A Decade of Cognitive Radio Technology

Abstract

Cognitive radio (CR) can successfully deal with the growing demand and scarcity of the wireless spectrum. To increase the spectrum usage, CR technology allows unlicensed users to access licensed spectrum bands. Since licensed users have priorities to use the bands, the unlicensed users need to continuously monitor the licensed users’ activities to avoid interference and collisions. How to obtain reliable results of the licensed users’ activities is the main task for spectrum sensing. Based on the sensing results, the unlicensed users should adapt their transmit powers and access strategies to protect the licensed communications. The requirement naturally presents challenges to the implementation of CR. In this report, we provide an overview of recent research achievements of CR by looking at the spectrum sensing and sharing techniques. The applications of CR are also discussed.

Index Terms

Cognitive radio, cooperative communications, spectrum sensing, spectrum sharing.

I. INTRODUCTION

Due to the rapid growth of wireless communications, more and more spectrum resources are needed. Within the current spectrum framework, most of the spectrum bands are exclusively allocated to specific licensed services. However, a lot of licensed bands, such as those for TV broadcasting, are underutilized, resulting in spectrum wastage [1]. This has promoted Federal Communications Commission (FCC) to open the licensed bands to unlicensed users through the use of cognitive radio (CR), which is a spectrum agile radio being able to adapt operating parameters to changing environments [2]–[6]. The IEEE 802.22 working group [7] has been formed to develop the air interference for opportunistic secondary access to TV bands.

In practice, the unlicensed users, also called secondary users (SUs), need to continuously monitor the activities of the licensed users, also called primary users (PUs), to find the spectrum holes (SHs), which is defined as the spectrum bands that can be used by the SUs without interfering with the PUs. This procedure is called spectrum sensing [8], [9]. There are two types of SHs, namely temporal and spatial SHs [8], respectively. A temporal SH appears when
there is no PU transmission during a certain time period and the SUs can use the spectrum for transmission. A spatial SH appears when the PU transmission is within an area and the SUs can use the spectrum outside that area.

To determine the presence or absence of the PU transmission, different spectrum sensing techniques have been used, such as matched filtering detection, energy detection, and feature detection [10]. However, the performance of spectrum sensing is limited by noise uncertainty, multipath fading, and shadowing, which are the fundamental characteristics of wireless channels. To address this problem, cooperative spectrum sensing (CSS) has been proposed [11] by allowing the collaboration of SUs to make decisions.

Based on the sensing results, the SUs have information about the channels that they can access. However, the channel conditions may change rapidly and the behavior of the PUs might change as well. To use the spectrum bands effectively after they are found available, spectrum sharing and allocation techniques are important [6], [12]. As PUs have priorities to use the spectrum when SUs co-exist with the PUs, the interference generated by the SU transmissions needs to be below a tolerable threshold of the PU system [13]. Thus, to manage the interference to the PU system and the mutual interference among SUs, the power control schemes should be carefully designed. By utilizing advanced technologies such as multiple-input multiple-output (MIMO) and beamforming with smart antenna, interference-free co-existing transmissions can be achieved [14]. In the multi-hop CR system, relays can assist SUs’ transmissions, which generate spatial SH and achieve more communication opportunities. Moreover, the resource competition among SUs needs to be addressed.

There are a lot of progresses on CR technology in the last ten years. This report provides an overview of some recent techniques, potential challenges, and future applications of CR. In Section II, fundamental spectrum sensing techniques are provided. In Section III, cooperative spectrum sensing techniques to boost the sensing performance are presented. Spectrum sharing and allocation schemes are discussed in Section IV. The applications of CR technology and conclusions are in Section V and Section VI, respectively.

Table I lists some abbreviations that have been or will be used in this report.
II. LOCAL SPECTRUM SENSING

Spectrum sensing enables SUs to identify the SHs, which is a critical element in CR design [8], [9], [15]. Fig. 1 shows the principle of spectrum sensing. In the figure, the PU transmitter is sending data to the PU receiver in a licensed spectrum band while a pair of SUs intends to access the spectrum. To protect the PU transmission, the SU transmitter needs to perform spectrum sensing to detect whether there is a PU receiver in the coverage of the SU transmitter.

Instead of detecting PU receiver directly, the SU transmitter can detect the presence or absence of PU transmitter signals easily. However, as shown in Fig. 1, the radius of PU transmitter and PU receiver detections are different, which lead to some shortcomings and challenges. It may happen that the PU receiver is outside the PU transmitter detection radius, where the SH may be missed. Since the PU receiver detection is difficult, most work focuses on PU transmitter detection [6], [12].

It is worth noting that, in general, it is difficult for the SUs to differentiate the PU transmitter signals from other pre-existing SU transmitter signals. Therefore, we treat them all as one received signal, $s(t)$. The received signal at the SU, $x(t)$, can be expressed as [16]

$$
x(t) = \begin{cases} 
n(t) & \mathcal{H}_0, \\
s(t) + n(t) & \mathcal{H}_1, 
\end{cases}
$$

(1)

where $n(t)$ is the additive white Gaussian noise (AWGN). $\mathcal{H}_0$ and $\mathcal{H}_1$ denote the hypotheses of the absence and presence of the PU transmitter signals, respectively. The objective for spectrum sensing is to decide between $\mathcal{H}_0$ and $\mathcal{H}_1$ based on the observation $x(t)$.

The detection performance is characterized by the probabilities of detection, $P_d$, and false-alarm, $P_f$. $P_d$ is the probability that the decision is $\mathcal{H}_1$ while $\mathcal{H}_1$ is true; $P_f$ denotes the probability that the decision is $\mathcal{H}_1$ while $\mathcal{H}_0$ is true. Based on $P_d$, the probability of miss-detection $P_m$ can be obtained by $P_m = 1 - P_d$.

A. Hypothesis Testing Criteria

There are two basic hypothesis testing criteria in spectrum sensing: the Neyman-Pearson (NP) and Bayes tests. The NP test aims at maximizing $P_d$ (or minimizing $P_m$) under the constraint of $P_f \leq \alpha$, where $\alpha$ is the maximum false alarm probability. The Bayes test minimizes the average cost given by $\mathcal{R} = \sum_{i=0}^{1} \sum_{j=0}^{1} C_{ij} \Pr(\mathcal{H}_i | \mathcal{H}_j) \Pr(\mathcal{H}_j)$, where $C_{ij}$ are the cost of declaring $\mathcal{H}_i$
when $\mathcal{H}_j$ is true, $\Pr(\mathcal{H}_i)$ is the prior probability of hypothesis $\mathcal{H}_i$ and $\Pr(\mathcal{H}_i|\mathcal{H}_j)$ is the probability of declaring $\mathcal{H}_i$ when $\mathcal{H}_j$ is true. Both of them are equivalent to the likelihood ratio test (LRT) [17] given by
\[
\Lambda(x) = \frac{P(x|\mathcal{H}_1)}{P(x|\mathcal{H}_0)} = \frac{P(x(1), x(2), \ldots, x(M)|\mathcal{H}_1)}{P(x(1), x(2), \ldots, x(M)|\mathcal{H}_0)} \overset{\mathcal{H}_1}{\gtrless} \gamma,
\]
where $\Lambda(x)$ is the likelihood ratio, $P(x(1), x(2), \ldots, x(M)|\mathcal{H}_i)$ is the distribution of observations $x = [x(1), x(2), \ldots, x(M)]$ under hypothesis $\mathcal{H}_i$, $i \in \{0, 1\}$, $M$ is the number of samples, and $\gamma$ is the detection threshold, which is determined by the maximum false alarm probability, $\alpha$, in NP test and $\gamma = \frac{\Pr(\mathcal{H}_0)(C_{10} - C_{00})}{\Pr(\mathcal{H}_1)(C_{01} - C_{11})}$ in the Bayes test.

In both tests, the distributions of $P(x|\mathcal{H}_i)$, $i \in \{0, 1\}$, are known. When there are unknown parameters in the probability density functions (PDFs), the test is called composite hypothesis testing. Generalized likelihood ratio test (GLRT) is one kind of the composite hypothesis test. In GLRT, the unknown parameters are determined by the maximum likelihood estimates (MLE) [18]–[20]. GLRT detectors have been proposed for multi-antenna system in [18] and for sensing OFDM signal in [19], [20] by taking some of the system parameters, such as channel gains, noise variance and PU transmitter signal variance as the unknown parameters.

Sequential testing is another type of hypothesis testing, which requires a variable number of samples to make decision. The sequential probability ratio test (SPRT) minimizes the sensing time subject to the detection performance constraints [21]. In SPRT, samples are taken sequentially and the test statistics are compared with two threshold $\gamma_0$ and $\gamma_1$ ($\gamma_0 < \gamma_1$), which are determined by the detection requirements. Using the SPRT, the SU makes decisions according to the following rule: $\mathcal{H}_1$ if $\Lambda(x) > \gamma_1$; $\mathcal{H}_0$ if $\Lambda(x) < \gamma_0$; more samples are needed if $\gamma_0 < \Lambda(x) < \gamma_1$.

General sequence detection algorithms for Markov sources in noise have been proposed in [22]. A weighted, soft-input sequence detection algorithm based on forward-backward procedure is shown to be optimal in minimizing the Bayesian risk when different Bayesian cost factors are assigned for missed detections and false alarms. Moreover, a new limitation called risk floor has been discovered for traditional physical layer sensing schemes, which is caused by finite channel dwell time, where longer observation windows are more likely to mix the PU’s behavior from multiple states, leading to degraded performance.
B. Local Spectrum Sensing Techniques

To identify the SHs and protect the PU transmission, different local spectrum sensing techniques have been proposed for individual SUs by applying the hypothesis testing criteria discussed above.

1) Matched filtering detector:
If the SUs know information about the PU transmitter signal, the optimal detection method is matched filtering [10], which correlates the known primary signal with the received signal to detect the presence of the PU transmitter signal and thus maximize the signal-to-noise ratio (SNR). The matched filtering detector requires short sensing time to achieve good detection performance. However, it needs knowledge of the PU transmitter signal that may not be known at the SUs. Thus, the matched filtering technique is at a disadvantage in general environment where SUs do not know what PU signals to expect.

2) Energy detector:
Energy detector [10] is the most common spectrum sensing method. The decision statistics of the energy detector are defined as the average energy of \( N \) observed samples

\[
Y = \frac{1}{M} \sum_{t=1}^{N} |x(t)|^2. \tag{3}
\]

The decision is made by comparing \( Y \) with a threshold, \( \gamma \). If \( Y \geq \gamma \), the SU makes a decision that the PU transmitter signal is present (\( H_1 \)); otherwise, it declares that the PU transmitter signal is absent (\( H_0 \)).

The energy detector is easy to implement and requires no prior information about the PU transmitter signal. However, the performance of the energy detector is subject to the uncertainty of noise power and the sensing time taken to meet the detection requirement may be high. More importantly, the energy detector cannot distinguish the PU transmitter signal from the noise and other interference signals, which may lead to a high false-alarm probability.

3) Feature detector:
Cyclostationary detector is one of the feature detectors that utilize the cyclostationary feature of the signals for spectrum sensing [23], [24]. It can be realized by analyzing the cyclic autocorrelation function (CAF) of the received signal \( x(t) \), expressed as

\[
R^\beta_x(\tau) = E[x(t)x^*(t-\tau)e^{-j2\pi\beta t}], \tag{4}
\]
where $E[\cdot]$ is the expectation operation, $*$ denotes complex conjugation, and $\beta$ is the cyclic frequency. CAF can also be represented by its Fourier series expansion, called the cyclic spectrum density (CSD) function [25], denoted as

$$S(f, \beta) = \sum_{\tau = -\infty}^{+\infty} R_x^\beta(\tau) e^{-j2\pi f \tau}. \quad (5)$$

The CSD function exhibits peaks when the cyclic frequency $\beta$ equals the fundamental frequencies of the transmitted signal. Under hypothesis $\mathcal{H}_0$, the CSD function does not have any peaks since the noise is, in general, non-cyclostationary.

Generally, feature detector can distinguish noise from the PU transmitter signals and can be used for detecting weak signals at very low SNR region, where the energy detection and matched filtering detection are not applicable. In [26], a spectral feature detector (SFD) has been proposed to detect low SNR television broadcasting signals. The basic strategy of the SFD is to correlate the periodogram of the received signal with the selected spectral features of a particular transmission scheme. The proposed SFD is asymptotically optimal according to the NP test, but with lower computational complexity.

4) Other techniques:

There are several other spectrum sensing techniques, such as eigenvalue-based and moment-based detectors.

Eigenvalue-based detector: In the multiple-antenna system, eigenvalue-based detection can be used for spectrum sensing [27], [28]. In [27], maximum-minimum eigenvalue (MME) and energy with minimum eigenvalue detectors have been proposed, which can simultaneously achieve both high probability of detection and low probability of false-alarm without requiring information of the PU transmitter signals and noise power. In most of the existing eigenvalue-based methods, the expression for the decision threshold and the probabilities of detection and false-alarm are calculated based on the asymptotical distributions of eigenvalues. To address this issue, the exact decision threshold for the probability of false-alarm for the MME detector with finite numbers of cooperative SUs and samples has been derived in [28], which leads to our next section on cooperative spectrum sensing (CSS).

Moment-based detector: When accurate noise variance and PU transmitter signal power are unknown, blind moment-based spectrum sensing algorithms can be applied [29]. Unknown parameters are first estimated by exploiting the constellation of the PU transmitter signal.
When the SU does not know the PU transmitter signal constellation, a robust approach that approximates a finite quadrature amplitude modulation (QAM) constellation by a continuous uniform distribution has been developed [29].

C. Sensing Scheduling

When and how to sense the channel are also crucial for spectrum sensing. Usually, short quiet periods are arranged inside frames to perform a coarse intra-frame sensing as a pre-stage for fine inter-frame sensing [30]. Accordingly, intra-frame sensing is performed when the SU system is quiet and the performance depends on the observation samples in the quiet periods. The frame structure for CR network is shown in Fig. 2. Based on this structure, there are sensing-transmission tradeoff problems. Under the constraint of PU system protection, the optimal sensing time to maximize the throughput [31] and to minimize outage probability [32] of the SU system have been studied, respectively.

However, there are some problems about the conventional structure: (1) the sample size of the quiet periods may not be enough to get good sensing performance; (2) all CR communications have to be postponed during channel sensing; (3) the placement of the quiet periods causes an additional burden of synchronization. To address these problems, novel spectrum sensing scheduling schemes have been proposed.

In [33], adaptively scheduling spectrum sensing and data transmission schemes have been proposed to minimize the negative effect caused by the traditional structure. The spectrum sensing is carried out when the channels are in poor conditions and transmitting data when the channels are good. To increase the sample size, quiet-active and active sensing schemes have been proposed [34]. In the quiet-active sensing scheme, the inactive SUs sense the channel in both the quiet and active data transmission periods. To fully avoid synchronization of quiet-periods, pure active sensing has been proposed where the quiet periods are replaced by “quiet samples” in other domains, such as quiet sub-carriers in orthogonal frequency division multiple access (OFDMA) systems.

D. Challenges

1) Wideband sensing:

Wideband sensing faces technique challenges and there is limited work on it. The main challenge
stems from the high data rate radio-front (RF) end requirement to sense the whole band, with the additional constraint that deployed CR systems (like mobile phones) will be limited in data processing rates. To achieve reliable results, the sample rate should be above the Nyquist rate if conventional estimation methods are used, which is a challenging task. Alternatively, the RF end can use a sequence of narrowband bandpass filters to sense one narrow frequency band at a time [35]. However, a large number of RF components are needed for the whole band. For more effective SU network, a multiband sensing-time-adaptive joint detection framework has been proposed in [36], [37], which adaptively senses multiple narrowband channels jointly to maximize the achievable opportunistic throughput of the SU network while keeping the interference with the PU network bounded to a reasonably low level. Based on energy detector for narrowband sensing, the sensing time and detection thresholds for each narrowband detector are optimized jointly, which is different from the previous multiband joint detection framework in [38].

2) Synchronization:
Besides the synchronization problem for quiet sensing period, spectrum synchronization before the data transmission for non-contiguous OFDM based systems is also a challenge. To address this challenge, a scheme has been proposed in [39] to use the received training symbols to calculate a posterior probability of each subband’s being active without the information of out-of-band spectrum synchronization. The proposed hard-decision-based detection (HDD) utilizes a set of adjacent subbands while the soft-decision-based detection (SDD) uses all the subbands for detection. Both HDD and SDD schemes provide satisfactory performance while SDD performs better.

III. COOPERATIVE SPECTRUM SENSING

The performance of spectrum sensing is limited by noise uncertainty, multipath fading, and shadowing, which are the fundamental characteristics of wireless channels. If the PU transmitter signal experiences deep fading or blocked by obstacles, the power of the received PU transmitter signal at the SU can be too weak to be detected, such as the case for SU_3 shown in Fig. 3. If the SU transmitter cannot detect the presence of the PU transmitter, while the PU receiver is within the transmission range of the SU, the transmission of the PU will be interfered. To address this problem, CSS has been proposed [11]. With the collaboration of several SUs for spectrum sensing, the detection performance will be improved by taking advantage of independent fading.
channels and multiuser diversity. Based on the decision fusion criteria, CSS can be realized in either a centralized or a distributed manner.

A. Centralized Cooperative Spectrum Sensing

A centralized CSS system consists of a secondary base station (SBS) and a number of SUs. In this system, the SUs first send back the sensing information to the SBS. After that, the SBS will make a decision on the presence or absence of the PU transmitter signal based on its received information and informs the SUs about the decision.

1) Data fusion schemes:

Different data fusion schemes for CSS have been studied in the literature. Reporting data from the SUs may be of different forms, types, and sizes. In general, the sensing information combination at the SBS can be categorized as soft combination and hard combination techniques.

Soft Combination

In soft combination, the SUs can send their original or processed sensing data to the SBS [4]. To reduce the feedback overhead and computational complexity, various soft combination schemes based on energy detection have been investigated [40]. In these schemes, each SU sends its quantized observed energy of the received signal to the SBS. By utilizing LRT at the SBS, the obtained optimal soft combination decision is based on a weighted summation of those energies.

At the SBS, linear combination of the test statistics from the SUs is the most common fusion rule. The global test statistic of linear combination is

$$Y_c = \sum_{j=1}^{N} w_j Y_j,$$

(6)

where $Y_j$ is the local test statistic (e.g. received energy in energy detection or in matched filtering [41], [42]) from SU$_j$, and $w_j$ is the weight. $Y_c$ is compared with a threshold, $\gamma_c$, to make decision. The optimization of linear CSS for the general model is non-convex and challenging. According to a taxonomy based on the probabilities of false alarm and detection, three kinds of CR systems have been proposed, namely conservative, aggressive, and hostile [41]. Since the last mode is too complex and of limited interest in applications, only the first two modes have been studied in [41]. Recently, a general model for all the modes has been investigated in [42]. The problem of determining the weights to maximize the detection probability under a given target false-alarm
probability has been studied. Based on the solution of a polynomial equation, the global optimum is found by an explicit algorithm.

The linear CSS design does not only focus on the detection probability optimization but also the tradeoff in sensing time setting. In the multi-channel system based on linear CSS, the optimal value of the decision threshold, $\gamma_c$, and sensing time, $\tau$, are obtained by maximizing the throughput of the SU system for a given detection probability [43]. The original non-convex problems can be successfully converted into convex subproblems. To avoid the convex approximation, an alternative optimization technique based on genetic algorithms [44] has been proposed to directly search the optimal solution.

Although soft combination schemes can provide a good detection performance, the overhead for feedback information is high. It makes the CSS impractical under a large number of cooperative SUs. A soften-hard combination with two-bit overhead [40] has been proposed to provide comparable performance with less complexity and overhead.

**Hard Combination**

For hard combination, the SUs feed back their own binary decision results to the SBS. Let $u_i$ denote the local decision of SU$_i$, where $u_i = 1$ and 0 indicate the presence ($H_1$) and the absence ($H_0$) of the PU transmitter signal, respectively. $u$ denotes the decision of the SBS. The most common fusion rules are OR-rule, AND-rule, and majority rule. Under the OR-rule, $u = 1$ if there exists $u_i = 1$. The AND-rule refers to the SBS determines $u = 1$ if $u_i = 1$, for all $i$. For the majority rule, if more than half of the SUs report $u_i = 1$, the SBS decides $u = 1$. These fusion rules can be generalized to a $K$-out-of-$N$ rule, where $u = 1$ if $K$ out of $N$ SUs report the presence of the PU transmitter signal. When $K = 1$ and $K = N$, the $K$-out-of-$N$ rule becomes the OR-rule and the AND-rule, respectively.

When the OR-rule or the AND-rule is used, the threshold of detector should be adjusted according to $N$ to get better performance than a non-cooperative system [45]. For the $K$-out-of-$N$ rule, the optimal value of $K$ and sensing time are obtained in [46] by maximizing the average achievable throughput of the SU system subject to the detection performance requirement. When all the SUs employ identical constant detection threshold, an optimal $K$ has been derived to improve both false-alarm and miss-detection probabilities in [47].

When the SUs have different detection SNRs, it is not efficient to use the $K$-out-of-$N$ fusion rule since it ignores the difference between decisions from a SU with high detection SNR and a
SU with low detection SNR. Weighted decision fusion schemes have been proposed to take into account the difference in the reliability of the decisions made by different SUs [48], which are reflected in the weights of the decisions at the SBS. The optimal fusion rules in three different scenarios have been derived during the optimization of the sensing-throughput tradeoff problem.

2) User selection:
User selection in CSS is crucial. Since SUs are located differently and strengths of received PU signals are different, it is shown in [45] that cooperation of all the SUs is not optimal. The optimal detection/false-alarm probabilities are achieved by selectively cooperating among SUs with high detection SNRs of the PU signal. The user selection is hard for the detection of small-scale PU transmitter signals which have small-footprint due to their weak power and unpredictability of spatial and temporal spectrum usage patterns [49]. Data-fusion range is identified as a key factor that enables effective CSS. The SUs in the data-fusion range cooperate to sense PU signals while others do not [49].

In multi-channel CR networks, it is impractical to make SUs to sense all the channels. The multi-channel coordination issues, such as, how to assign SUs to sense channels and to maximize the expected transmission time, have been studied in [50]. It has been shown that multi-channel coordination can improve CSS performance. Similar issues can be also found in sensor networks [51].

If the SUs cannot distinguish the signals from the PU and other SUs, it may lose the opportunity to access the spectrum [52]. The presence/absence of possible interference from other SU transmitters is a major component of the uncertainty limiting the detection performance. Coordinating the nearby SUs can reduce the uncertainty [52].

3) Sequential cooperative spectrum sensing:
In CSS, SPRT can opportunistically reduce the sample size required to meet the reliability target. In [53], sequential detection scheme has been designed to minimize the detection time. In the scheme, each SU calculates the log-likelihood ratio of its measurement and the SBS accumulates these statistics to determine whether to stop making measurement. A robust design is developed for the scenarios with unknown system parameters, such as noise variance and signal power. Moreover, a tradeoff between sensing time and average data rate of the SUs based on sequential sensing for multi-channel system has been studied in [54]. A stopping policy and an access policy are given to maximize the total achievable rate of the SU system under the miss detection
probability constraint for each channel.

4) Compressive sensing:
Compressive sensing can be applied as an alternative to reduce the sensing and feedback overhead. In [55], each SU senses linear combinations of multiple narrow bands by selective filters. The results are reported to the SBS, where matrix completion and joint sparsity recovery algorithms are applied to decode the occupied channels. Both algorithms allow exact recovery from incomplete reports and reduce feedback from the SUs to the SBS. Compressive sensing can also be used with other techniques [56].

B. Distributed Cooperative Spectrum Sensing

In the centralized CSS, the cooperative SUs need to feed back information to the SBS, which may incur high communication overhead and make the whole network vulnerable to node failure. To address these problems, distributed CSS can be applied.

In the CR networks, a SU can act as a relay for other SUs to improve the sensing performance [57]–[59]. For the proposed scheme in [57], one SU works as a amplify-and-forward (AF) relay for another SU to get the agility gain when the relay user detects the high PU transmitter signal power and the link between two SUs is good. The scheme is extended into multi-user networks [58]. To ensure asymptotic agility gain with probability one, a pairing protocol is developed. Besides AF relay scheme, a detect-and-relay (DR) scheme has been proposed [59], where only the relay SUs that detect the present of the PU transmitter signals forward the received signals to the SU transmitter. The results show that DR mode outperforms AF mode.

By using both temporal redundant information in two adjacent sensing periods and the spatial redundant information between two adjacent SUs, a space-time Bayesian compressive CSS for wideband networks has been developed to combat the noise [60]. For the multi-hop CR networks, a scheme [61] has been proposed to compress the signal in the time domain rather than the power spectral density (PSD) domain by letting each SU estimate PU transmitter and its own signal iteratively, and exchanging information with its neighboring SUs to get the global decision about the availability of the spectrum.
C. Challenges

1) Common control channel:
Common control channel between the SUs and the SBS is assumed in most of existing work, which requires extra channel resources and introduces additional complexity. Moreover, in the CR networks, it is difficult to establish the control channel at the beginning of the sensing stage and the change of the PUs’ activities may destroy the established control channel. In [62], a selective-relay based cooperative spectrum sensing scheme without common reporting control channels has been proposed. To limit interference to the PUs, only the relays (SUs) that detect the absence of the PU transmitter signal feed back to the SBS. The SBS then uses the received signals that experience fading to make a decision. Compared with the traditional scheme with common reporting control, the proposed scheme does not sacrifice the performance of the receiver operating characteristics (ROC). How to set up and maintain common control channel is still a challenge and open issue for CR networks.

2) Synchronization:
Most work is based on synchronous local observations. However, SUs locate at different places in practical CR system, resulting in a synchronization problem for data fusion. To enable combination of both synchronous and asynchronous sensing information from different SUs, a probability-based combination method has been proposed in [63] by taking the time offsets among local sensing observations into account.

3) Non-ideal information:
Most of the work analyzes the performance of CSS based on the perfect knowledge of the average received SNR of the PU transmitter signal. However, in practice, this is not always the case. The effect of average SNR estimation errors on the performance of CSS has been examined in [64]. In the noiseless-sample-based case, the probability of false alarm decreases as the average SNR estimation error decreases for both independent and correlated shadowings. In the noise-sample-based case, there exists a surprising threshold for the noise level. Below the threshold, the probability of false alarm increases as the noise level increases, where the probability decreases as the noise increases above the threshold.
IV. Spectrum Allocation and Sharing

In the previous sections, we have discussed the spectrum sensing techniques for CR networks. Based on the sensing results, the SUs have information about the channels that they can access. However, the channel conditions may change rapidly and the behavior of the PUs might change as well. In order to achieve better system performance, SUs should decide which channel can be used for transmission together with when and how to access the channel. To protect the PU system, the interference generated by the SUs should also be taken into account. Moreover, one SU needs to consider the behavior of other co-existing SUs. In the section, we will discuss the spectrum allocation and sharing schemes to address these problems.

Depending on spectrum bands the SUs use, the schemes can be divided into two types, namely open spectrum sharing and licensed spectrum sharing [6], [12]. In the open spectrum sharing system, all the users have the equal right to access the channels. The spectrum sharing among SUs for the unlicensed bands belongs to this type. The licensed spectrum sharing can also be called hierarchical spectrum access model. In such systems, the licensed PUs have higher priorities than the unlicensed SUs. Usually, there are no conflicts among PUs since they all have their own licensed bands. For the SUs, they need to adjust their parameters, such as transmit power and transmission strategy, to avoid the interruption to the PUs. According to the access strategies of the SUs, the hierarchical spectrum access model can be further divided into spectrum underlay and spectrum overlay [12]. In the spectrum underlay system, the SUs are allowed to transmit while the PUs are transmitting. The interference generated from the SUs need to be constrained to protect the PUs. The power control problem is one of the key issues in the systems. In the spectrum overlay systems, the SUs only can transmit when PUs are not or the SUs create interference-free transmissions to the PUs by using advanced techniques. Spectrum overlay is also called opportunistic spectrum access (OSA).

Another classification depends on whether there exists a central node to manage spectrum allocation and access procedure [6]. The whole procedure may be controlled by a central node. Due to the cost of the central node and information feedback, the centralized approaches may be impractical in some cases. In this case, the SUs may make their own decisions based on the observations of the local spectrum dynamics. This is called distributed spectrum sharing. Of course, several SUs in a system may cooperate with each other, which is called cooperative
spectrum sharing [6]. In the following, we will discuss some important techniques on spectrum allocation and sharing.

A. Resource Allocation and Power Control

In order to limit interference to the PUs created by the SUs, various resource allocation and power control schemes have been proposed for the CR networks.

1) Single-carrier and single-antenna systems:
For a point-to-point system with single antenna, the spectrum sharing model can be shown as in Fig. 4, where the SU transmitter can transmit as long as interference caused to the PU receiver is below a threshold. The channel gains from the SU transmitter to the SU receiver and the PU receiver are denoted $g_1$ and $g_0$, respectively. We denote the instantaneous transmit power at the SU transmitter as $P(g_0, g_1)$. In such a system, the most common constraints to protect the PUs are peak or average interference powers constraints (IPCs). Under peak IPCs, the overall instantaneous interference power generated by the SUs must be below a threshold, $Q_{pk}$, that is

$$g_0 P(g_0, g_1) \leq Q_{pk}, \quad \forall (g_0, g_1). \quad (7)$$

Similarly, the constraint on the average interference power can be expressed as

$$E[g_0 P(g_0, g_1)] \leq Q_{av}, \quad (8)$$

where $Q_{av}$ is the threshold. Moreover, the transmit power constraints (TPCs) of the SUs should be taken into account. The peak TPC can be expressed as

$$P(g_0, g_1) \leq P_{pk}, \quad (9)$$

where $P_{pk}$ is the peak transmit power limit. The average TPC can be expressed as

$$E[P(g_0, g_1)] \leq P_{av}, \quad (10)$$

where $P_{av}$ is the average transmit power limit.

The power control for systems with single PU pair and single SU pair have been investigated in [65]–[68]. In [65], different kinds of capacity for the SU system, such as the ergodic, outage, and minimum-rate, are determined for Rayleigh fading environments under both peak and average IPCs. The analysis has been extended to the case with TPCs in [66]. It is shown that the
average IPCs can provide better capacities than the peak average IPCs. If the statistics of any sensing metric $\xi$ conditioned on the PU being ON/OFF are known a priori to the SU transmitter, optimal power control schemes [67] and adaptive rate and power control schemes [68] have been proposed to maximize SU system capacity subject to average IPCs and peak TPCs. The system throughput can be improved using soft information.

More general models with multiple PUs and SUs have been studied in [69]. The power allocation problems for sum-rate maximization on Gaussian cognitive MAC under mutual interferences between the PU and the SU communications are formulated as a standard nonconvex quadratically constrained quadratic problem (QCQP) where semidefinite relaxation (SDR) has been applied to find a simple solution.

All the above work focuses on performance analysis for SU systems while the performance of PU systems under average and peak IPCs has been studied in [70]. It has been shown that the average IPCs can be advantageous over the peak IPCs in most cases. Moreover, the existing results demonstrated that the SU system can get better performance under average IPCs. Thus, average IPCs should be used in practice to protect both PU and SU systems.

Besides using IPCs, PU outage probability constraint (OPC) can be used to protect PU transmission [71], [72], where the outage probability of the PU transmission should not be below a given threshold. Under the OPC and average/peak TPCs, optimal power allocation strategies have been developed to maximize the ergodic and outage capacities of SU systems in [71]. Compare to IPCs, performance gains are obtained. By utilizing the outage information from the PU receiver on the PU feedback channel as an inference signal for coordination, a discounted distributed power control algorithm has been proposed in [72] to maximize the utilities of the SUs under OPC and peak TPCs.

2) Multi-carrier and multi-channel systems:

In a multi-carrier or multi-channel system, interference generated by the SU to the PU can be considered either in the whole bands/channels or each sub-band (sub-channel) separately. Similar to the case of single-carrier and single-antenna systems, the IPCs for the PUs can be divided into two types: peak and average IPCs.

Power control schemes under different constraints for both PU and SU systems have been extensively studied. In [73], capacity maximization for the SU system under TPCs as well as either peak or average IPCs is investigated. It is shown that the average IPC provides better
performance for the SU system than the peak IPC. Instead of using IPC directly, optimal power allocation under OPC has been investigated [74]. With the CSIs of the PU link, the SU link, and the SU-to-PU link at the SU, a rate loss constraint (RLC) has been proposed, where the rate loss of the PUs due to the SU transmission should be below a threshold. Under RLC, the transmission efficiency of the SU system increases [75]. For practical point of view, a hybrid scheme by using both IPC and RLC is analyzed as well. Since the spectrum sensing results are not reliable, the probabilistic information of channel availability has been used to assist resource allocation in a multi-channel environment [76]. Compared with the conventional hard decision based IPCs, the proposed approach can utilize the spectrum more efficiently while protect the PUs from unacceptable interference. By considering the SINR requirements for the SUs, downlink channel assignment and power control schemes have been studied under the IPCs to the PUs [77] to maximize the number of active SUs.

Besides the above co-existence scenario, another scenario is in the multi-band system where PU and SU are co-located in the same area with side-by-side bands. For this scenario, power allocation schemes have been proposed in [78]. A risk-return model, which includes these two co-existence scenarios together, has been introduced in [79], and takes into account the reliability of the available sub-bands, their power constraints, and IPCs to the PUs. Besides the optimal power allocation, three suboptimal schemes, namely, the step-ladder, nulling and scaling schemes have been developed.

3) Multi-antenna systems:
For multi-antenna systems, most work jointly optimizes power allocation and beamforming [80]–[83]. Under IPCs and peak TPCs, the power allocation and beamforming design for sum-rate maximization and signal-to-interference-plus-noise ratios (SINRs) balancing problems have been studied for SIMO systems in [80]. For SINR balancing, all the SUs can achieve their target SINRs fairly. When linear minimum mean-square-error (MMSE) receivers are utilized, multiple constraints can be decoupled into several subproblems with a single constraint. The study of SINR-balancing has been extended into MIMO systems in [81], where a robust beamforming design is developed to limit the interference leakage to PU below a specific threshold with a certain probability. Beamforming for MIMO systems has been proposed to maximize the SINR of SUs under IPCs in [82]. A unified homogeneous quadratically constrained quadratic program is used to solve the optimization problems. In practice, it may be impossible that the SINR
requirements of all the SUs are satisfied. For this situation, a joint beamforming and admission
control scheme has been proposed to minimize the total transmit power of the SU system under
IPCs [83].

4) Multi-hop systems:
In a relay-assisted system, interference from all relay nodes to the PU receiver should be
considered. In [84], transmit power allocation (TPA) schemes among relays have been studied,
where overall transmit power is minimized under IPCs as well as the SINR requirement of the
targeting SU receiver. A fully distributed TPA has been proposed and provides an almost optimal
solution as centralized solution. To reduce the energy consumption of the fully distributed TPA, a
distributed feedback assisted TPA has been proposed by feeding back the estimated real-valued
transmit power. Besides power allocation, channel allocation has been studied in [85]. In a
three-node CR network, end-to-end transmission is categorized into three modes, namely direct,
dual-hop, and relay channels. The optimal end-to-end channel and power allocation scheme can
be realized by analyzing optimal power allocation for each mode and choose the mode that can
provide the highest system throughput. Joint rate, power control, and channel allocation problem
to maximize the throughput of the relay-assisted SU system has been studied in [86], where
an optimal solution can be obtained by dividing the original problem into a base station (BS)
master problem and the relay station subproblems.

B. Spectrum Sharing Game

Game theory is a well-developed mathematical tool to model strategic situations, where any
individual’s success in making choices depends on the choices of others. In the CR networks, the
SUs compete for spectrum resources to maximize their own utilities where game theory models
can be used [87]. Moreover, the game theory can also be utilized to analyze both the PU and
SU systems’ behaviors, where they try to maximize their own profits.

From the game-theoretical perspective, power control can be formulated as a distributed game
among all the SUs [88], where SUs maximize their own utilities by adjusting transmission
powers. The total CR network capacity is maximized when the game reaches a Nash equilibrium
(NE). In a uplink multiuser CR system, a non-cooperative power control game among SUs can be
applied to maximize energy efficiency with a fairness constraint [89]. To jointly design waveform
and resource allocation, a general framework has been developed [90], which can be applied to
many radio platforms, such as frequency, time, or code division multiplexing, and even agile framework with different expansion functions.

The above work considers SU system only. To take the activities of PUs into account, a dynamic spectrum leasing paradigm based on a game-theoretical framework has been proposed [91], [92], which provides an incentive for the PUs to actively allow SUs’ transmission.

Besides for the resource allocation, game theory can also have other applications such as stimulating the cooperation between SUs [93] and combating PU emulation attacks [94], [95].

However, there are still unaddressed issues in this area. Only spectrum sharing constraints are imposed on the games in most of existing work. Deviations from the ideal games due to non-cooperating SUs or channel constraints still need further study.

C. Transmission Design for Cognitive Radio Systems

In CR networks, the transmission protocols of the SUs can be designed to achieve satisfactory system performance together with fulfilling the IPCs for the PUs.

Relays are the most common choices for increasing SU system performance, as shown in Fig. 5. Unlike the traditional cooperation transmission system, the performance of the cooperative SU system decreases by introducing the IPCs. For example, the outage probability may increase [96]. With the increase of the number of relays, the outage performance gap decreases. The relays in the CR networks can assist the transmission between the SU transmitter and receiver to reduce the required transmit power and decrease the interference generated to the PU system [97]. The transmission opportunities created through this way is called as spatial SHs. The relay selection for outage performance optimization of the SU system under either IPCs [98] or OPC [99] for the PU system have been studied. Power allocation and relay selection can be designed jointly to maximize SU system throughput [100]. Moreover, spectrum sensing and relay selection can be designed jointly [62], [101]. Without a dedicated relay channel, the best relay is selected for transmission based on the sensing information from the relays that detect the PU transmitter signals.

The SU itself can work as a relay to assist PU transmission while transmitting its own data at the same time [102], [103]. A two-phase transmission protocol in a single antenna system has been considered in [102], where the PU transmits in the first phase and the SU transmitter assigns fractions of the available power to the PU data and its own data for the second phase
transmission, respectively. This protocol guarantees the performance of the PU system. With the help of a multi-antenna SU transmitter, both PU and SU systems can achieve better performance by beamforming at the AF SU transmitter [103].

To reduce interference in a MIMO system, the spatial freedom created by antennas can be used. An opportunistic spatial orthogonalization (OSO) scheme [104] has been proposed. With OSO, the SU system can get significant performance improvement without sacrificing of PU system’s performance much. Taking the time dimension into account, the interference-free co-existing PU and SU transmissions can be achieved based on orthogonal space-time coding [14].

D. Challenges

1) Joint sensing and access:
In most existing work, the sensing and access techniques are designed separately. However, these two parts are interactive. With different objectives of SU systems, different protection levels for PU systems are needed. It is beneficial to consider these two parts jointly [105]. A joint sensing time and power allocation scheme has been studied in [105] under the average IPCs and TPCs to maximize the ergodic throughput of SU systems. More work is desired in this topic.

2) Channel estimation:
The link condition between PU-and-SU is an important parameter for most of techniques in CR networks. However, the SU-to-PU channel gain is difficult to be observed by the SU in practice. To estimate the link condition, the SU can observe PU’s behavior by sending out a disturbing probing signal [106] or eavesdrop PU’s automatic repeat request feedback information [107]. To avoid the estimation of the actual channels between SU transmitter and PUs, a novel practical cognitive beamforming [108] has been proposed based on the effective interference channel, which combines information of the actual channels and the beamforming vectors used by the PUs.

V. APPLICATIONS OF COGNITIVE RADIO

The development of spectrum sensing and spectrum sharing techniques enable the applications of CR in many areas. In this section, we introduce some of them.
A. TV White Spaces

The main regulatory agencies for the unlicensed use of TV white spaces are the FCC in the United States, the Office of Communications (Ofcom) in the United Kingdom, and the Electronic Communications Committee (ECC) of the conference of European Post and Telecommunications in Europe. After many years of effort in this area, FCC released the final rules for using the TV white space in September 2010 [109], which led to the culmination of this field. Meanwhile, other agencies have been also getting progress [110]. This is based on the idea of having an accessible database (centralize-fashion) of free TV bands, otherwise called TV white space, or to sense and obtain SHs (distributed-fashion) within TV bands to utilize for SUs communication.

B. Cellular Networks

The applications of CR in cellular networks are emerging in recent years. To overcome the indoor coverage problem and adapt to traffic growth, the concept of small cells, such as femtocells, has been proposed in 3GPP LTE-Advanced (LTE-A) [111] and IEEE 802.16m [112], and companies like PicoChip driving femtocell revolution. The femtocell unit has the function of the typical BS (eNodeB in LTE). However, the self-deployment property of the femtocells makes the centralized interference management impractical. Fig. 6 illustrates the femtocell interference scenario, where distributed spectrum planning schemes are needed. With CR, the femtocells can search and estimate the available spectrum bands in order to maintain the coverage and avoid the interference to the other femtocells and macrocells.

C. Military Usage

CR is a must-have technique for military usage. With CR, the users can recognize the enemies’ communications and protect their own. Moreover, the users can search for more transmission opportunities. The US department of defense (DoD) has already established programs such as SPEAKeasy radio system and next Generation (XG) to exploit the benefits of CR techniques [6].

VI. Conclusions

CR technology has been studied to increase the spectrum utilization efficiency. With spectrum sensing techniques, the SUs are able to monitor the activities of the PUs. To address the
limitations of the spectrum sensing techniques by a single SU, cooperative spectrum sensing schemes have been discussed. Based on the spectrum sensing results, the SUs can access the spectrum bands under the interference limit to the PUs. Different spectrum sharing and allocation schemes have been considered to increase the spectrum efficiency. Even though many critical issues in CR have been addressed in the past decade, there are still some challenges. Nevertheless, we believe this technology will be applied to many real systems in the near future.

Due to the space limitation, we have left out some topics, such as security, policy issues, and CR implementation architecture. The readers can refer to some other publications in recent special issues, e.g., [113], [114], and [115], which may cover these topics.

REFERENCES


27


TABLE I
LIST OF ABBREVIATIONS.

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Description</th>
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<tbody>
<tr>
<td>AF</td>
<td>amplify-and-forward</td>
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<tr>
<td>AWGN</td>
<td>additive white Gaussian noise</td>
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<tr>
<td>BS</td>
<td>base station</td>
</tr>
<tr>
<td>CAF</td>
<td>cyclic autocorrelation function</td>
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<td>CR</td>
<td>cognitive radio</td>
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<tr>
<td>CSD</td>
<td>cyclic spectrum density</td>
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<td>CSS</td>
<td>cooperative spectrum sensing</td>
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<tr>
<td>DoD</td>
<td>department of defense</td>
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<td>DR</td>
<td>detect-and-relay</td>
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<td>ECC</td>
<td>Electronic Communications Committee</td>
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<tr>
<td>FCC</td>
<td>Federal Communications Commission</td>
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<tr>
<td>GLRT</td>
<td>generalized likelihood ratio test</td>
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<td>HDD</td>
<td>hard-decision-based detection</td>
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<tr>
<td>IPC</td>
<td>interference powers constraint</td>
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<tr>
<td>LRT</td>
<td>likelihood ratio test</td>
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<td>LTE-A</td>
<td>LTE-Advanced</td>
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<td>MIMO</td>
<td>multiple-input multiple-output</td>
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<td>MLE</td>
<td>maximum likelihood estimate</td>
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<td>MME</td>
<td>maximum-minimum eigenvalue</td>
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<td>MMSE</td>
<td>minimum mean-square-error</td>
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<td>NE</td>
<td>Nash equilibrium</td>
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<td>NP</td>
<td>Neyman-Pearson</td>
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<tr>
<td>Ofcom</td>
<td>Office of Communications</td>
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<td>OFDMA</td>
<td>orthogonal frequency division multiple access</td>
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<td>OPC</td>
<td>outage probability constraint</td>
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<td>OSA</td>
<td>opportunistic spectrum access</td>
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<tr>
<td>OSO</td>
<td>opportunistic spatial orthogonalization</td>
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<tr>
<td>PDF</td>
<td>probability density function</td>
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<td>PSD</td>
<td>power spectral density</td>
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<td>PU</td>
<td>primary user</td>
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<td>QAM</td>
<td>quadrature amplitude modulation</td>
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<tr>
<td>QCQP</td>
<td>quadratically constrained quadratic problem</td>
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<tr>
<td>RF</td>
<td>radio-front</td>
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<tr>
<td>RLC</td>
<td>rate loss constraint</td>
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<tr>
<td>ROC</td>
<td>receiver operating characteristics</td>
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<tr>
<td>SBS</td>
<td>secondary base station</td>
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<tr>
<td>SDD</td>
<td>soft-decision-based detection</td>
</tr>
<tr>
<td>SDR</td>
<td>semidefinite relaxation</td>
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<tr>
<td>SFD</td>
<td>spectral feature detector</td>
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<tr>
<td>SH</td>
<td>spectrum hole</td>
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<tr>
<td>SINR</td>
<td>signal-to-interference-plus-noise ratio</td>
</tr>
<tr>
<td>SNR</td>
<td>signal-to-noise ratio</td>
</tr>
<tr>
<td>SPRT</td>
<td>sequential probability ratio test</td>
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<tr>
<td>SU</td>
<td>secondary user</td>
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<tr>
<td>TPA</td>
<td>transmit power allocation</td>
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<tr>
<td>TPC</td>
<td>transmit power constraint</td>
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<tr>
<td>XG</td>
<td>next generation</td>
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Fig. 1. Spectrum sensing concept.
Fig. 2. Frame structure for periodic spectrum sensing, where $\tau$ denotes the sensing period and $T - \tau$ denotes the data transmission or silent period.
Fig. 3. Cooperative spectrum sensing model, where SU₁ is shadowed over the reporting channel to the secondary base station (SBS) and SU₃ is shadowed over the sensing channel.
Fig. 4. Spectrum sharing model.
Fig. 5. Relay-aided transmission in SU system.
Fig. 6. Illustration of femtocell interference.