



# INBOUND SHIPMENT COORDINATION

SENIOR DESIGN FINAL PRESENTATION  
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# PROJECT OVERVIEW

## Problem

< 2% of shipments are part of multi-stop pickups

## Design Strategy

Integer programming

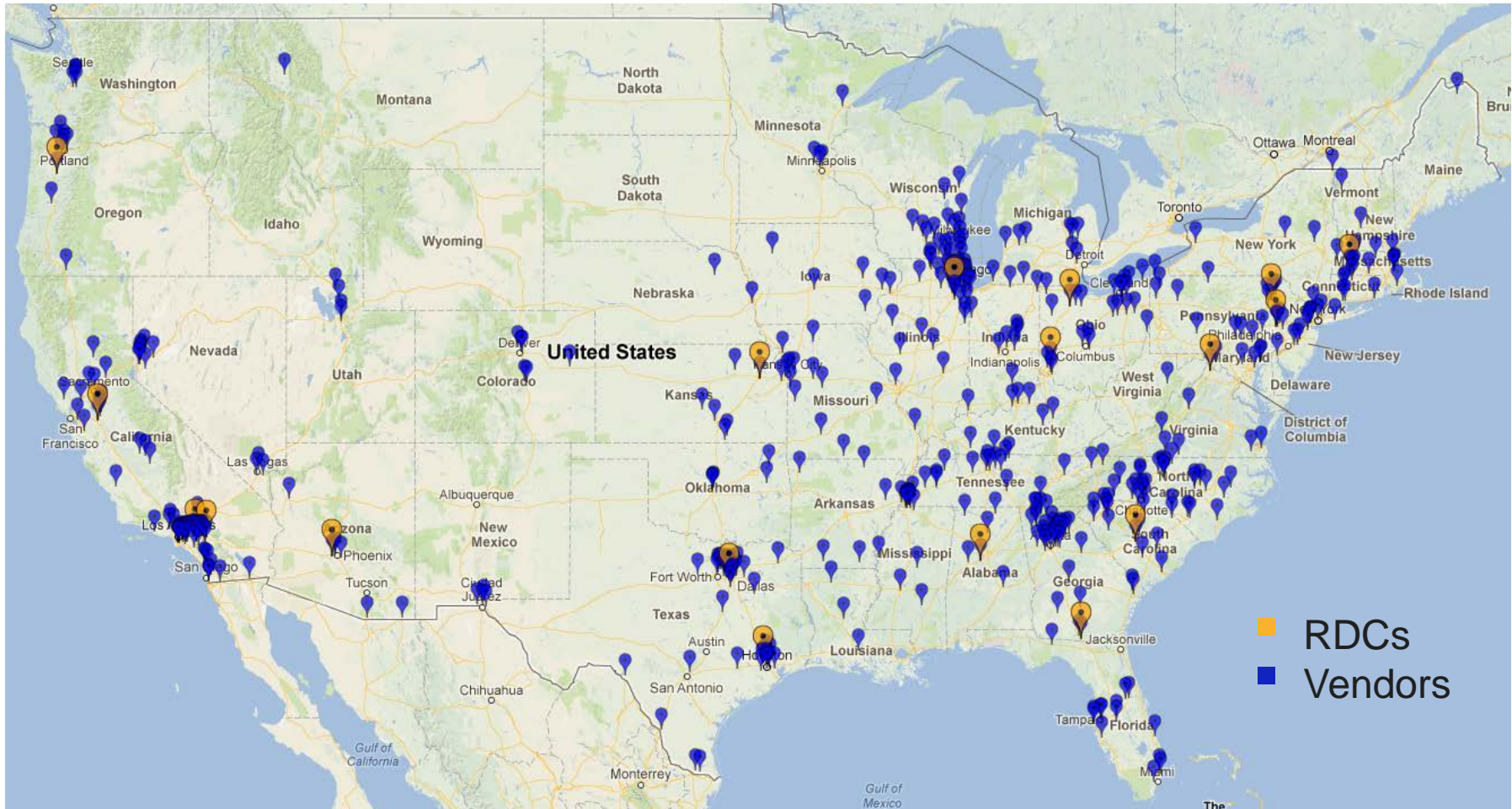
## Deliverable

Excel tool of 1,233 vendor groups

## Project Value

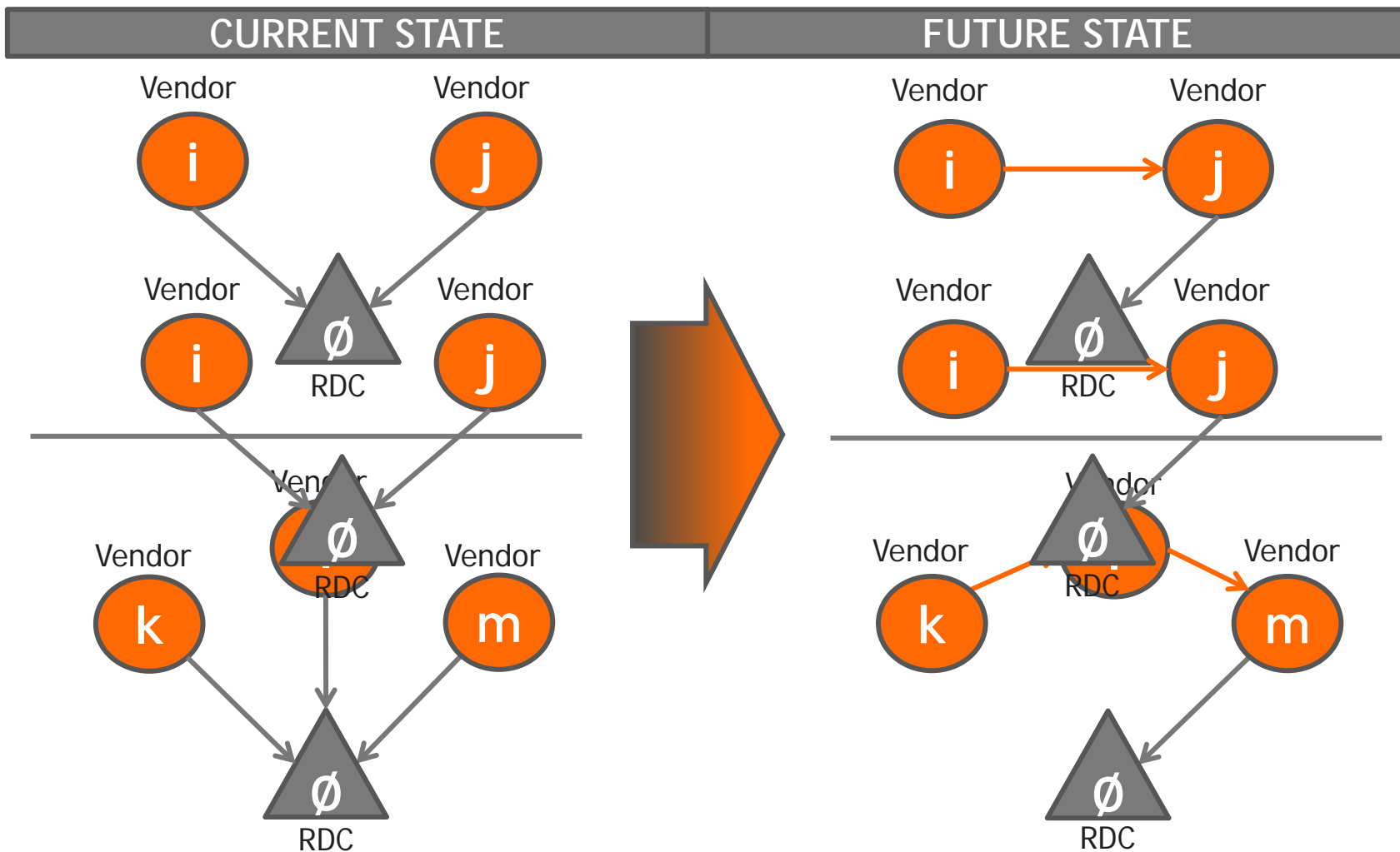
14,923 multi-stop pickup opportunities  
\$9.1M reduction in transportation costs

# INBOUND TRANSPORTATION NETWORK



18 Rapid Deployment Centers (RDCs) & 633 Vendors

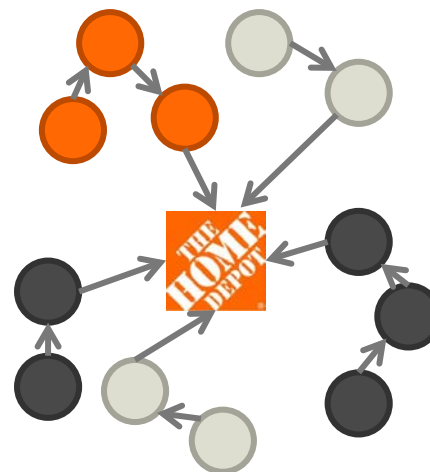
# PROBLEM



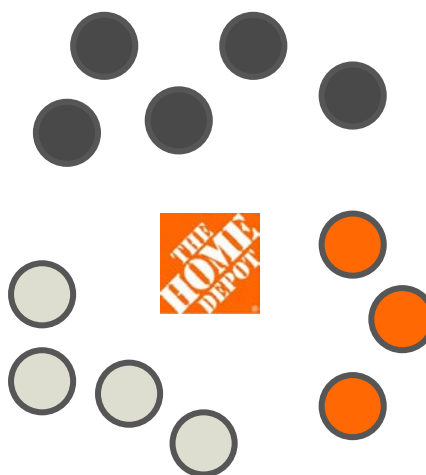
# PROJECT FLOW



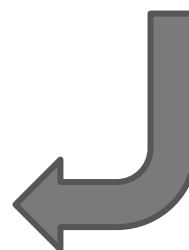
Individual Shipments



Multi-Stop Shipments



Vendor Groups



# DATA

- Bid Rate
- Mode of Transportation
- Shipment Date
- Total Cost
- Volume
- Weight



Bid Rate from Boston to Los Angeles



# DESIGN STRATEGY

## Objective

Maximize cost savings via multi-stop pickup coordination



## Pre-processing

Create all feasible pairs and triplets



## Optimization

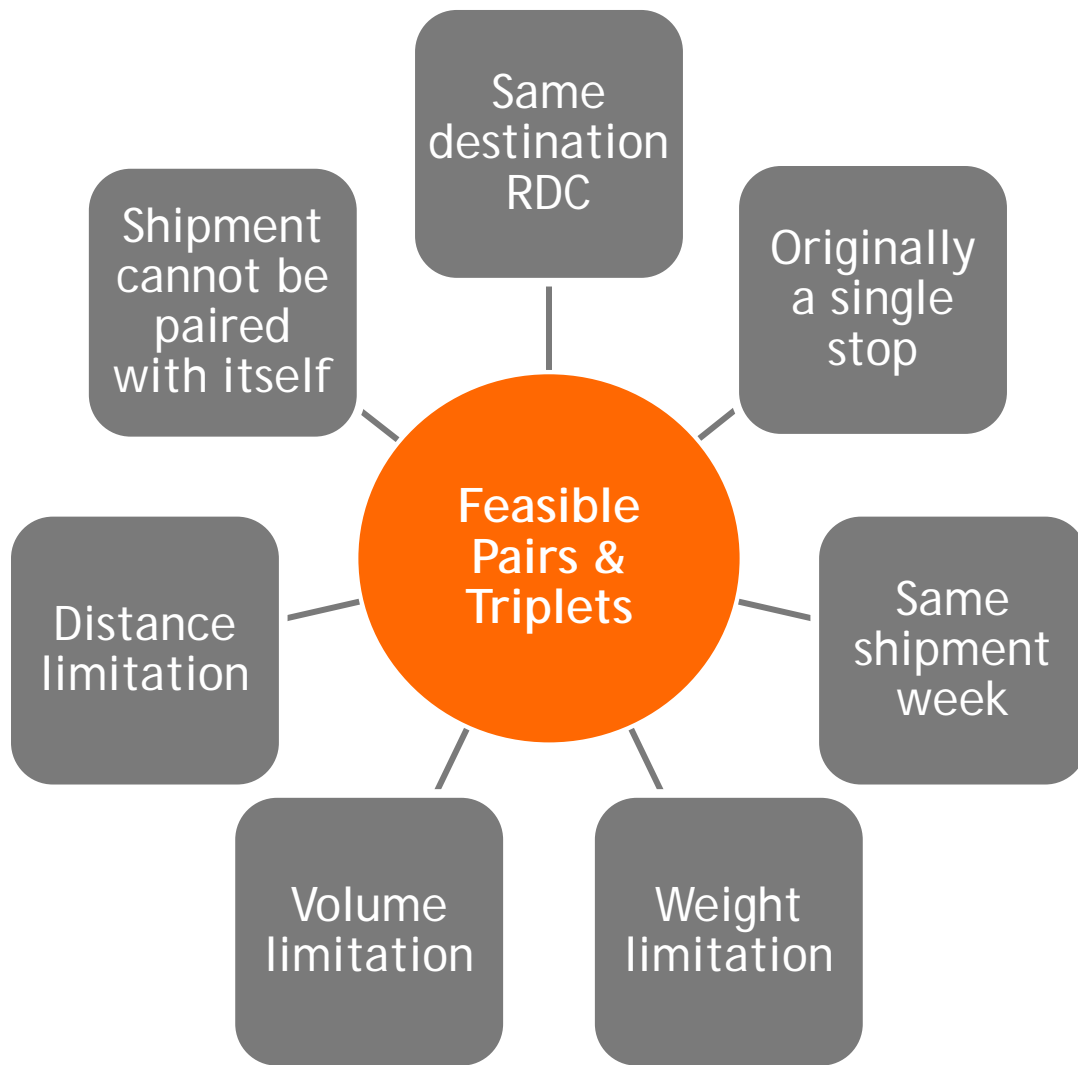
Integer Programming via FICO® Xpress Optimization Suite



## Post-processing

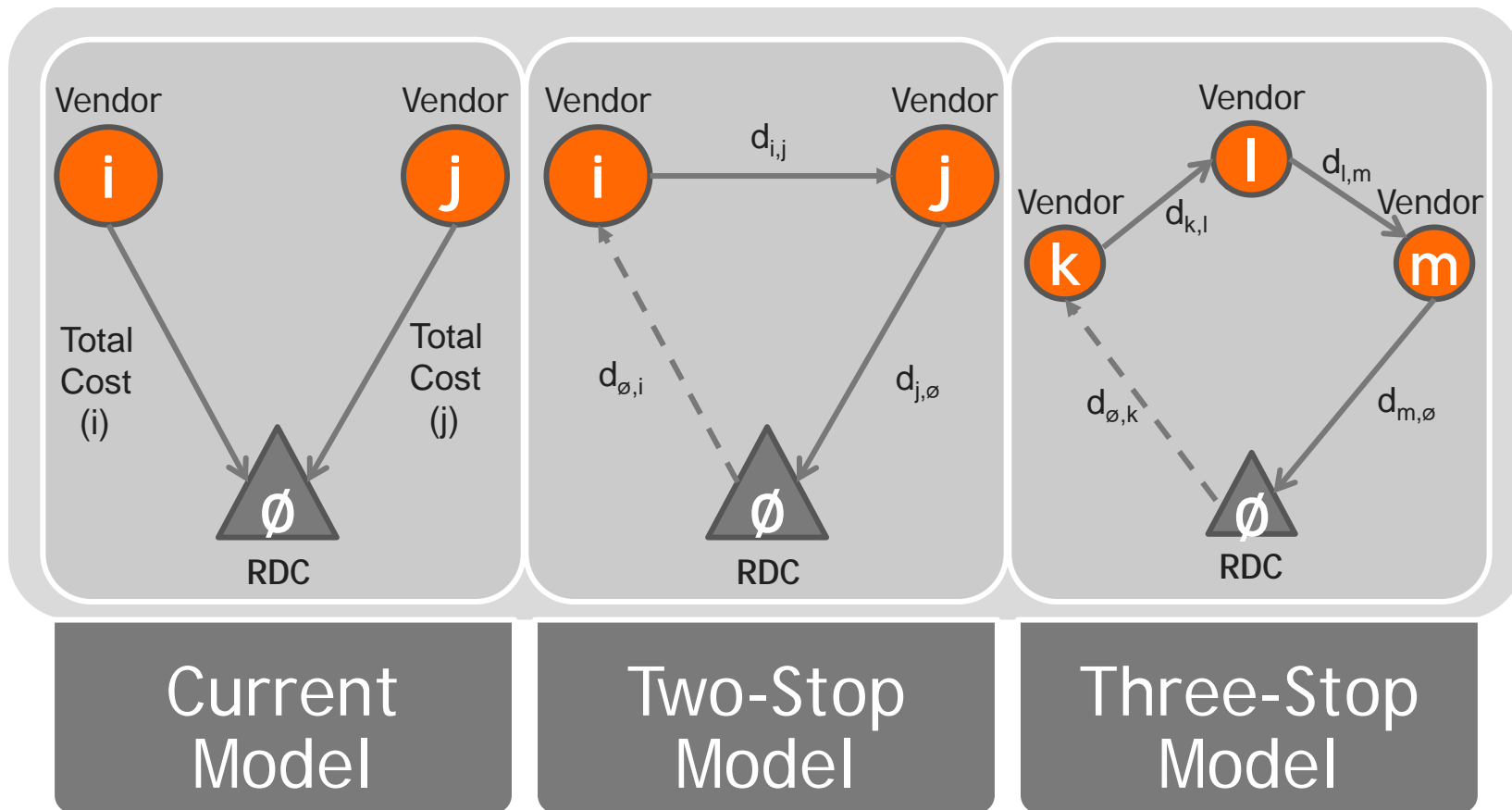
Create vendor groups from combined shipments

# MATLAB PRE-PROCESSING





# COST MODEL





# OPTIMIZATION MODEL & CONSTRAINTS

## Objective Function

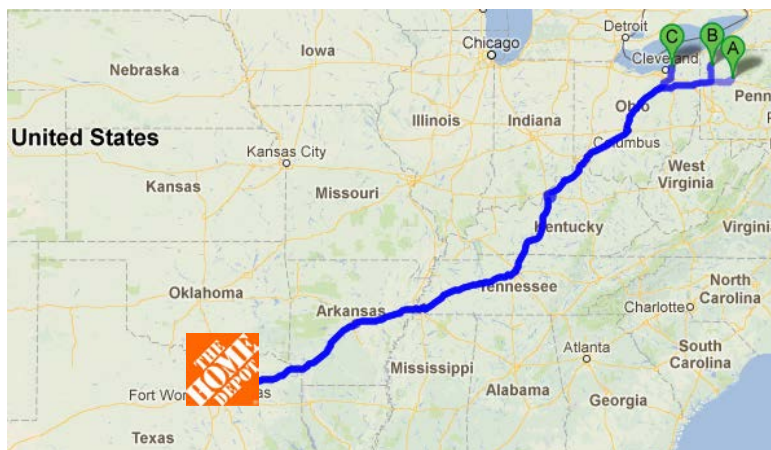
$$\max \left\{ \sum_i \sum_j s_{i,j} x_{i,j} + \sum_k \sum_l \sum_m s_{k,l,m} x_{k,l,m} \right\}$$

s.t.

- 1)  $\left[ \frac{ORM_{i,j}}{50} + 2.5 \right] * x_{i,j} \leq 11$
- 2)  $\left[ \frac{ORM_{k,l,m}}{50} + 2.5 \right] * x_{k,l,m} \leq 11$
- 3)  $\sum_i \sum_j x_{i,j,k} + \sum_j \sum_l x_{j,k,l} + \sum_l \sum_m x_{k,l,m} + \sum_j x_{j,k} + \sum_l x_{k,l} \leq 1, \forall k$
- 4)  $x_{i,j} \in \{0,1\}$
- 5)  $x_{k,l,m} \in \{0,1\}$

# OPTIMIZATION OUTPUT SAMPLE

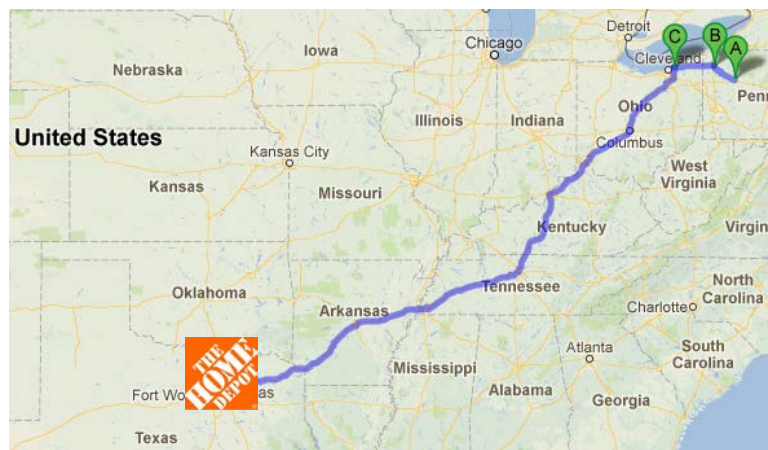
## Independent Routes



Total Distance: 3,748.96 miles

Total Cost: \$2,751.79

## Combined Routes

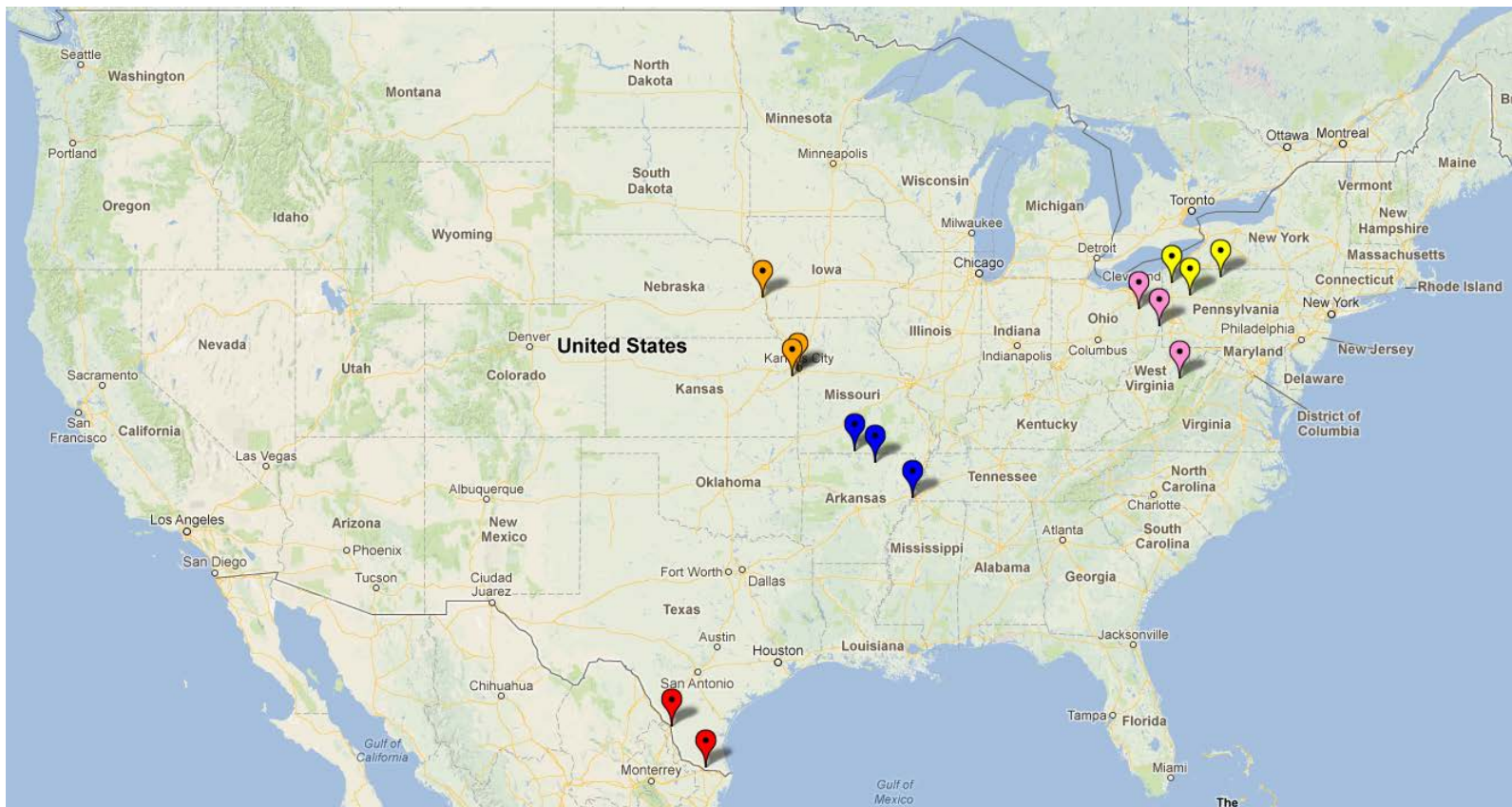


Total Distance: 1,321.17 miles

Total Cost: \$1,681.30

Savings: \$890.49

# POST PROCESSING OUTPUT SAMPLE

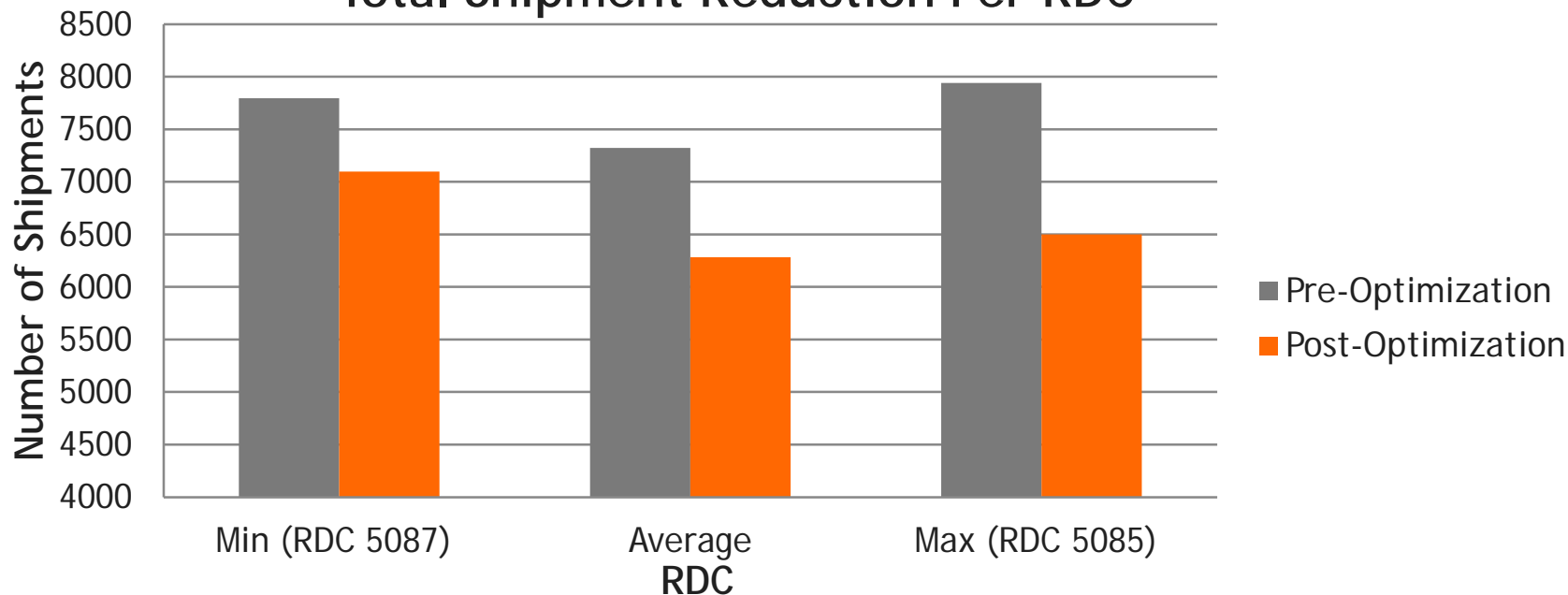


Five Most Frequently Combined Vendor Groups for all RDCs



# ANALYSIS

## Total Shipment Reduction Per RDC



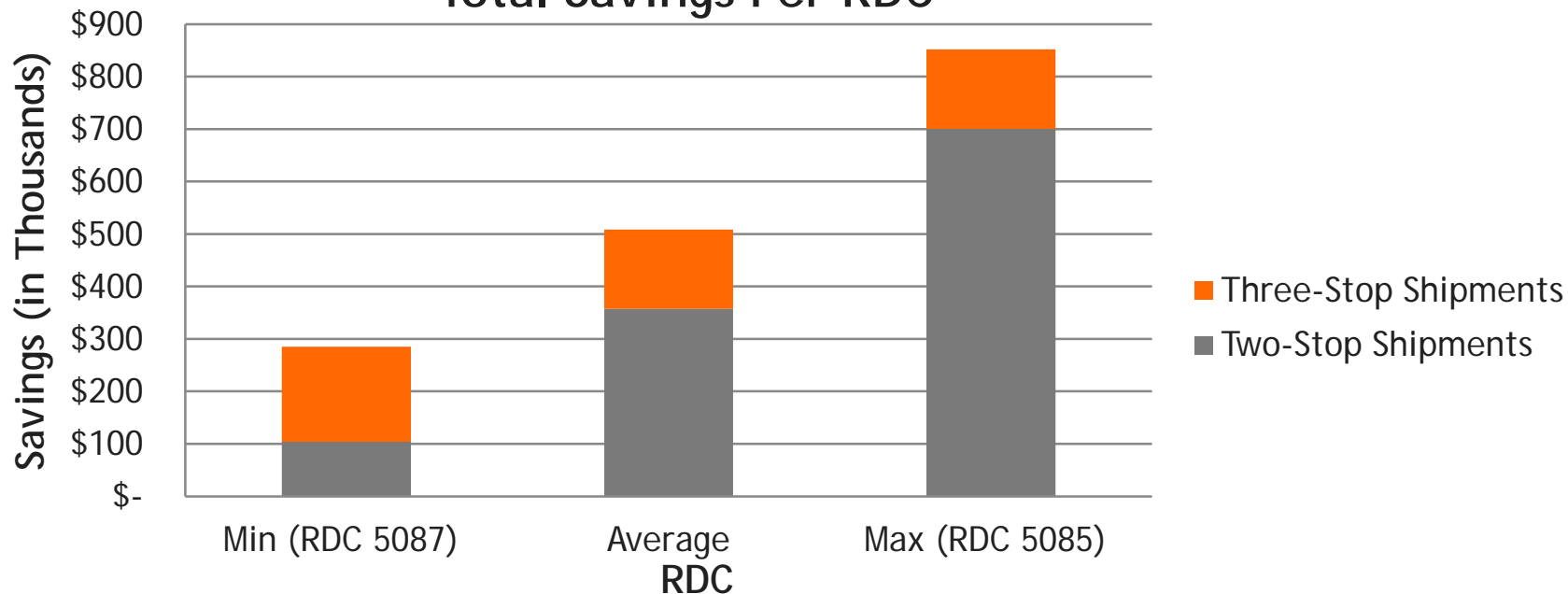
## Number of Multi-Stop Pickups Per RDC

	2-Stops	3-Stops
Minimum	208	161
Average	620	209
Maximum	1121	309



# ANALYSIS

## Total Savings Per RDC



## Vendor Group Sizes Per RDC

	Groups of 3	Groups of 4	Groups of 5
Average	52	13	3
Total	940	240	53



# DELIVERABLE

State: MO | Vendor: 327123MO001 | RDC: 5023



## Inbound Vendor Coordination

State: MO  
Vendor ID: 327123MO001 RDC: 5023

Run

Clear

### Vendor Pairs and Triplets

A	B	C	Frequency	Savings
327123MO001	50920MO001	6366820KS001	12	\$ 10,029.23
327123MO001	576006MO001	6366820KS001	5	\$ 3,211.14
327123MO001	50920MO001	73755MO001	5	\$ 5,725.12
14894KS001	327123MO001	6366820KS001	3	\$ 1,111.71
327123MO001	50920MO001	801613MO001	3	\$ 4,170.23
327123MO001	50920MO001	689130MO001	3	\$ 1,986.08
-	327123MO001	6366820KS001	3	\$ 1,679.69
-	10618NE001	327123MO001	2	\$ 990.86

### Vendor Groups

A	B	C	D	E	Group Size
327123MO001	50920MO001	6366820KS001	689130MO001	801613MO001	5
-	327123MO001	50920MO001	576006MO001	6366820KS001	4
-	327123MO001	50920MO001	6366820KS001	73755MO001	4
-	14894KS001	327123MO001	6366820KS001	689130MO001	4
-	-	10618NE001	327123MO001	801613MO001	3
-	-	327123MO001	689130MO001	817880MO002	3

# SUMMARY

## Problem:

< 2% of shipments are part of multi-stops

## Design Strategy:

IP optimization model

## Deliverable:

Excel tool of 1,233 vendor groups

## Project Value:

14% of shipments are part of multi-stops  
\$9.1M in transportation cost savings





# QUESTIONS



# APPENDIX



# MATLAB DATA PRE-PROCESSING

1. The distance between vendors that are combined is limited to 225 miles.
  - a) For a two-stop from  $i$  to  $j$ :  $\text{distance}_{i,j} < 225$
  - b) For a three-stop from  $i$  to  $j$  and  $j$  to  $k$ :  $\text{distance}_{i,j} + \text{distance}_{j,k} < 225$
2. The maximum weight that a 53-foot container can withstand is 42,000 pounds.
  - a) For a two-stop combining shipments  $i$  and  $j$ :  $\text{weight}_i + \text{weight}_j \leq 42,000$
  - b) For a three-stop combining shipments  $i$ ,  $j$ , and  $k$ :  $\text{weight}_i + \text{weight}_j + \text{weight}_k \leq 42,000$
3. The maximum volume that a 53-foot container can withstand is 3,000 cubic feet.
  - a) For a two-stop combining shipments  $i$  and  $j$ :  $\text{volume}_i + \text{volume}_j \leq 3,000$
  - b) For a three-stop combining shipments  $i$ ,  $j$ , and  $k$ :  $\text{volume}_i + \text{volume}_j + \text{volume}_k \leq 3,000$
4. The shipment date can move within the same calendar week as it is currently scheduled.
  - a) For a two-stop combining shipments  $i$  and  $j$ :
    - i.  $\text{week}_i = \text{week}_j$
    - ii.  $\text{year}_i = \text{year}_j$
  - b) For a three-stop combining shipments  $i$ ,  $j$ , and  $k$ :
    - i.  $\text{week}_i = \text{week}_j = \text{week}_k$
    - ii.  $\text{year}_i = \text{year}_j = \text{year}_k$



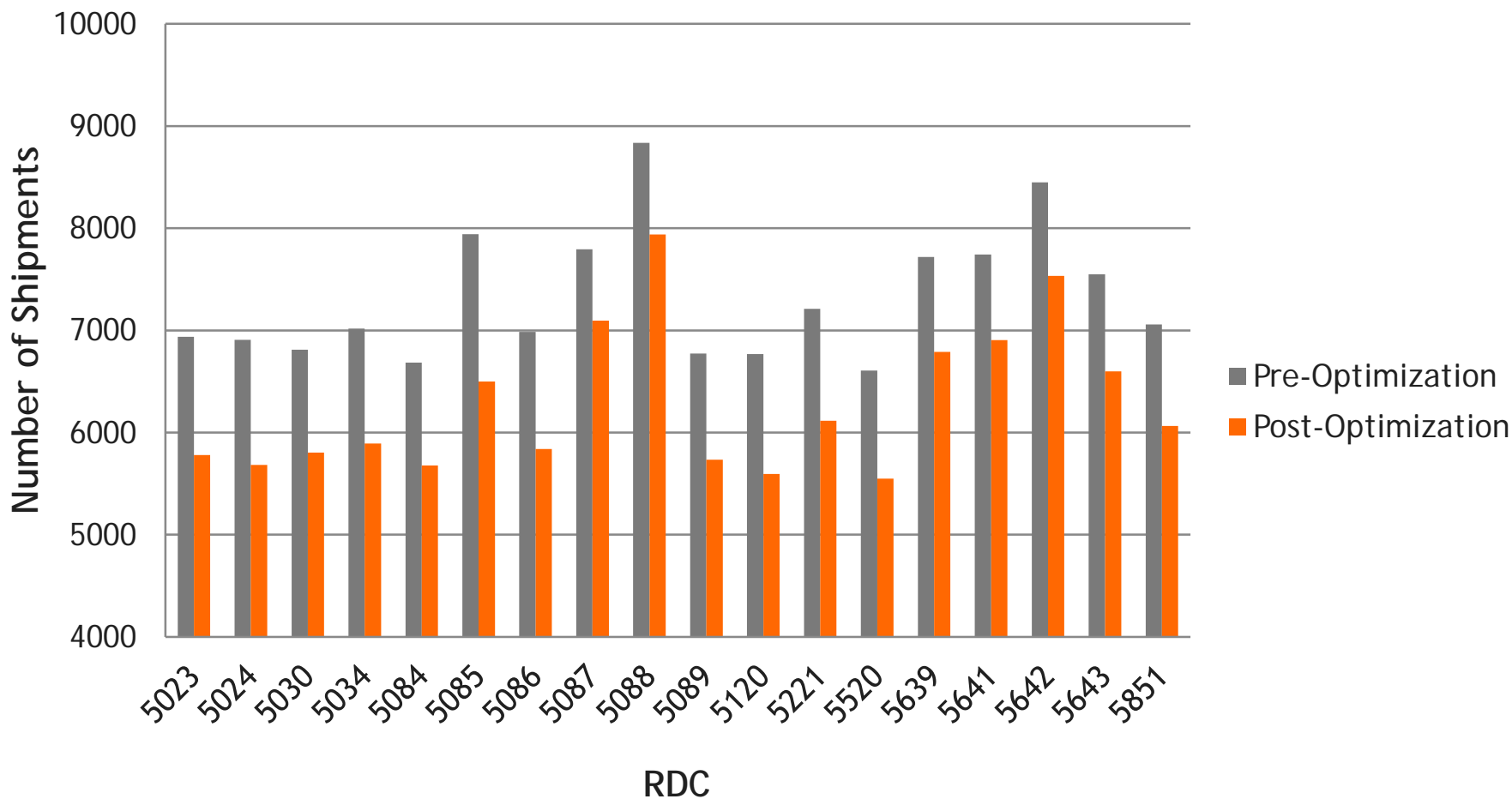
# OPTIMIZATION VARIABLES

- Data parameters
  - $i = j = k = l = m = \{\text{shipments}\}$
  - $\emptyset = \{\text{RDC}\}$
  - $s_{i,j}$ : cost savings per truck if shipments  $i$  and  $j$  are combined
  - $s_{k,l,m}$ : cost savings per truck if shipments  $k$ ,  $l$ , and  $m$  are combined
  - $ORM_{i,j}$ :  $\text{distance}_{\emptyset,j} + \text{distance}_{i,j} - \text{distance}_{\emptyset,l}$
  - $ORM_{k,l,m}$ :  $\text{distance}_{\emptyset,m} + \text{distance}_{l,m} + \text{distance}_{k,l} - \text{distance}_{\emptyset,k}$
- Decision variables
  - $x_{i,j} = 1$ , if a truck drives directly from shipment  $i$  to shipment  $j$   
0, otherwise
  - $x_{k,l,m} = 1$ , if a truck drives from the origin of shipment  $k$  to shipment  $m$  to shipment  $l$   
0, otherwise



# ANALYSIS

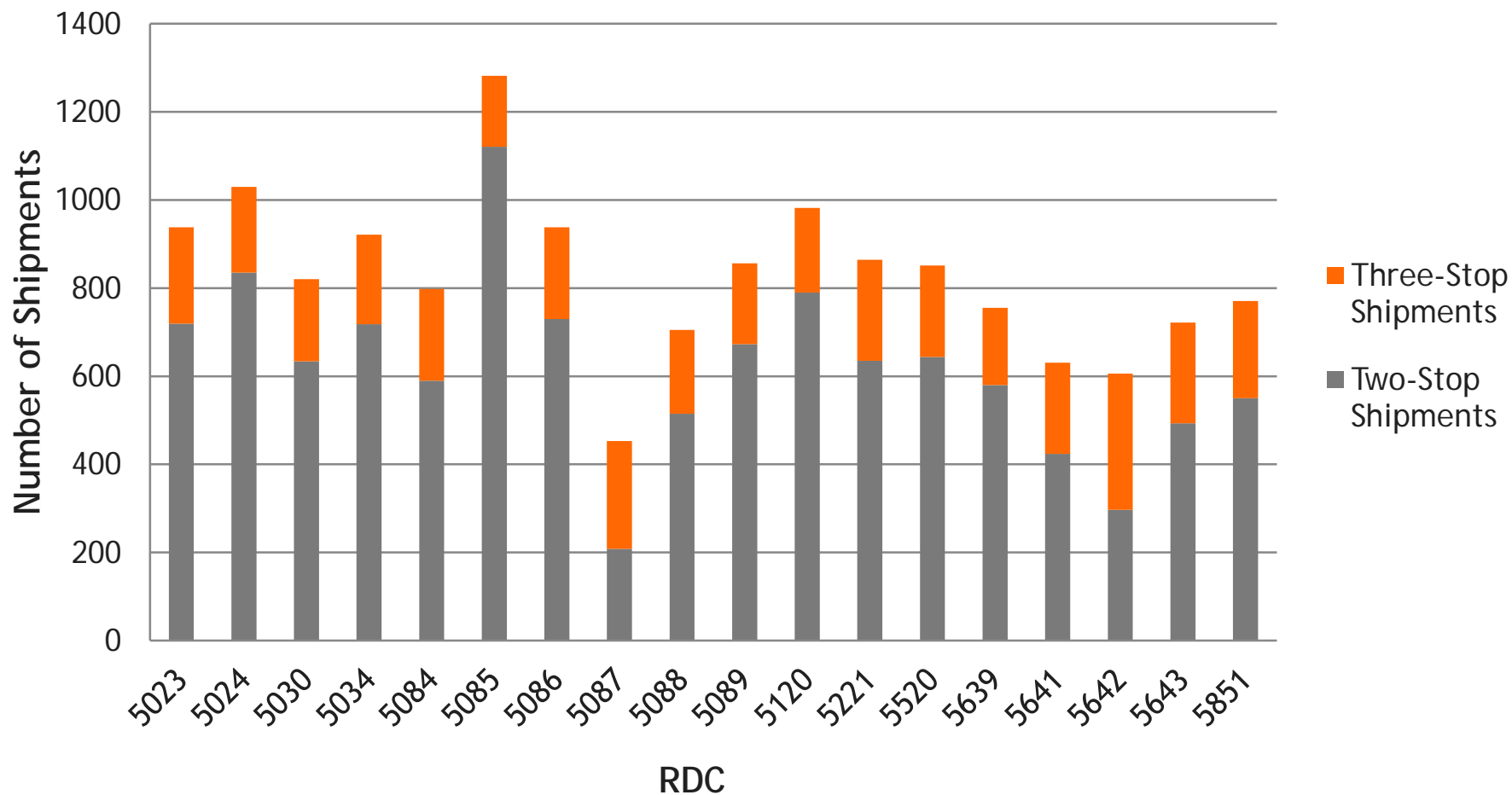
## Total Shipments Per RDC





# ANALYSIS

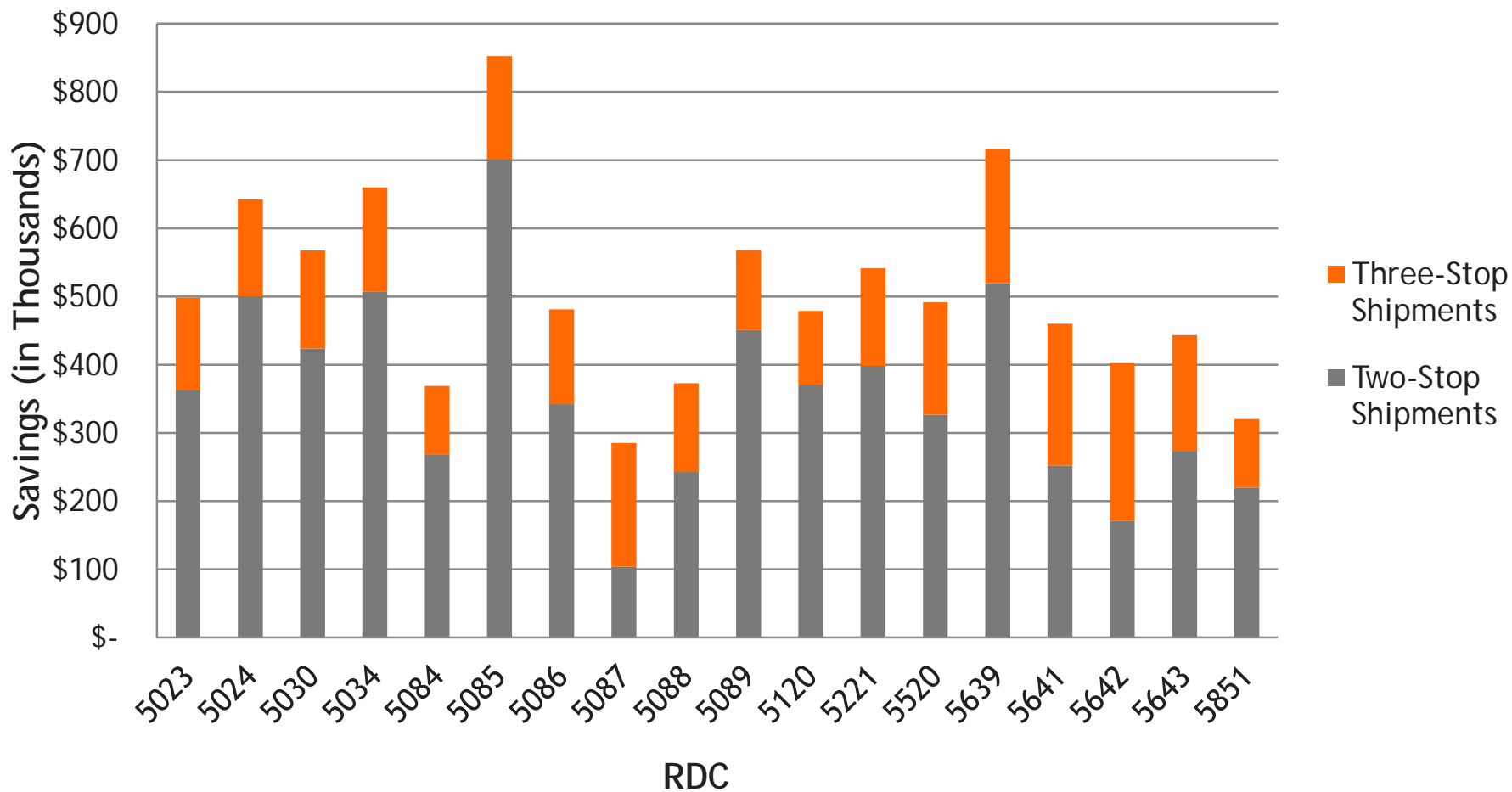
## Total Number of Multi-Stop Shipments Per RDC





# ANALYSIS

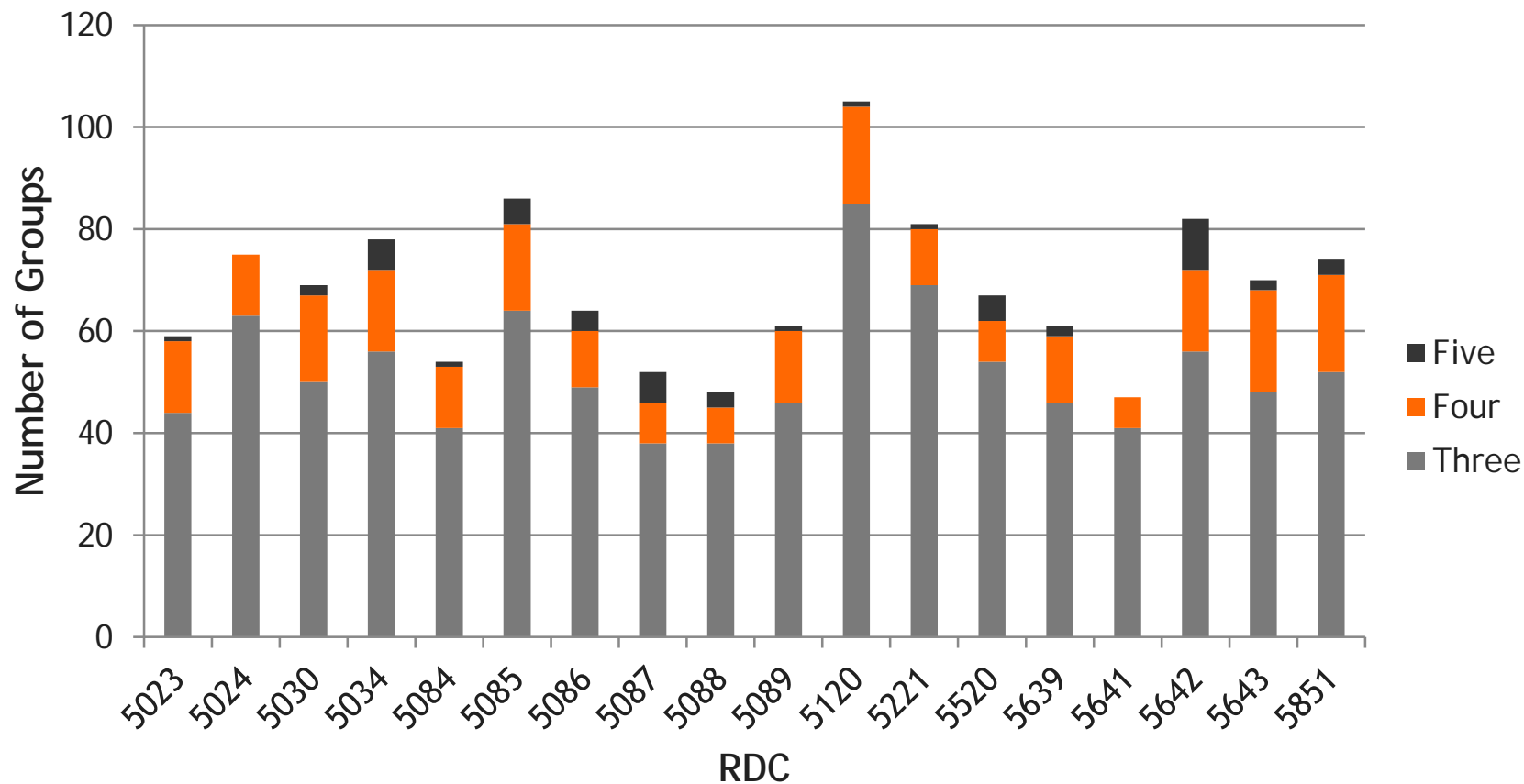
## Total Savings Per RDC





# ANALYSIS

## Group Sizes per RDC





# HIGH FREQUENCY OPTIMIZATION MODEL



$$\max \left\{ \left( \sum_i \sum_j s_{i,j} x_{i,j} - \lambda_1 * \sum_a \sum_b y_{a,b} \right) + \left( \sum_k \sum_l \sum_m s_{k,l,m} x_{k,l,m} - \lambda_2 * \sum_c \sum_d \sum_e y_{c,d,e} \right) \right\}$$

s.t.

$$\sum_i \sum_j x_{i,j,k} + \sum_j \sum_l x_{j,k,l} + \sum_l \sum_m x_{k,l,m} + \sum_j x_{j,k} + \sum_l x_{k,l} \leq 1 \forall k \quad (1)$$

$$\sum_{v(i)=a} \sum_{v(j)=b} x_{i,j} + \sum_{v(i)=b} \sum_{v(j)=a} x_{i,j} \leq c_1 * y_{a,b} \quad (2)$$

$$\sum_{v(k)=c} \sum_{v(l)=d} \sum_{v(m)=e} x_{k,l,m} + \sum_{v(k)=c} \sum_{v(l)=e} \sum_{v(m)=d} x_{k,l,m} + \sum_{v(k)=d} \sum_{v(l)=c} \sum_{v(m)=e} x_{k,l,m} + \dots$$

$$\sum_{v(k)=d} \sum_{v(l)=e} \sum_{v(m)=c} x_{k,l,m} + \sum_{v(k)=e} \sum_{v(l)=c} \sum_{v(m)=d} x_{k,l,m} + \sum_{v(k)=e} \sum_{v(l)=d} \sum_{v(m)=c} x_{k,l,m} \leq c_2 * y_{c,d,e} \quad (3)$$

$$x_{i,j} \in (0,1) \quad (4)$$

$$x_{k,l,m} \in (0,1) \quad (5)$$

$$y_{a,b} \in (0,1) \quad (6)$$

$$y_{c,d,e} \in (0,1) \quad (7)$$