapidly from one connection scheme to another, so as to eliminate an intermediate calibration step in terms of the secondary emission current \( I_i' \), proved to be unworkable for essentially the same reasons. Therefore, a slightly more indirect procedure than that indicated above was required. The detector was first connected to observe \( I_i \) and \( I_i' \), and \( I_i' \) was calibrated in terms of \( I_i \) for the ion beam at a given energy. The connections were then changed to observe \( I_i' \) and \( P \), and \( P \) was calibrated in terms of
Figure 52. Response of the Thermocouple of the Neutral Particle Detector to the Impinging Beam.
I′, again using the same ion beam. This procedure was repeated at several energies throughout the energy range, to verify that, even though the calibration of I′ was energy dependent, that of P was not. (The calibration of I′ was also time dependent as the surface condition of the foil changed, but it was verified that the calibration of P was stable within about ten percent over periods of many weeks operation. However, the calibration of P was performed daily.) The established calibration of P was then assumed applicable to the neutral beam, as previously explained.

On the rather rare occasions when it was desired to use the secondary emission function for measurement of the neutral beam, its calibration was checked several times per day and separately at each value of the beam energy against the established calibration of the beam power. Note that no assumptions are made about the relative calibration of I′ for ions vs. atoms, or about the energy dependence of the calibration.

Figure 53a is a block diagram of the electrical connections for the simultaneous observation of I and I′, using two Keithley (Model 410) electrometers.

The reading of electrometer number 1 was the secondary emission current I′ and that of electrometer number 2 was the net beam current plus the secondary emission current, I + I′. I and I′ were always of the same order of magnitude. For H+ beams, I was about half I′, and for He+ beams, I was about one-quarter I′. Therefore, I′ was never a small difference between two nearly equal readings. In this manner, I′ was calibrated in terms of I as

\[ I′ = \gamma I \]  

(34)
Figure 53. Schematic Diagram of Electrical Connections Employed in the Calibration of the Neutral Beam Detector.
where $\gamma$, the constant of proportionality, is the effective secondary emission coefficient for the singly charged ion beam on this copper foil at this given energy.

Figure 53b is a diagram of the electrical connections for simultaneous observation of $I'_1$ and $P$, using electrometer number 1 and a Keithley (Model 149) nano-voltmeter for observation of the thermocouple emf. These observations yield the relation between the secondary emission current, which will be designated as $I'_1$ (because it may be different in magnitude from the former $I'_1$) and the emf $\epsilon_1$ at a single energy value,

$$I'_1 \propto \epsilon_1$$  \hspace{1cm} (35)

which in itself is not very useful. Figure 52 demonstrated that the emf $\epsilon_1$ was proportional to the beam power, which is a product of the beam current and the accelerator voltage $I_1V$. Therefore, to derive some useful information from this set of observations, they should all be combined to produce a relationship between the beam power and the emf. This objective can be accomplished by use of Equation 34 and the accelerator voltage to relate Equation 35 to the total beam power $I_1V$ as

$$V \left( \frac{I'_1}{\gamma} \right) \propto \epsilon_1$$  \hspace{1cm} (36)

which is valid for all energies and currents used in this experiment. It should be noted that the $I'_1$ contained in the expression for $\gamma$ cannot be
cancelled with the $I_i^\prime$, because even though they represent the same type of current, they were measured at different times and may, therefore, be unequal in magnitude.

A more useful form of Equation 36 for the measurement of the neutral beam is

$$\frac{E_iI_i^\prime}{e\gamma} \propto \epsilon_i$$

in which $E_i$ is the energy of the singly charged ion beam and $e$ is the charge of an electron.

Finally, to determine the "particle current" of the neutral beam (the number of atoms per second $N_a$ striking the foil target) it was only necessary to make two measurements and to use Equation 37. The measured quantities were the emf $\epsilon_a$ generated in the thermocouple by the atomic beam, and the energy $E_a$ of the atomic beam. With this information, one can write

$$\frac{N_aE_a}{\epsilon_a} = \frac{\epsilon_a}{\epsilon_i}$$

and

$$N_a = \frac{\epsilon_a}{E_a} \left[ \frac{E_iI_i^\prime}{\epsilon_i e} \right] \text{ const.}$$

Thus $N_a$ (atoms/sec) is expressed in terms of measurable quantities and the electron charge $e$. This expression was written in terms of the energy $E_i$. 
and charge $e$ rather than simply the accelerator voltage $V$ because, when substituted into the cross section expressions, the charge $e$ cancels. The bracketed term is a constant in Equation 39 and, like the $I_1$ in Equation 36, the energies $E$ should not be cancelled. As such, Equation 39 is valid over the entire energy range of this experiment, even though the calibration was performed at only one energy $E_1$. 
APPENDIX II

DETERMINATION OF APPARENT CROSS SECTIONS
FROM EXPERIMENTAL OBSERVABLES

In this section expressions for the apparent cross sections $\sigma_{-}$ and $\sigma_{+}$, the total cross section for the production of negative and positive charges, respectively, will be developed in terms of experimental observables.

Consider a parallel, monoenergetic beam of $N_p$ projectiles per second to be directed through a chamber filled with the target gas of density $m$. The number of free electrons per second $N_-$ produced along a length $L$ of the beam path by the passage of the beam may be expressed as

$$N_- = m L N_p \sigma_-$$

(40)

where $\sigma_-$ is the effective cross sectional area of the target molecule for the production of electrons. Specifically, $\sigma_-$ is the cross section for production of one electron plus twice the cross section for production of two electrons plus three times the cross section for production of three electrons, etc. Thus $\sigma_-$ is referred to as the apparent cross section for electron production. It is assumed that the number density $m$ is sufficiently low such that no target molecule is shielded by another, and that no projectile undergoes more than one collision.
The application by means of parallel plate electrodes of a sufficiently strong transverse electric field to this collision region will result in the collection of all the free electrons on one electrode and all of the slow positive ions on the other. This collection of $N_e$ electrons per second produced a current

$$I_e = eN_e$$  \hspace{1cm} (41)$$

where $e$ is the charge of an electron.

Simultaneously, the ionizing beam was collected and measured. In this part of the experiment the projectiles used were He$^{++}$, He$^0$, and H$^0$. For the charged projectile, He$^{++}$, the measurement consisted of stopping the beam in a deep Faraday cup which produced a current $I_p$, where

$$I_p = 2eN_p$$  \hspace{1cm} (42)$$

For the atomic projectiles He$^0$ and H$^0$, the "neutral current"

$$I_n = eN_p$$  \hspace{1cm} (43)$$

was determined as described in Equation 39 of Appendix I.

Thus we have expressions that permit the evaluation of $N_p$ for both ionic and atomic beams. These are Equations 42 and 43, respectively. Substitution of Equations 41 and 42 into 40 yields
In order to obtain the corresponding equation for the atomic beams, substitute Equation 41 and 43 into 40. One obtains

\[
[\sigma^-]_{He^{++}} = \frac{2}{mL} \frac{I}{I_p} \tag{44}
\]

A similar analysis applied to the measurement of the slow positive ions leads to the following results:

for He\(^{++}\) projectiles

\[
[\sigma^+]_{He^{++}} = \frac{2}{mL} \frac{I}{I_p} \tag{46}
\]

and

for He\(^o\), H\(^o\) projectiles

\[
[\sigma^+]_{He^o, H^o} = \frac{1}{mL} \frac{I}{I_n} \tag{47}
\]

Thus the apparent cross sections for production of electrons \(\sigma^-\) and positive ions \(\sigma^+\) are presented in terms of measurable quantities. The composition of these cross sections is investigated in detail in Chapter II.
APPENDIX III

THE USE OF A McLEOD MANOMETER TO MEASURE
GAS PRESSURES BETWEEN $10^{-2}$ AND $10^{-5}$ TORR

Introduction

The classical instrument that has stood, since its invention in 1874, as the absolute standard of pressure measurement for gas pressure in the range from 1 to $10^{-6}$ Torr, is the McLeod manometer.

The accuracy of this instrument was almost unchallenged until a few years ago when investigations uncovered several systematic errors associated with its customary mode of operation. To date, it appears that the evaluation of these errors is still unsure. This is evidenced by the fact that the National Bureau of Standards has not been willing for some time to calibrate any vacuum gauges below about one Torr. However, even with the knowledge of the existence of these errors, it was felt, at the beginning of this work, that the McLeod gauge was still the best calibration standard available, although at present it seems that more investigators are turning to the recently developed capacitance manometer for an absolute pressure standard. However, since the McLeod gauge was used as the primary standard of the present work, the following discussion will be limited to this instrument. The operating principle, the major associated errors, the gauge preparation, and the actual method of operation will be described.
Operating Principle of the McLeod Gauge

Basically this is an instrument that isolates a rather large volume of gas at the pressure to be measured and compresses it through a large and known volume ratio by means of a rising column of mercury that acts as a piston. As the gas is compressed, it exerts a downward force on the mercury column. At a suitable compression, the height of this mercury column is compared with that of a like column which has not compressed any gas. This offset in mercury columns along with the compression ratio yields the desired pressure.

In this investigation, a Model GM-110 McLeod gauge manufactured by Consolidated Vacuum Corporation was used as the primary standard. This gauge was originally equipped with 0.535 mm diameter capillaries by the manufacturer. As will be discussed later under the heading "Systematic Errors," these capillaries were found to be unsatisfactory and were replaced by 1.00 mm diameter capillaries.

In order to obtain the "McLeod gauge equation," one may start with the assumption that Boyle's law will apply to this situation. Thus

\[ P_i V_i = P_f V_f \]  \hspace{1cm} (48)

where \( P_i \) and \( V_i \) are the pressure of the gas and volume of the gauge, respectively, before the gas is compressed. \( P_f \) and \( V_f \) denote those same quantities after the compression. The quantity of interest is, of course, \( P_i \), the initial gas pressure.

\( V_i \) for this gauge is 2185 cm\(^3\)
\[ V_f = \frac{\pi d^2}{4} H \]

where \( d = 1.00 \text{ mm} \) is the compression capillary diameter and \( H \) is shown on Figure 54; \( V_f = \Delta h \) is also shown in Figure 54. With this information then, Equation 48 becomes the "McLeod gauge equation"

\[ p = \frac{\pi d^2}{4} \frac{H\Delta h}{V_f} \]

\[ = 3.906 \times 10^{-7} H\Delta h \]

for this gauge. Here, \( p \) is in Torr when \( H \) and \( \Delta h \) are expressed in mm. For future reference, this pressure will be denoted simply as \( P \).

The conventional method of operating the McLeod gauge is to run the mercury up in the capillaries until \( H = \Delta h \), this simplifies the reading procedure. However, as will be discussed later under the heading of "Systematic Errors," a more reliable determination of pressure is usually possible when a series of different compressions of the sample gas is made. This is accomplished by raising the mercury in the capillaries to several different heights and measuring \( H \) and \( \Delta h \) at each position. A position in the vicinity of \( \Delta h = H \) is usually included in these measurements. This procedure is referred to here as the "multiple - compression - mode" of operating a McLeod gauge.

**Systematic Errors**

The chief systematic errors inherent in even a well constructed
Figure 54. McLeod Gauge.
McLeod gauge are the result of:

1. Departures from Boyle's law;
2. nonuniform capillary depression; and
3. the presence of a cold trap in the tabulation between the manometer and the system whose pressure is to be measured.

Each of these effects will now be examined with the purpose in mind of either eliminating or correcting for them.

1. Departures from Boyle's Law

The McLeod gauge equation presumes that the gas obeys Boyle's law; the behavior of a real gas at low pressure is more closely approximated by Van der Waal's equation, which takes account of the finite size of the molecules and certain of the forces between them. The relative error introduced by assuming that the gas obeys Boyle's law has been computed by Jansen and Venema.\(^7\) They found this error for all the gases used in this work to be less than 0.1 percent for pressures up to 400 Torr in the compression capillary. In the present research, the pressure in the closed capillary did not exceed about 50 Torr; therefore, this error may be neglected.

There is a further reason that use of Boyle's law may not accurately describe the gas sample in the manometer. During the pressure measurement cycle, this gas may be partially adsorbed and desorbed on the walls of the gauge.

An especially alarming consideration is the following. If a monolayer of gas adsorbed on the spherical bulb of a McLeod gauge, one liter in volume should rapidly desorb, the pressure in the gauge would increase by \(10^{-2}\) Torr. Therefore, for less than one percent error at \(10^{-4}\) Torr,
the number of molecules adsorbed must be stable to $10^{-4}$ of a monolayer. Thus this sorption effect appears to be a potential source of a large error.

Kreisman has performed three separate tests in an attempt to detect this sorption effect. The following description of these tests was taken from his own report.

Another possible source ... [of error] ... is temporary adsorption of the gas during its compression into the fine-bore, closed-end capillary. However, tests made with gases having different adsorption properties showed no noticeable effects.

A direct experimental search for adsorption effects in the McLeod gauges is made in the following way: with a fixed amount of gas in the closed McLeod gauge system, a measurement is made with both gauges simultaneously and the pressures recorded. Next, the top of the closed capillary of one of the gauges is cooled with dry ice or liquid nitrogen. If there are gas molecules adsorbed on the capillary wall, cooling the wall will decrease their tendency to desorb. When the mercury is removed from the gauges, a lower system pressure should be obtained due to the molecules remaining on the capillary wall. If the gas pressure is again measured with the uncooled gauge, the lower pressure should be evident. The experiment was carried out with the lower pressure gauge being cooled and showed no indication of the adsorption.

Adsorption of gas by the walls of the McLeod gauge compression bulb can be measured in the following way: After a pressure measurement has been made with the gauge, the gas compressed into the top of the closed-end capillary is trapped there by freezing some of the mercury in the capillary. The remainder of the mercury is lowered to a point just above the bulb cutoff level. Any gas adsorbed by the compression bulb walls should desorb at the lower pressure obtained. If the mercury is now raised in the bulb, any desorbed gas will be trapped between the rising mercury and that frozen in the capillary tube. The volume and pressure of the desorbed gas can be measured and the amount of desorbed gas can be determined. This experiment, carried out with nitrogen under conditions that were not ideal, indicated that the amount of nitrogen desorbed by the large compression bulb of the low pressure McLeod gauge was less than one percent of the total gas originally admitted to the gauge.

The somewhat surprising conclusion from Kreisman's work is that these sorption effects are not important in a "clean" high vacuum McLeod
It appears then that we are justified in using the ideal gas law to derive the McLeod gauge equation, given here as Equation 49.

2. Nonuniform Capillary Depression

Of the three chief sources of error previously listed, it is the capillary depression error that the investigator is most likely to notice. In fact, in the beginning of the present experiment this was the cause of some very obvious and intolerable errors.

Capillary depression is caused by the forces of interaction between the mercury and glass wall of the capillary. The normal mercury depression as calculated for clean glass capillaries of 1.0 mm diameter is 11 mm. This is quite appreciable compared to the mercury depression produced by the compressed gas in the closed capillary, which is about 22 mm for a typical initial pressure of $2 \times 10^{-4}$ Torr. It is reasonable to expect that additional interaction of the mercury with the forces due to local impurities on the glass capillaries might radically alter the normal capillary depression and, because this is such a large portion of the total depression, it would result in a substantial error in the pressure determination.

The test employed in this work to detect nonuniform capillary depression is as follows. The gauge was evacuated to about $5 \times 10^{-7}$ Torr and the mercury was raised in the capillaries and the 8.0 mm diameter side arm. At this low pressure $\Delta h$ should be essentially zero except in the last three or four centimeters of compression. This left more than 15 cm of capillary over which the mercury in both capillaries should be the same height. In this region then the mercury was raised in intervals of
a centimeter or less and was allowed to rest at each position until the level ceased to change, which usually required several minutes. At each position the level of the mercury in both capillaries and the side arm was measured. In this test a Gaertner (M 911) cathetometer was used to measure the menisci positions. The smallest reading on its vernier was 0.05 mm. It could be expected that the mercury in the relatively large side arm would be the least sensitive to wall effects. For this reason, it was used as the reference against which the mercury levels of two capillaries were plotted to show the depression of the menisci levels in the capillaries as a function of mercury position.

With the 0.535 mm diameter capillaries with which the gauge was originally equipped, the levels in both capillaries varied rather badly, and furthermore, the interesting quantity \( \Delta h \) varied from +10 mm to -1 mm with the sign of the slope changing several times. This test was repeated four or five times and in each the procedure was varied, but always with similar results. These variations in operating procedures will be discussed later.

A decision was based on the above results to replace the 0.535 mm capillaries with 1.0 mm diameter capillaries. This was accomplished and the preceding test was repeated. This time the mercury in the two capillaries rose smoothly and there were no systematic variations. The mercury in the open capillary appeared to ride slightly lower than that of the closed capillary, about 0.1 to 0.2 mm. When the pressure to be measured is so low that this offset, \( \Delta h_d \), is appreciable compared to \( \Delta h \) or \( H \), then one must correct for it.

A test of the above type, however, may not be sufficient to evaluate
for operational pressure measurements. During the pressure measurement, the conditions above the mercury in the closed capillary are different from those in the open capillary, due to the radically different gas pressure.

A good way of evaluating $\Delta h_d$ during the pressure measurement is the following: a test sample of gas is compressed in the gauge, and $H$ and $\Delta h$ are recorded as usual. However, instead of the normal McLeod gauge equation

$$P = KH\Delta h$$

(49)

where $K = 3.906 \times 10^{-7}$

the depression error $\Delta h_d$ is inserted and the equation becomes

$$P = KH (\Delta h - \Delta h_d)$$

(50)

where $(\Delta h - \Delta h_d)$ is the true depression due to the pressure. Equation 50 may be rearranged to give

$$\Delta h = \frac{P}{K H} + \Delta h_d$$

(51)

Thus a plot of $\Delta h$ versus $1/H$ would give a straight line of slope $P/K$ and intercept on the $\Delta h$ axis of $\Delta h_d$. Of course, if $\Delta h_d$ is a function of $H$, then Equation 51 will not produce a straight line.

The test was performed on the modified gauge, with 1.00 mm diameter capillaries, and the graph of Equation 51 is presented as Figure 55.
PLOT OF $\Delta h = P/K (1/H) + \Delta h_d$

$P = 1.43 \times 10^{-4}$ Torr

Figure 55. Plot of Modified McLeod Gauge Equation for this Gauge.
Out of eleven positions of the mercury, each being carefully read one time, the maximum deviation of any point from the straight line was less than 1.3 percent. The line drawn through these points intersected Δh at
\[ \Delta h_d = -0.30 \pm 0.05 \text{ mm}. \]

The conclusion is that there is no appreciable dependence of \( \Delta h_d \) on \( H \), and that \( \Delta h_d \) is only important when

\[ \Delta h \leq 100 \Delta h_d \]  \hspace{1cm} (52)

or

\[ H \leq 100 \Delta h_d \]  \hspace{1cm} (53)

For this modified McLeod gauge, \( \Delta h_d \) causes less than one percent error for pressures above \( 3 \times 10^{-4} \) Torr. However, \( \Delta h_d \) might be an unstable quantity and must be frequently checked.

3. Errors Due to the Cold Trap

The third and sometimes largest source of systematic error arises from the use of a cold trap.

A cold trap is normally placed between the gauge and the system whenever it is desirable to prevent the flow of mercury into the system or to prevent condensable gases from entering the McLeod gauge. When this is done, two significant errors will be introduced. One is caused by thermal transpiration and the other by the Gaede effect.

**Thermal Transpiration.** Rusch and Bunge have dealt with this problem. This effect is caused by temperature differences between the various parts of the system and may result in pressure differences even between parts that have a common temperature.
At high pressures, when the mean free path of the gas molecules is small compared to the dimensions of the tube connecting the warm and cold regions, the pressure will be the same everywhere. This is because the gas-gas collisions predominate over the gas-wall collisions. For the other extreme of very low pressures, in which the mean free path is very long compared to the tube dimensions, the regions of common temperature will still have common pressure; however, the regions of different temperature will have different pressures, because the gas-wall collisions are now predominant.

Between these two extremes are cases in which there will be a pressure difference between the warm and cold places which depends on the dimensions of the connecting tubulation. The effect can be particularly serious with regard to a cold trap where there are large temperature gradients along relatively narrow tubes. Even if the portions of the system on both sides of the trap are at equal temperatures, there can be a net pressure difference if the conductances of the tubes from the cold region of the trap to the two warm regions on either side are unequal.

Rusch and Bunge have demonstrated that errors attributable to this effect can rise to ten percent. However, they were able to essentially eliminate these errors by proper dimensioning of the trap or by using a symmetric trap.

In the present experiment, the traps used were not made strictly in accordance with the suggested design of Rusch and Bunge. However, from information presented in their paper, it appears that our traps should produce considerably less than one percent error in the pressure range below $1 \times 10^{-3}$ Torr. Other considerations, during the time before
we were aware of the present effect, led to a trapping arrangement that used two asymmetrical traps "back-to-back," which, of course, produced a symmetrical trapping arrangement. Thus, despite the design of the individual traps, the final arrangement did comply strictly with the suggestions of Rusch and Bunge, and the errors produced by thermal transpiration should now be negligible.

Gaede Effect. The error produced in this case is due to mercury vapor streaming from the McLeod gauge reservoir through the connecting tubulation to the cold trap. The diffusing mercury molecules undergo collisions with, and impart momentum to, the molecules of the gas under measurement. This momentum has a component directed away from the manometer. Thus, this mercury and trap arrangement functions as a diffusion pump. The result is that the pressure of the gas to be measured would be lower in the McLeod gauge than it would be in the system supplying the gas. Hence, the measurement of pressure would be falsely low.

In his paper in which he described his invention of the mercury diffusion pump, in 1915, Gaede \[75\] presented an analysis of this effect, and even gave warning to the users of McLeod gauges that cold traps would cause errors. However, it appears from the lack of mention of this effect in subsequent literature until 1962\[76,77\] that his warning went unheeded. In recent years, similar treatments have been presented by several investigators. Principal among these were Ishii and Nakayama, \[76\] Meinke and Reich, \[77\] and Vries and Rol. \[78\] The only analysis that differed substantially from Gaede's was that based on kinetic theory by Takaishi. \[79\] The treatment presented here is not radically different from those mentioned above.
To describe this process mathematically, consider a stationary cloud of mercury vapor in a tube whose diameter is large compared to the mean free path of the molecules. Into one end of the tube a gas is introduced, whose pressure is much lower than that of the mercury. These gas molecules flow into the mercury by the process of ordinary diffusion. This diffusion can be described by the equation

\[ j = -D_{12} \frac{dn}{dx} \text{molecules cm}^2 \text{sec}^{-1} \]  

(54)

in which \( j \) is the flux of molecules into the mercury, \( D_{12} \) is the diffusion coefficient for the diffusion of gas against mercury, and \( \frac{dn}{dx} \) is the density gradient of the gas. When this diffusion takes place in the tubulation between the McLeod gauge and the cold trap, in which the mean free path is comparable to the tube dimensions, the process will be slowed by the finite impedance of the tube. Denote the inhibiting factor by \( f \) and write

\[ j = -f D_{12} \frac{dn}{dx} \]  

(55)

However, in practice the mercury vapor is not stationary but moves with a net velocity \( u \) from the gauge to the trap, which acts as a sink. If it were not for the diffusion just described, this flow of mercury would sweep \( nu \) gas molecules per cm\(^2\) per second back to the trap, in a tube of zero impedance. However, wall effects retard this process by a factor which, it is argued, is precisely the same inhibiting factor \( f \) appearing in Equation 55.
In the stationary state these two processes are equal in magnitude and one may write

\[ nuf = - f D_{12} \frac{dn}{dx} \]  \hspace{1cm} (56)

Thus, the inhibiting factor \( f \) cancels out in the final relation. Since the density, \( n \), is proportional to pressure, \( p \), this equation becomes

\[ \frac{dp}{p} = - \frac{u}{D_{12}} \, dx \]  \hspace{1cm} (57)

Integration over the length of tube, \( L \), from gauge to trap yields

\[ \ln \frac{p \ (\text{trap})}{p \ (\text{gauge})} = \frac{uL}{D_{12}} \]  \hspace{1cm} (58)

The velocity \( u \) of the mercury is related to the conductance \( C \) of the tubulation through

\[ u = \frac{C}{rr^2} \]  \hspace{1cm} (59)

in which \( r \) is the radius of the tube.

The following equation for \( C \), which is applicable in the molecular flow region, is given by Dushman. \(^{80}\)

\[ C = 3.048 \times 10^4 \frac{r^3 \sqrt{T}}{L \sqrt{M}} \]  \hspace{1cm} (60)
This expression is applicable to a cylindrical tube for which \( L > 100 \, r \).

When the tube length \( L \) and radius \( r \) are given in cm, then \( C \) has the units of \( \text{cm}^3/\text{sec} \). \( T \) is the temperature (°K) and \( M \) is the molecular weight of the gas.

However, in the operating temperature range of this laboratory (23° - 28°C), the vapor pressure of mercury is not sufficiently low to be clearly in the molecular flow region. Dushman\(^81\) gives a multiplicative correction factor, \( C'/C \), which is in the vicinity of 0.97 for this temperature range. Substituting Equations 59 and 60 and \( C'/C \) into Equation 58 yields

\[
\ln \frac{p_{\text{trap}}}{p_{\text{gauge}}} = 3.048 \times 10^4 \frac{r}{\pi D_{12}} \sqrt{\frac{T}{M}} \frac{C'}{C} \tag{61}
\]

In this experiment \( r = 0.4 \text{ cm} \) and for mercury \( M = 200 \). Since \( D_{12} \) is inversely proportional to pressure and there is an abundance of data at atmospheric pressure from which \( D_{12} \) can be evaluated, the quantity \( D_{12} (1 \text{ at}) \times \frac{760}{P_{\text{Hg}}} \) will be calculated. With this expression Equation 61 becomes

\[
\frac{p_{\text{trap}}}{p_{\text{gauge}}} = \exp \left[ 0.361 \frac{P_{\text{Hg}}}{D_{12} (1 \text{ at})} \sqrt{\frac{T(\text{°K})}{C}} \right] \frac{C'}{C} \tag{62}
\]

The diffusion coefficient \( D_{12} (1 \text{ at}) \) was calculated from the expression given by Dushman,\(^82\)

\[
D_{12} (1 \text{ at}) = \frac{4 \left( v_{\text{Hg}}^2 + v_g^2 \right)^{\frac{1}{2}}}{3\pi n (5 \text{Hg} + 5g)^2} \tag{63}
\]
for the case in which the mercury vapor pressure is large compared to the real gas pressure. The $g$ subscripts refer to the real gas whose pressure is to be determined, $v$ represents the average velocity of the molecules, $n$ the number density at one atmosphere and $\delta$ is the molecular diameter. All of the quantities with the exception of the $\delta$ are computed in an obvious manner, and for this reason these values, which were computed from viscosity measurements, are shown in Table 8.

Table 8. Molecular Diameters ($\delta$) (Units of $10^{-8}$ cm)

<table>
<thead>
<tr>
<th>Temp ($^\circ$C)</th>
<th>$\delta_{H_2}$</th>
<th>$\delta_{He}$</th>
<th>$\delta_{N_2}$</th>
<th>$\delta_{Ar}$</th>
<th>$\delta_{Hg}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>24</td>
<td>2.70</td>
<td>2.18</td>
<td>3.73</td>
<td>3.62</td>
<td>5.12</td>
</tr>
<tr>
<td>26</td>
<td>2.71</td>
<td>2.18</td>
<td>3.73</td>
<td>3.62</td>
<td>5.10</td>
</tr>
<tr>
<td>28</td>
<td>2.71</td>
<td>2.18</td>
<td>3.72</td>
<td>3.61</td>
<td>5.09</td>
</tr>
<tr>
<td>30</td>
<td>2.70</td>
<td>2.18</td>
<td>3.72</td>
<td>3.61</td>
<td>5.07</td>
</tr>
</tbody>
</table>

Equation 62 was evaluated for $H_2$, $He$, $N_2$, and $Ar$ in the temperature range from 22$^\circ$ to 28$^\circ$C. It was also evaluated for $Ne$, $CO$, and $O_2$ between 24$^\circ$ and 26$^\circ$C. These results are plotted in Figure 56, and these calculated errors due to the Gaede effect seem to be substantial. However, it should be noted that these errors are at their maximum values, because it was assumed in the derivation of Equation 62 that the pressure of the real gas was negligible compared to the mercury vapor pressure. In the present work using $He^{++}$ projectiles, this was a reasonable assumption because the real gas pressure was always less than a few percent of the mercury vapor pressure, which was about $2.5 \times 10^{-3}$ Torr. However, the low cross sections
Figure 56. Indicated McLeod Gauge Correction Factor for Gaede Effect.
for the neutral projectiles necessitated the use of higher gas pressures, sometimes as high as $1 \times 10^{-3}$ Torr. As the percentage of the real gas pressure rises the Gaede effect decreases, although not in direct proportion. Therefore, in the present experiment it seems that the error would be larger for He$^{++}$ projectiles than for H$^0$ and He$^0$. Existing experimental measurements $^{62,76-78,84-87}$ of this effect are not in close agreement, although they are usually within $+5$ and $-50$ percent of these calculated values. At present the reasons for these discrepancies are not obvious.

An investigation of this effect was undertaken in this laboratory by Thomas. $^{87}$ His procedure was to compare the pressure as indicated by a McLeod gauge, operated in the multiple-compression-mode, with that of a capacitance manometer. Although this McLeod gauge was not the same as the one used in the present experiment, the calculated Gaede effect was of the same order of magnitude. The pressure range investigated was from about $1 \times 10^{-4}$ to $5 \times 10^{-3}$ Torr. At the lower pressures, i.e., less than about $4 \times 10^{-4}$ Torr, he did observe that the pressures indicated on the two instruments sometimes differed. However, the difference was always in the wrong sense for it to be ascribed to the Gaede effect. Thomas attributed this to errors in the capacitance manometer for such low pressures. Above the pressure of $4 \times 10^{-4}$ Torr there appeared no evidence for the existence of the Gaede effect or systematic errors in either of the two manometers. However, as mentioned previously, in this pressure range above $4 \times 10^{-4}$ Torr, the assumption that the real gas pressure is negligible compared to that of the mercury vapor is no longer valid, and consequently the Gaede effect should be less than those values indicated
in Figure 56. Thomas has suggested that the reason he did not observe the Gaede effect is because his McLeod gauge was "dirty." That is, the gauge and mercury are old and perhaps contaminated with adsorbed gases and no recent attempt has been made to clean either. Specifically, the surface of the mercury from which the vaporization takes place was visibly dirty and hence the rate of evaporation would be inhibited. If one recalls, the working mechanism that produces this effect is the evaporation and condensation of the mercury from the reservoir and on the cold trap, respectively. It is therefore evident that the Gaede effect will be reduced in proportion to the reduction in the evaporation rate of the mercury.

The above suggestion is perhaps substantiated by the work of Utterback, who used what would be classified as a "clean" gauge. His technique was nominally the same as that of Thomas, and he did observe the effect. Furthermore, it appeared to be of about the expected magnitude.

However, Utterback's results are somewhat suspect because he did not observe the predicted pressure dependence, i.e., the effect he observed was a constant, independent of pressure, over the entire range investigated, which extended up to about $2.5 \times 10^{-3}$ Torr. It should be noted, however, that other investigators did observe the expected pressure dependence.

From the foregoing considerations it appears quite likely that the Gaede effect does exist and may produce substantial errors in the measurement of pressure. However, it is not felt that the magnitude of this effect has been sufficiently substantiated at this time to be used as a correction factor. Rather, it is felt that for the purpose of the present
investigation, the critical parameters such as temperature, tube dimensions, and indicated pressure should be recorded. If one wishes to consider the cleanliness of the gauge, perhaps it is even important to note that it was connected to the system by means of a greased stopcock. Such quantities as the gauge cleanliness would be extremely difficult to evaluate. However, the other quantities mentioned are explicitly accounted for in the theory.

The purpose in recording such parameters would be twofold. First, it would at most allow an absolute correction of the data if ever the magnitude of this effect is established; and second, at the least, it would allow some other investigator to make a more meaningful comparison to the present results. The latter would be accomplished by noting from these parameters in which gauge the effect is expected to be greatest, and relatively how much greater.

Preparation of the McLeod Gauge for Pressure Measurement

Upon receipt of this gauge from the manufacturer, it was rinsed in the following sequence with acetone, distilled water, concentrated nitric acid (approximately 30 seconds in the capillaries), and distilled water. After each rinsing the liquid was removed and deposited in a reservoir by evacuation. Following the final rinse with distilled water, the gauge was placed in its operating location and connected to the high vacuum system. When a vacuum of about $1 \times 10^{-6}$ Torr was attained, the gauge was heated to approximately 100°C for several hours by means of a hot air gun. At the completion of this procedure it was estimated that the gauge vacuum was about $1 \times 10^{-7}$ Torr. Next, the McLeod gauge was valved off from the
high vacuum system and the existing gauge vacuum was utilized to "draw" the triple-distilled mercury through a connecting tube and into the gauge reservoir.

Following the installation of the mercury, the gauge was returned to the system vacuum and heating was resumed for several hours. During this time the capillaries were maintained at a higher temperature ($\sim 75^\circ \text{C} - 100^\circ \text{C}$).

The purpose in this final heating was to remove residual gases such as water vapor and carbon dioxide from the gauge. A higher temperature bake would have been desirable; however, no facilities were available that would enable this to be done in a controlled manner.

Alpert observed, in heating a McLeod gauge to 400°C, that as many as 30 monolayers of water vapor and substantial quantities of N$_2$ and CO$_2$ are released from the glass surfaces.

Aside from the glass walls outgassing, Kriesman, in a very detailed study of the McLeod gauge, observed that the mercury itself outgassed. Several days under high vacuum conditions were required for the outgassing to cease. He then back-filled the gauge to several $\times 10^{-3}$ Torr with dry N$_2$ or Ar and sealed it off overnight. He concluded that the readings before and after this storage period indicated that under these conditions neither the mercury nor the glass adsorbed any significant amount of this dry N$_2$ or Ar.

**Operational Procedure**

In the present research, the pressure range of interest is between $5 \times 10^{-5}$ and $2 \times 10^{-3}$ Torr, and a description of the measurement proce-
dure follows. In order to minimize the amount of capillary surface exposed to gas, the mercury is left in the fully raised position when the gauge is not in use, after first evacuating to about $1 \times 10^{-7}$ Torr. Several minutes before the gauge is to be used, the traps are cooled to liquid nitrogen temperature so that all the condensable vapors will be removed from the connecting tube between the mercury surface in the side arm and the trap. The mercury is then lowered into the reservoir. The gas to be measured is slowly admitted into the vacuum system and thereby into the McLeod gauge. Several minutes are allowed for pressure equilibrium to be reached. Then, by admitting dry nitrogen into the reservoir, the mercury is allowed to rise. This must be done slowly so that the gas undergoing compression will remain in thermal equilibrium with the rest of the gauge. If the gas is allowed to heat, a falsely high pressure will be indicated. To insure that this did not occur, the mercury was allowed to rest several minutes before the reading was made.

Care should be taken to allow the mercury to approach its rest position only by rising. This insures that the rest position of the mercury meniscus is not affected by the electrostatic charge on the glass wall. This charge is produced by the friction between the mercury and glass if the mercury is allowed to overshoot and then must be lowered to the desired rest position.

Most investigators advocate tapping of the capillaries before the reading is taken. In the McLeod gauge used by Jansen and Venema it was demonstrated that tapping against the capillary tubes enables the mercury meniscus to reach the most stable position, corresponding to the average position of a large number of positions formed
during experiments without tapping.

The results clearly show that, although the average difference in height, $\Delta h$, is almost the same with and without tapping, the average error in one observation with tapping is much smaller than without.

This was not observed to be the case with the gauge used in this work. In fact, with tapping, a lower pressure was indicated than without tapping. This was attributed to the observation that the closed capillary was attached on one end only, and because of this it would have larger amplitudes of vibration than the comparison capillary. Moreover, sometimes the closed capillary would resonate and the mercury would rise above its equilibrium position. When this occurred, it would seldom completely recover because of the frictional forces previously described. Consequently, for readings with this gauge, the capillaries were not tapped.

After the mercury was allowed to remain in its rest position for several minutes, the menisci levels were read by means of a cathetometer. Following this, the mercury was allowed to compress the gas further and the levels were again read. This was repeated for three or four measurements. If the sequence of these measurements indicated a trend toward higher or lower pressure, they were plotted to determine the $\Delta h_d$ correction factor (refer to previous discussion under the subheading of nonuniform capillary depression).

When the gauge was operated in this fashion, the pressure from one sequence of measurements to the next was usually reproducible within one percent. Although after the gauge had been used for several days the individual data points, as shown in Figure 55, would begin to scatter three or four percent from the straight line, this was remedied by return-
ing the gauge to high vacuum and heating it with a hot air gun for an hour or two.

**Conclusions**

It was found that, if great care were taken and the operating procedure outlined in the preceding paragraphs was followed, then the random errors in this gauge could be reduced to less than one percent in the pressure range from $5 \times 10^{-5}$ to $2 \times 10^{-3}$ Torr.

In consideration of the systematic errors, it was concluded that the effect of thermal transpiration was negligible due to the symmetrical trapping arrangement. The other major systematic error, which is due to the Gaede effect, appears to be significant, if one judges from either the theoretical calculations or the experimental results. The poor agreement among the experimental results, however, has caused some investigators to doubt that this effect has been properly evaluated.

In the present investigation, it was felt that the calculated Gaede effect was based on well established quantities, such as conductances, diffusion coefficients, etc. and was probably very nearly correct in the assumed pressure range and for clean mercury. Evidence in support of this opinion exists in the form of data taken by Meinke and Reich who have paid close attention to satisfying all of these assumptions. It seems that one such confirmation of this effect should outweigh several less ambitious attempts that either measure less than the full predicted effect or no effect at all. In particular, it seems that once the full effect has been observed, then the investigators that measure a lesser effect are only demonstrating that their apparatus failed in some capa-
city to satisfy the assumptions of the calculation. Unfortunately, these convictions do not serve any useful purpose so far as correcting for this effect in the present McLeod gauge is concerned.

If one recalls the work of Thomas \(^{87}\) for a rather dirty gauge in which no Gaede effect was observed and contrasts it to the work of Meinke and Reich \(^{84}\) for a clean gauge, in which the full effect was observed, then one should realize the magnitude of the Gaede effect for the present moderately clean gauge could fall anywhere in between these two extremes. On this basis for the systematic error bracket on these pressure measurements, it seems only reasonable to choose the lower one to correspond to no Gaede effect and the upper one to correspond to the full effect as indicated by the curves of Figure 56.

Assigning the systematic errors in the above fashion and allowing a plus or minus one percent for random errors, then one has for the gases used in the present experiment the following total errors in pressure measurements:

<table>
<thead>
<tr>
<th>Gas</th>
<th>The indicated pressure is from</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\text{H}_2)</td>
<td>1 percent high to 3 percent low</td>
</tr>
<tr>
<td>(\text{He})</td>
<td>1 percent high to 4 percent low</td>
</tr>
<tr>
<td>(\text{N}_2)</td>
<td>1 percent high to 12 percent low</td>
</tr>
<tr>
<td>(\text{Ar})</td>
<td>1 percent high to 14 percent low</td>
</tr>
</tbody>
</table>

Rather than attempt to correct the measured cross sections for these pressure errors, they will simply be added to the other errors to determine the overall error limits of this experiment.
APPENDIX IV

ALIGNMENT OF ANGULAR ROTATION MECHANISM

Prior to the measurements of the angular distribution of the recoil ions, it was necessary to align the apparatus such that the spectrometer would rotate about a fixed point in the ion beam.

The tools employed for alignment purposes were an engineers transit, a three meter rod to which was taped a 15-inch scale divided into 1/100 inch increments, and a π tape.

The alignment procedure was the following.

1. The spindle axis was adjusted to be vertical. This adjustment was accomplished by utilizing the precision machined features of the apparatus. When the precision spindle seat was turned in the base tripod, a flat surface was also turned on the large diameter steel base plate on which the angle scale was to be mounted. Hence, if the machined surface on the base plate is leveled, then the spindle is vertical. Utilizing this feature, the three meter rod and machinist scale were positioned approximately vertical at several locations around the circumference of the base plate. At each location, the elevation was determined with the aid of the transit, and the indicated adjustments were made by the jack screws in the tripod legs. After such a series of successive leveling approximations, it was estimated that the spindle was aligned within one minute of angle from the vertical.

2. The top and bottom flanges of the collision chamber were re-
moved and a machined (conical) pointer was fitted into a precision 0.375 inch hole (on axis) in the top of the spindle. The tip of the pointer defined the position of intersection of the line of sight through the spectrometer collimator and the fast beam collimator.

3. The transit was set up about five feet from the collision chamber (far enough for good focus, yet close enough for good magnification), approximately on the beam axis. The transit telescope was leveled and focused on the tip of the pointer in the collision chamber. Next, the beam collimator was adjusted to coincide with the axis defined by the transit telescope and the pointer, and the adjustments were locked.

The following step, which was later employed for the determination of the angle between the fast beam and the spectrometer, was to tilt the telescope downwards so that its axis swept out the vertical plane defined by the spindle axis and the transit axis. When the cross-wires of the telescope were focused on the outer edge of the large diameter base plate (on which the angle scale was mounted), a mark was made at the intersection of the cross-wires.

4. The transit was moved, readjusted and sighted through the "straight-through" port on the spectrometer. The rotation angle of the spectrometer was not important as long as it was near 90°. The vertical and horizontal adjustments on the spectrometer support were used, along with the horizontal displacement adjustment on the transit, to align the spectrometer axis with the axis defined by the telescope and pointer.

Next, the telescope was tilted downwards as previously described, and a mark was made on the edge of the base plate.

5. The π tape was then placed around the circumference of the base
plate and the plate diameter was measured to within 0.01 percent.

6. The angle scale, which was etched on a machined strip of aluminum of accurately known radius, was then mounted at the prescribed radius on the base plate. This was accomplished by measuring radially inwards from the edge of the plate with a micrometer.

7. The final measurement was the determination of the linear distance between the two marks made on the edge of the base plate in steps 3 and 4. This distance together with the known diameter of the plate permitted the calculation of the angular separation of the beam collimator and the spectrometer collimator. The angle pointer (mounted on the end of the counter weight support) was then adjusted to the calculated angle on the angle scale.

Thus, the alignment procedure was completed. It was estimated, on the basis of the accuracy of the individual alignment steps, that each collimator was aligned with 0.002 inch of the rotation axis, and the angular determination was within 0° 02′ at 90°.
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*Abbreviations used herein conform to those found in the American Institute of Physics Style Manual (1965).


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VITA

Lawrence Jackson Puckett was born in Claxton, Georgia on September 28, 1938. He is the son of Mr. and Mrs. Osbourne Puckett. On June 25, 1960 he was married to Anne Wilson Dukes, from Columbia, South Carolina. A daughter, Anne Lynne, and a son, David Lawrence, were born on February 25, 1962, and April 16, 1963, respectively.

Mr. Puckett attended public schools in Augusta, Georgia, where he was graduated from the Academy of Richmond County in 1956. He received the degrees of Bachelor of Science in Physics from the Virginia Military Institute in 1960, and a Master of Science in Physics from the Georgia Institute of Technology in 1962.

During the summers of 1960 and 1962, he was employed as a physicist by E. I. DuPont de Nemours and Company at the Savannah River Plant. Since the fall of 1962, he has been employed as a graduate research assistant with the Engineering Experiment Station of the Georgia Institute of Technology.

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